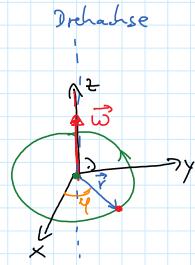
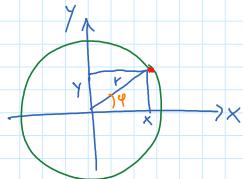


$$\vec{v} = \begin{pmatrix} 3 \\ 2 \\ 4 \end{pmatrix}$$



$$\vec{r} = \begin{pmatrix} r \cdot \cos \varphi \\ r \cdot \sin \varphi \end{pmatrix}$$

$$\boxed{\varphi = \omega \cdot t}$$



$$\omega = \frac{\Delta \varphi}{\Delta t}$$

$$x = r \cdot \cos \varphi$$

$$y = r \cdot \sin \varphi$$

Lineare Bew.

Weg  $x$

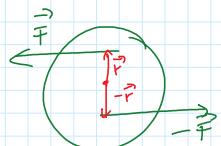
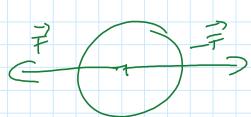
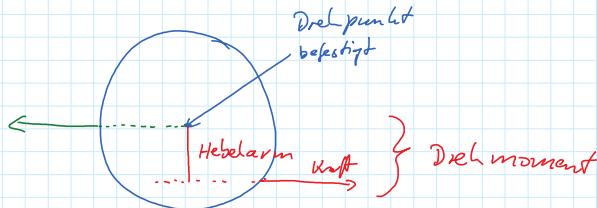
Geschr.  $\vec{v}$

Kreisbewegung

Winkel  $\varphi$

Winkelgeschw.  $\vec{\omega}$

Kraft  $\rightarrow$  Drehbeschleunigung  $\vec{\alpha}$    Kraft  $\rightarrow$  Drehmoment  $\rightarrow$  Änderung der Winkelgeschw.



$$\begin{pmatrix} a_1 \\ a_2 \\ a_3 \end{pmatrix} \times \begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix}$$

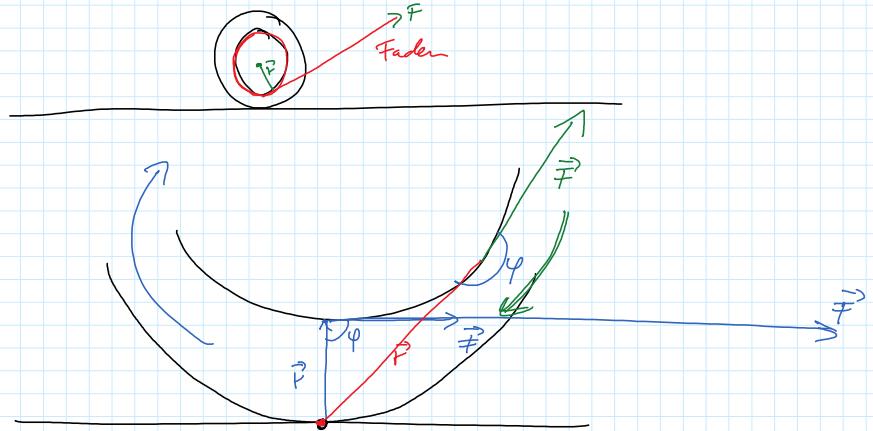
$$\begin{array}{ccc} a_1 & \cancel{a_2} & b_1 \\ \cancel{a_2} & a_3 & \cancel{b_2} \\ a_3 & b_1 & b_2 \end{array}$$

$$|\vec{a} \times \vec{b}| = |\vec{a}| |\vec{b}| \sin \varphi$$

$$\text{Drehmoment} \quad \vec{N} = \vec{r} \times \vec{F} = r \cdot \vec{r} \cdot \sin \varphi (\vec{r}, \vec{F})$$

Versuch · Garnrolle





Drehpunkt  
= Auflagepunkt

folgsame Rolle

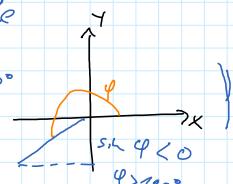
$$\varphi \leq \pi \rightarrow \sin \varphi > 0$$

Drehmomant > 0 in die Bildebene

stornende Rolle

$$\varphi > \pi \text{ bzw. } 180^\circ$$

$$\rightarrow \sin \varphi < 0$$



Drehmom. < 0 → aus der

Bildebene

Drehmoment und Trägheitsmoment

$$J = r^2 \cdot m$$

$$J = 0.18 \text{ kg m}^2$$

$$J_2$$

1. Umdrehung  
2.

3

4. Teil

12 sek  
17 sek

21

24 1. Teil

6 sek

9

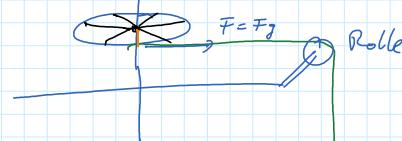
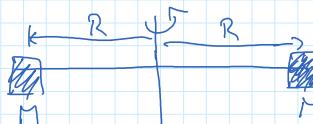
11

12 =  $t_1$

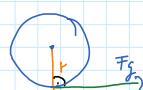
24 =  $t_{12}$

Offen:  
Repetitorium der  
Experimentalphysik

Versuch 2.1.



