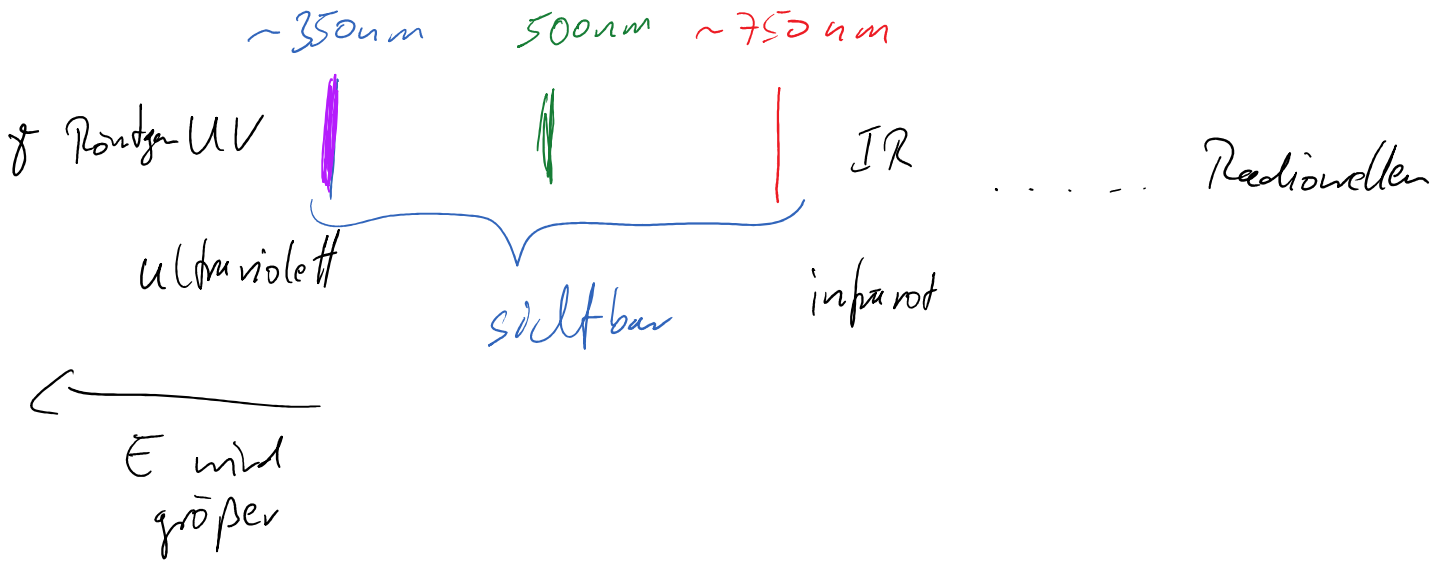
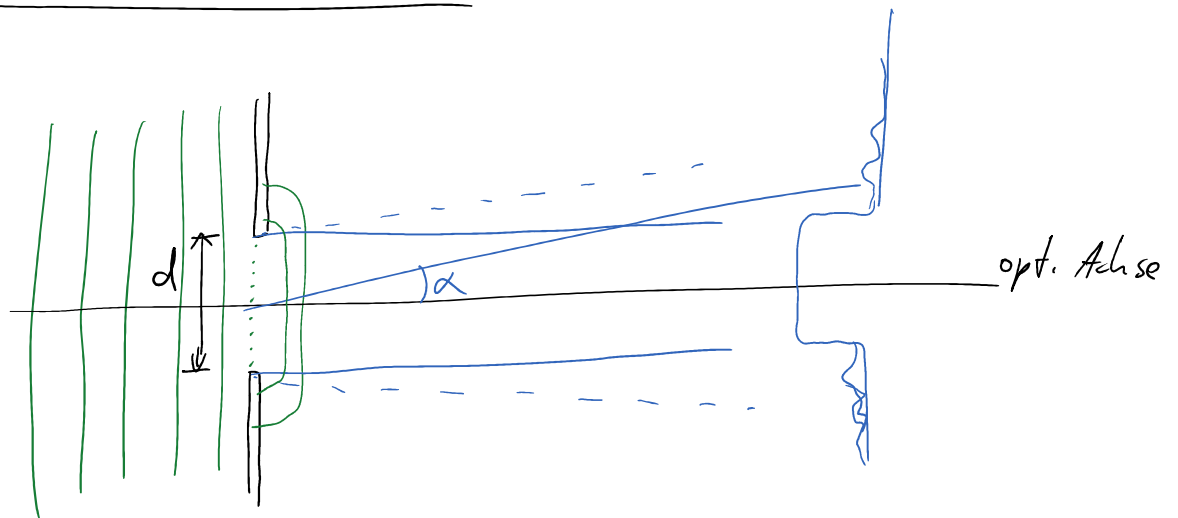


