

Photonics

Q-Ex-2

Randolf Pohl
SoSe 2023

Tue 12:15-13:45 HS KPH

Thu 12:15-13:45 HS KPH

Thu Apr. 27: Sem 1 KPH

pohl@uni-mainz.de

Contents of this lecture

(dynamic, this is just a proposal!)

- Intro (Refresh)
 - Atomic physics, light-atom interaction (optical Bloch equations, Rabi oscillations, Ramsey method)
- Absorption and Emission of light
 - Black body radiation, Einstein coefficients
 - classical and semi-classical description
- Spectral lines:
 - natural line width, line strength
 - AC Stark shift (light shift), DC Stark shift, Zeeman shift,
 - broadening mechanisms: Doppler, time-of-flight, pressure, ...
- Lasers
 - types of lasers: Ruby, HeNe, YAG, Ti:Sapphire, diode laser, fiber laser, ...
 - principles of operation, technical realization
- Resonators / Cavities
- Gaussian optics
- Laser stabilization
 - locking techniques: side-of-fringe, Hänsch-Couillaud, Pound-Drever-Hall, ...
- Optical devices: EOM, AOM, beat signals, mixer, spectrum analyzer, ...
- Frequency comb
- Non-linear optics: SHG, THG, SFG, DFG, OPO, ...
- Laser spectroscopy: (Saturated) absorption spectroscopy, Doppler-free spectroscopy,
- Trapping of atoms and ions (MOT, Penning traps,)
- Precision measurements and fundamental constants
-
- And whatever else YOU want to hear about

Literature

- * W. Demtröder, Laser Spectroscopy 1 & 2
(German version online on library web site)
- * C.J. Foot: Atomic Physics
- * H.J. Metcalf & P. van der Straten: Laser Cooling and Trapping
- * P. van der Straten & H.J. Metcalf: Atoms and Molecules Interacting with Light
- * A. Siegman: Lasers
- * R. Boyd: Nonlinear Optics
- * Saleh & Teich: Fundamentals of Photonics
- * M. Fox: Quantum Optics – an Introduction
I will try to mention which book I used to prepare a topic

Proton radius and Rydberg constant from electronic and muonic atoms

Randolf Pohl

Johannes Gutenberg-Universität Mainz
Institut für Physik, QUANTUM und PRISMA

Max-Planck Institute of Quantum Optics



Photonics, 18. Apr. 2023

Outline

- Muonic atoms

as a probe of nuclear physics (**charge radii**, magnetization radii, polarizabilities, ...)