kleine Schale  
Von  
oben



$$\text{Drehmoment } \vec{N} = \vec{r} \times \vec{F} = r \cdot F \begin{pmatrix} \sin 90^\circ \\ 1 \end{pmatrix}$$

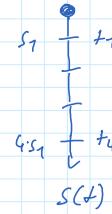
$$t_4 = 2 \cdot t_1$$

$$\text{Wobei } \varphi_4 = 4 \cdot \varphi_1$$

$$4 \times 360^\circ \quad 1 \times 360^\circ$$

$$\varphi(t) \propto t^2$$

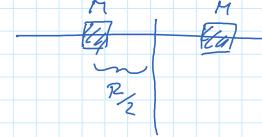
vg l. freier Fall



$$s(t) \propto t^2$$

gleichmäßige Beschleunigung

2. Teil:  $R \mapsto \frac{R}{2}$



$$\text{def: } J = M \cdot R^2$$

$$\downarrow \quad \downarrow \\ 2M \quad \frac{R^2}{4}$$

$$\Rightarrow J_{2.\text{Teil}} = \frac{1}{4} J_{1.\text{Teil}} \text{ d. Verhältnis}$$

Trägheitsmoment nur noch  $\frac{1}{4}$

$$\text{neue } t_4^1 (4U) = t_1^1 (1U)$$

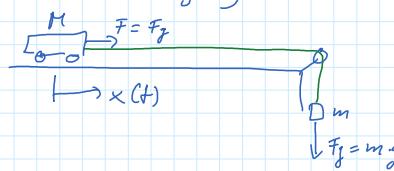
$$\Rightarrow \varphi(t) \propto \frac{1}{2} t$$

$$\Rightarrow \text{Bewegungsgl. d. Rotation} \quad \varphi(t) = \frac{1}{2} \frac{N}{J} \cdot t^2 = \frac{1}{2} \alpha t^2$$

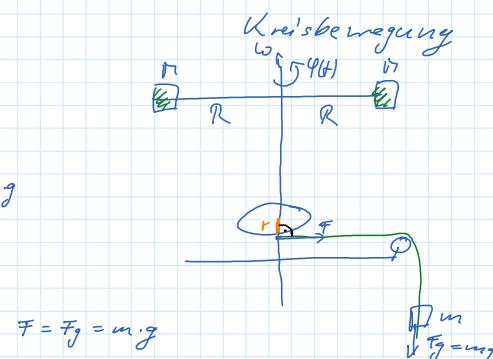
Winkelgesch.

Die gleichmäßige Beschleunigung

Lin. can. Bewegung



Kreisbewegung



Masse M

Trägheitsmoment

$$J = M \cdot R^2 \quad (3.22a)$$

(hier:  $2M \cdot R^2$   
weil 2 Massen!)

$$\text{Kraft} \quad \vec{F} = \vec{p} = M \cdot \vec{v} = M \cdot \vec{a}$$

Drehmoment

$$\vec{N} = \vec{r} \times \vec{F} = J \cdot \vec{\omega} = J \cdot \vec{\alpha}$$

$$\vec{N} = \vec{r} \times \vec{F} \quad (3.22b)$$

$$N = r \cdot F \cdot \sin \frac{1}{2} (F, \vec{r})$$

$$\Rightarrow N = r \cdot F$$

$$\text{Impuls} \quad \vec{p}(t) = M \cdot \vec{v}(t)$$

$$\text{Drehimpuls} \quad \vec{L}(t) = J \cdot \vec{\omega}(t)$$

$$(3.22c)$$

$$\text{Beschleunig.} \quad \vec{a}(t) = \frac{\vec{p}(t)}{M}$$

Winkelbesch.

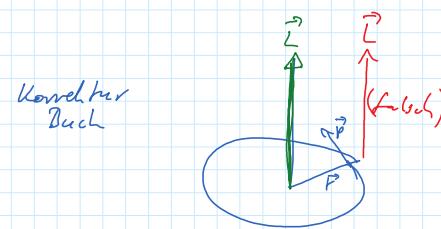
$$\vec{L}(t) = \frac{\vec{N}(t)}{J} \quad (3.22d)$$

$$\text{Geschwindig.} \quad v(t) = a \cdot t + v_0$$

Winkelgeschw.

$$\omega(t) = d \cdot t + \omega_0 \quad (3.21)$$

Strecke  $x(t) = \frac{1}{2} a t^2 + v_0 t + x_0$  Winkel  $\varphi(t) = \frac{1}{2} \alpha t^2 + \omega_0 t + \varphi_0$  (3.214)



Impulserhaltung  $\vec{F} = 0$   
 $\vec{p} = \vec{p} = \text{const}$

Konduktur  
Dreh   
 $\vec{L} \rightarrow \vec{L} = \text{const}$

Drehimpulserhaltung  $\vec{N} = 0$  (Kern  
Drehmom.)  
 $\vec{N} = \vec{L} = \text{const}$

Drehimpuls erhalten  
falls kein Drehmoment

Energie  $E_{\text{kin}} = \frac{1}{2} M v^2$  Rot. Energie  $\cdot E_{\text{rot}} = \frac{1}{2} J \omega^2$