Spektrum



Lichtstrahlen / -bündel



$$d = \frac{\lambda}{\sin \alpha} \approx \frac{600 \text{ nm}}{10^{-3}} \approx \underline{\underline{0.6 \text{ mm}}}$$

$\alpha = 1 \text{ mrad}$ $\frac{1}{2} \text{ mm}$



Brechungsindex n

$$c_0 = 299\,792\,458 \frac{\text{m}}{\text{s}} \pm 0 \quad \text{Lichtgeschw. im Vakuum }$$

$30 \frac{\text{cm}}{\text{ns}}$ $\uparrow$
fixiert den Meter
im SI

Im Medium (Luft, Wasser, Glas, ...):

$c < c_0$ lokale Lichtgeschw. ist kleiner

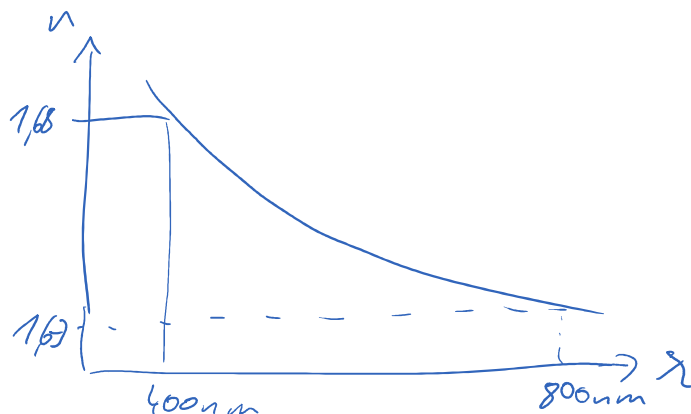
$$\boxed{c = \frac{c_0}{n}}$$

$$\text{H}_2\text{O}: n = 1,33$$

Brechungsindex n = Materialeigenschaft

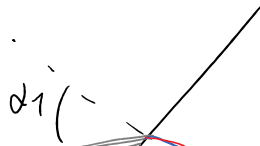
Dispersion:

n hängt von
 λ ab

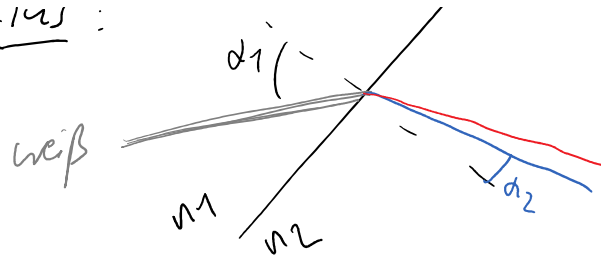


Regenbogen im Prisma
wg. Dispersion d. Glases

Snellius:



Snellius :



$$n_1 \sin \alpha_1 = n_2 \sin \alpha_2$$

Lichtstrom : Lumen lm

Lichtstärke : Lichtstrom in einem Raumwinkel



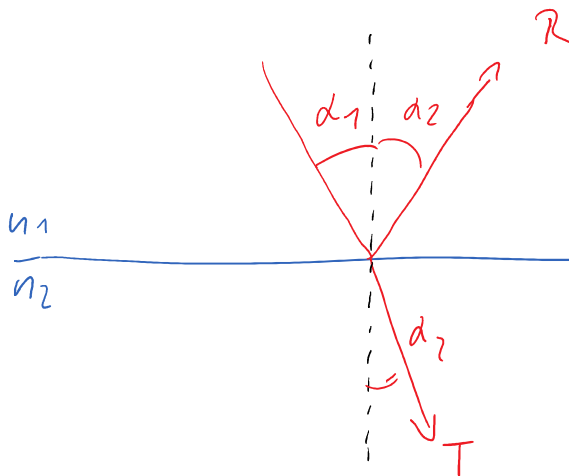
Candela cd

gesamter Raumwinkel
(Kugeloberfläche)

$$= 4\pi \text{ sr}$$

($\neq$ Winkel im Kreis (2D):
 $360^\circ = 2\pi \text{ rad}$)

Reflexion & Transmission



$$n_1 \sin \alpha_1 = n_2 \sin \alpha_2$$

Fresnel'sche Formeln

Fresnel'sche Formeln

für $d = 0$ (senkrechte Einfall):

$$R = \frac{I_{\text{refl.}}}{I_{\text{ein}}} = \frac{(n_2 - n_1)^2}{(n_1 + n_2)^2}$$

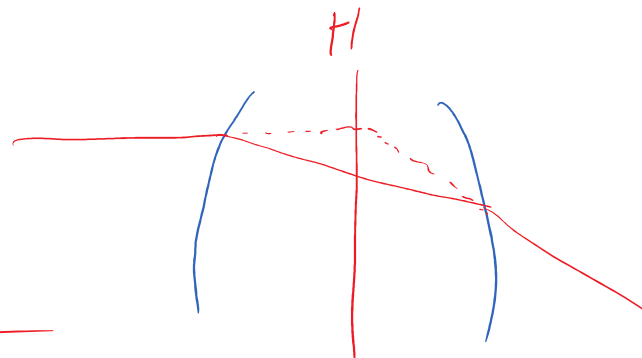
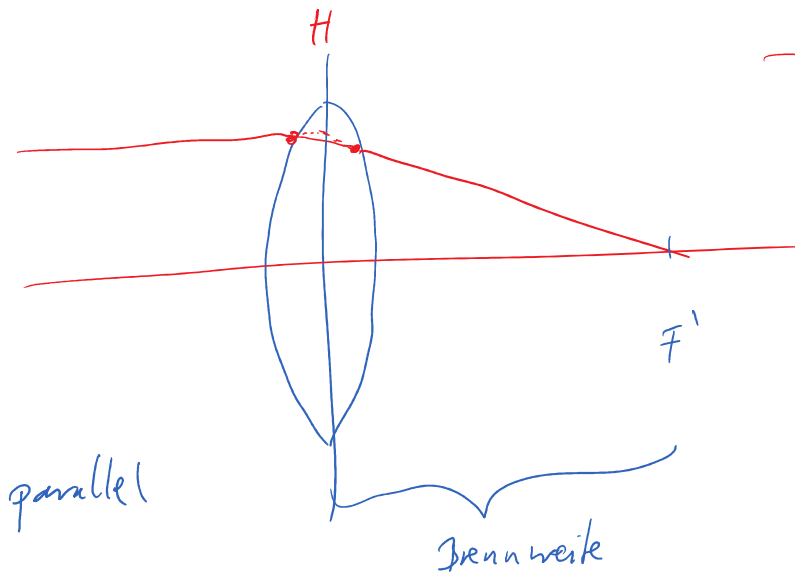
f. Luft - Glas : 4%

$$T = \frac{I_{\text{trans}}}{I_{\text{ein}}} = \frac{4n_1 n_2}{(n_1 + n_2)^2}$$

$R + T = 1$ (falls keine Absorption, Streuung)

Total reflexion ✓

Abbildung v. Linsen



Näherung : 1 Brechung an Hauptebene
statt 2x an den Grenzflächen (= phys.!)

1:1 ... d. l. ... bilinear ... inhomogen

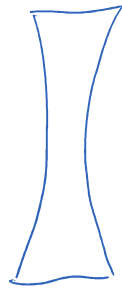
bikonvex



plankonvex



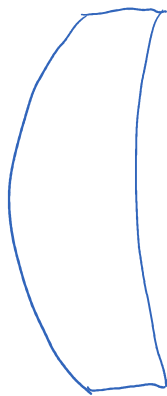
bikonkav



plankonkav

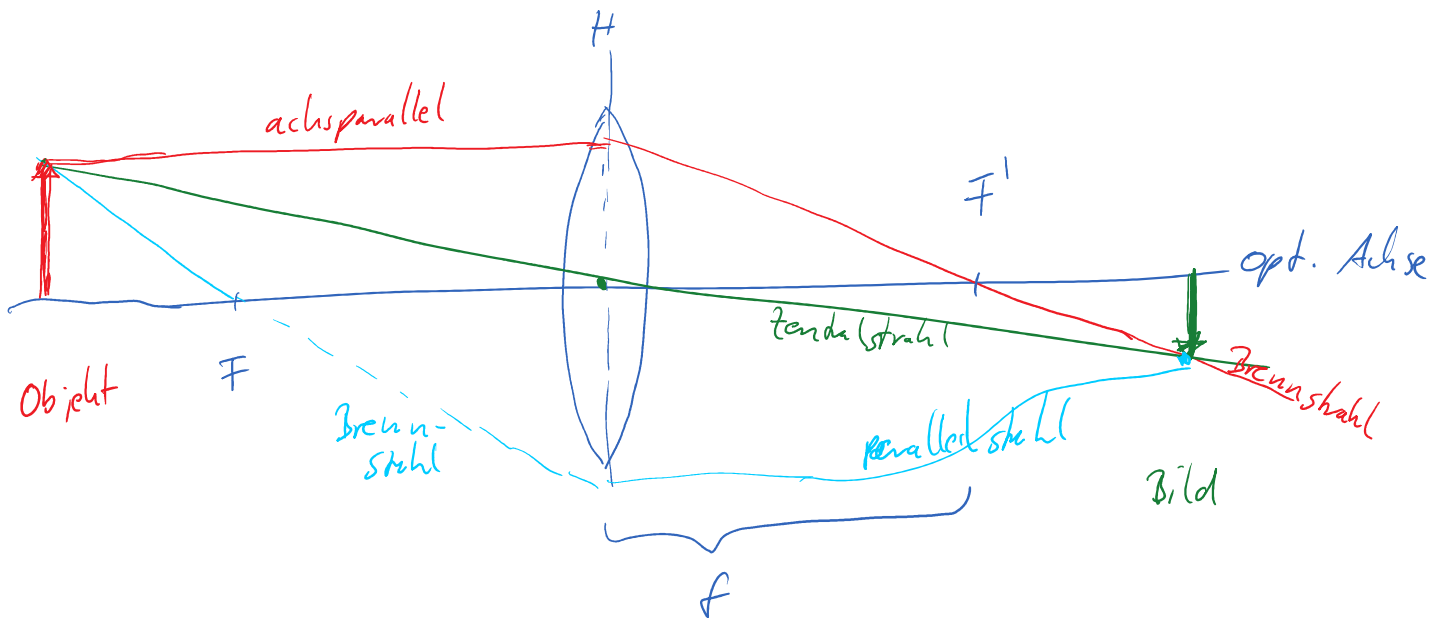


konvex-konkav



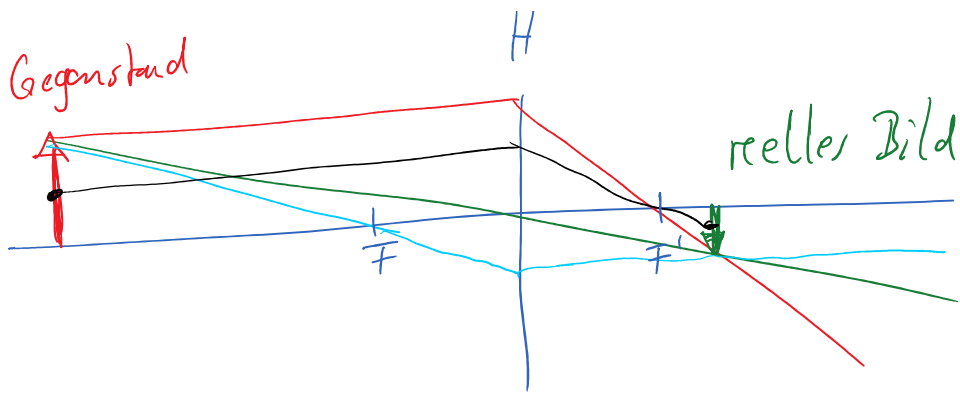
= physikalische Realisierung

Näherung : Hauptebene + Brennweite



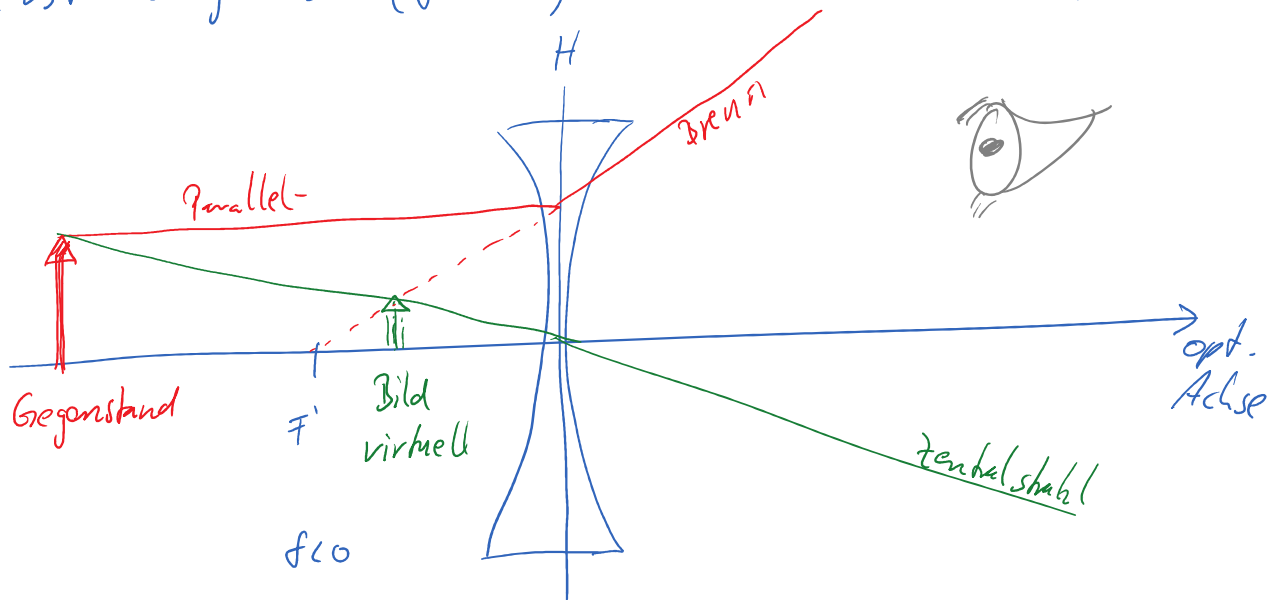
Gegenstand



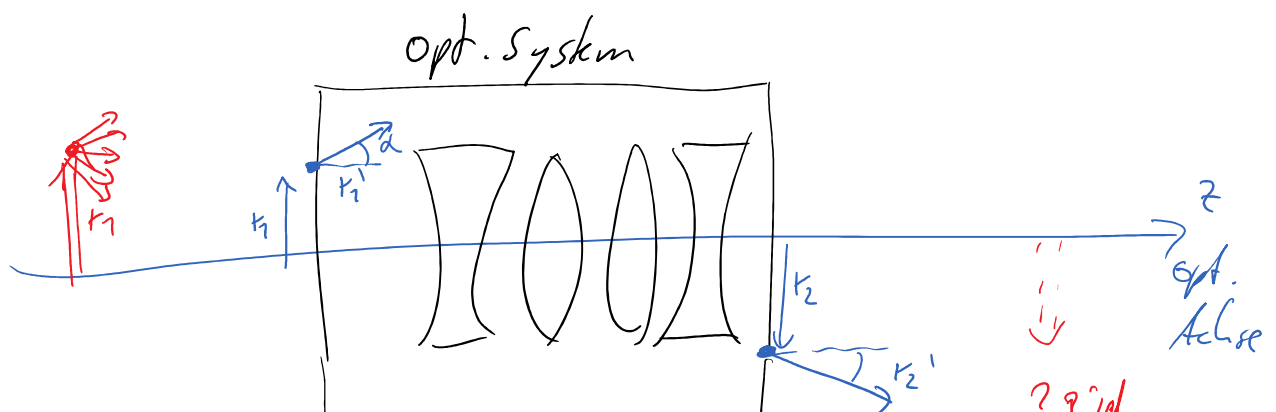


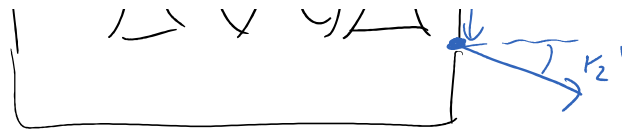
achsenparallel $\Leftrightarrow$ Brennpunkt
 zentralstabil = gerade

Zerstreuungslinse ($f < 0$) & virtuelles Bild



ABCD Matrix - Formalismus





↘ Achse
? g. id

$$\sin \alpha \approx \alpha = r' = \frac{dr}{dz}$$

$$\begin{pmatrix} r_1 \\ r_1' \end{pmatrix} \xrightarrow{?} \begin{pmatrix} r_2 \\ r_2' \end{pmatrix}$$

ABCD Matrix
ray transfer matrix

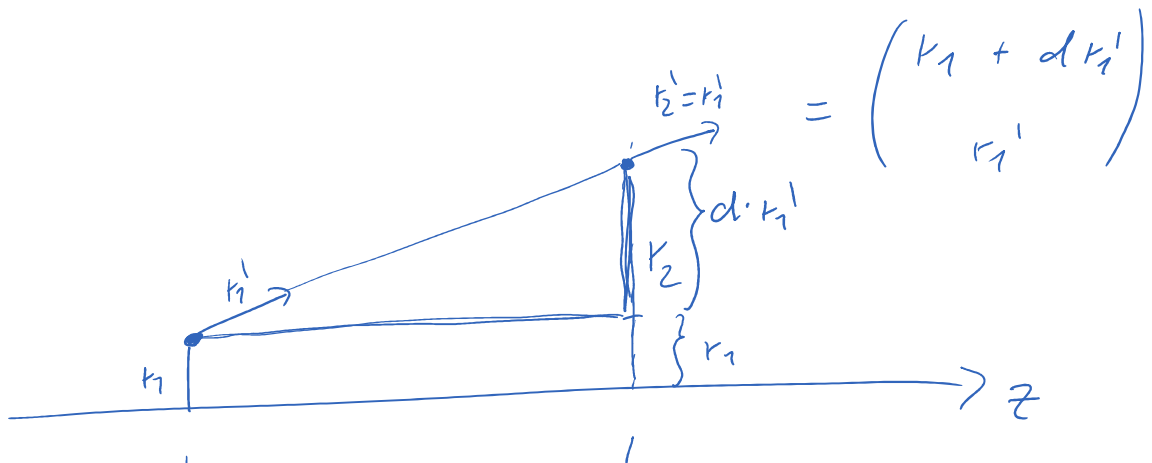
$$\begin{pmatrix} A & B \\ C & D \end{pmatrix} \quad 2 \times 2 \text{ Matrix}$$

$$\begin{pmatrix} r_2 \\ r_2' \end{pmatrix} = \begin{pmatrix} A & B \\ C & D \end{pmatrix} \cdot \begin{pmatrix} r_1 \\ r_1' \end{pmatrix} = \begin{pmatrix} A \cdot r_1 + B \cdot r_1' \\ C \cdot r_1 + D \cdot r_1' \end{pmatrix}$$

Bsp.

Wegstrecke d: $S = \begin{pmatrix} A & B \\ C & D \end{pmatrix} = \begin{pmatrix} 1 & d \\ 0 & 1 \end{pmatrix}$ Wegstrecke d

$$\begin{pmatrix} r_2 \\ r_2' \end{pmatrix} = \begin{pmatrix} 1 & d \\ 0 & 1 \end{pmatrix} \begin{pmatrix} r_1 \\ r_1' \end{pmatrix} = \begin{pmatrix} 1 \cdot r_1 + d \cdot r_1' \\ 0 \cdot r_1 + 1 \cdot r_1' \end{pmatrix}$$

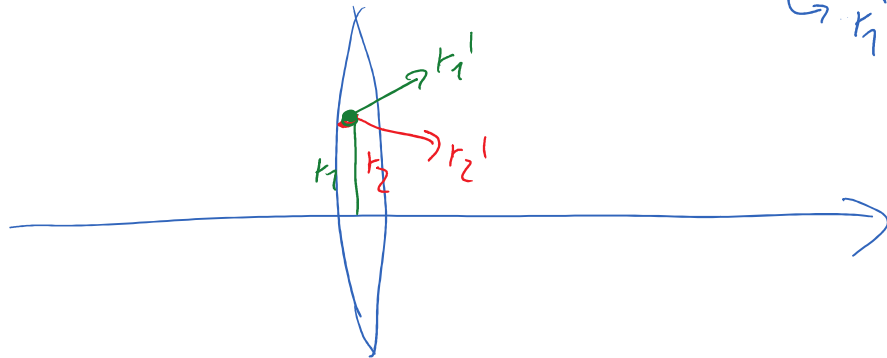




Linse f: $L = \begin{pmatrix} A & B \\ C & D \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ -\frac{1}{f} & 1 \end{pmatrix}$

$$\begin{pmatrix} r_2 \\ r_2' \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ -\frac{1}{f} & 1 \end{pmatrix} \begin{pmatrix} r_1 \\ r_1' \end{pmatrix} = \begin{pmatrix} r_1 \\ -\frac{r_1}{f} + r_1' \end{pmatrix}$$

$$\hookrightarrow r_2' = r_1' - \frac{r_1}{f}$$



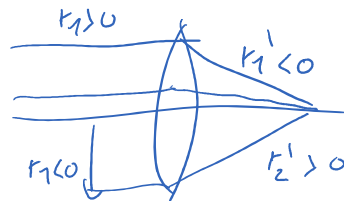
$$r_2' = r_1' - \frac{r_1}{f}$$

Zentralstrahl: $r_1 = 0$

$r_2' = r_1'$
wird nicht
gebrochen

Parallelstrahl: $r_1' = 0$

wird prop. zu r_1 gebrochen





$$(M) = (L_2)(d_1)(L_1) = \begin{pmatrix} 1 & 0 \\ -\frac{1}{f_2} & 1 \end{pmatrix} \begin{pmatrix} 1 & d_1 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ -\frac{1}{f_1} & 1 \end{pmatrix}$$

matrix-multiplication

$\begin{pmatrix} A_{tot} & B_{tot} \\ C_{tot} & D_{tot} \end{pmatrix}$ des Gesamtsystems