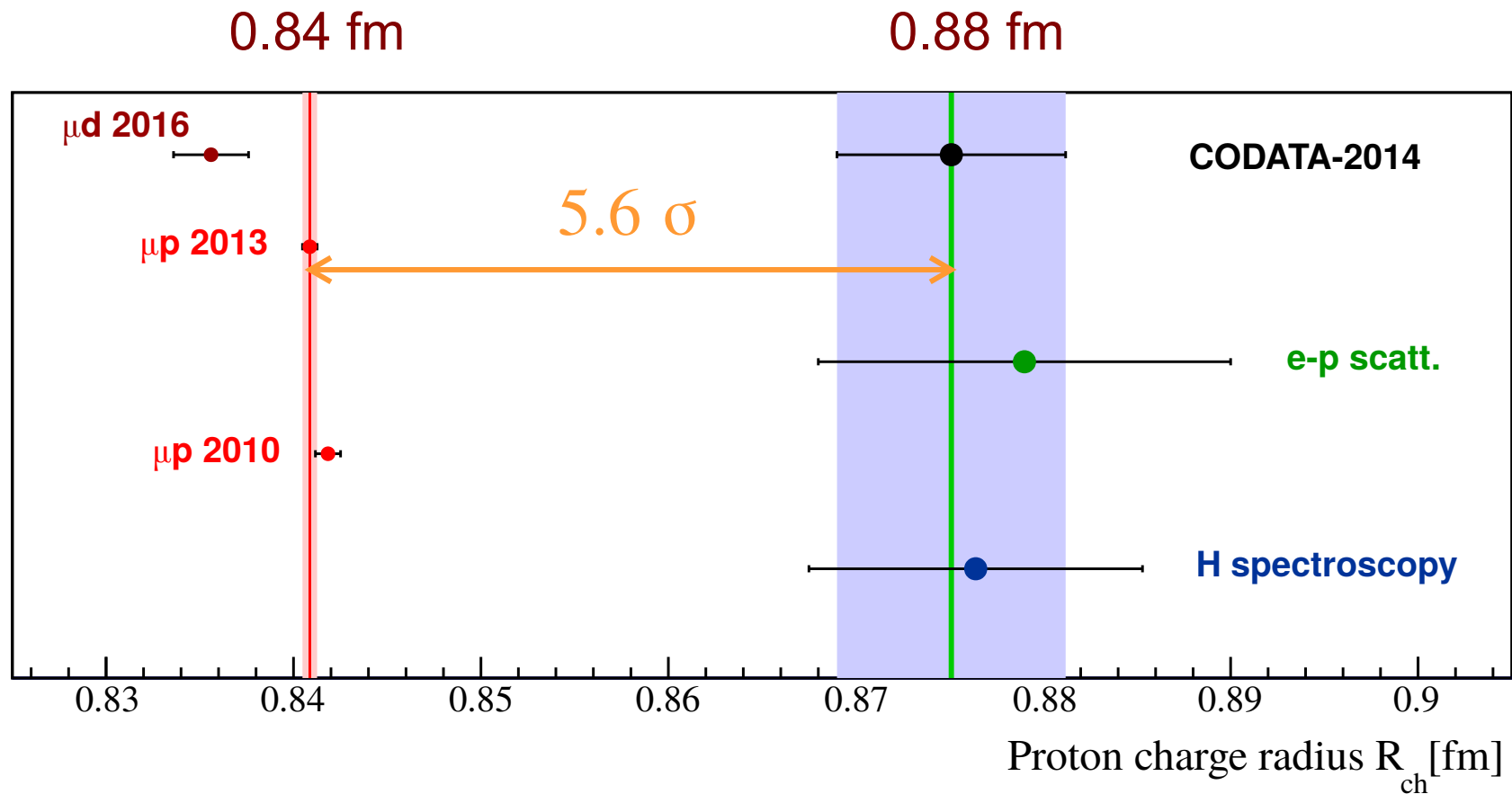
- The “Proton Radius Puzzle”

- Rydberg constant

key parameter to check **atomic physics** part of the discrepancy

- Muonic helium, later Li, Be, T?

The “Proton Radius Puzzle”



Measuring R_p using **electrons**: 0.88 fm (\pm 0.7%)
using **muons**: 0.84 fm (\pm 0.05%)

μd 2016: RP et al (CREMA Coll.) Science 353, 669 (2016)

μp 2013: A. Antognini, RP et al (CREMA Coll.) Science 339, 417 (2013)

nature

OIL SPILLS
There's more to come

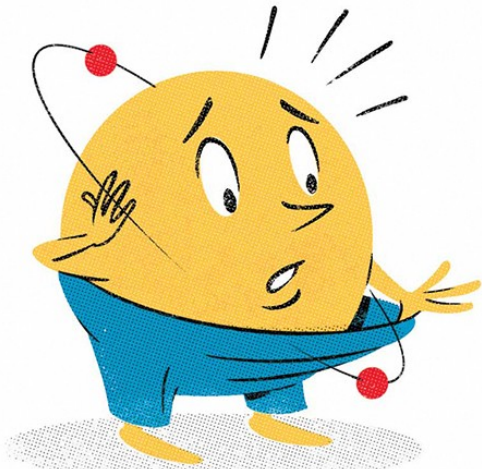
PLAGIARISM
It's worse than you think

CHIMPANZEES
The battle for survival

SHRINKING THE PROTON

New value from exotic atom trims radius by four per cent

NATURE JOBS
Researchers for hire



NY Times

NEUROSCIENCE People Who Remember Everything
MEDICINE A New Way to Tame Cancer
INFOTECH The Benefits of Video Games (Really)

SCIENTIFIC AMERICAN

ScientificAmerican.com

The Proton Problem

Could scientists be seeing signs of a whole new realm of physics?



FEBRUARY 2014

INSIDE THE NEANDERTHAL BRAIN
First hints of how their minds differed from ours

NewScientist

WEEKLY July 20 - 26, 2013

TINY PARTICLE BIG PROBLEM

The humble proton is nothing like we expected



No2926 US\$5.95 CAN\$5.95



EVOLUTION IN MINIATURE

It works differently if you're small

Science and technology news www.newscientist.com US jobs in science

CAR HACKING
Could cyberattackers arrange a crash?

LONG STORY
How the Diplodocus got its neck

WINDS OF CHANGE
Gale-force warnings from Antarctica

nature

OIL SPILLS
There's more to come

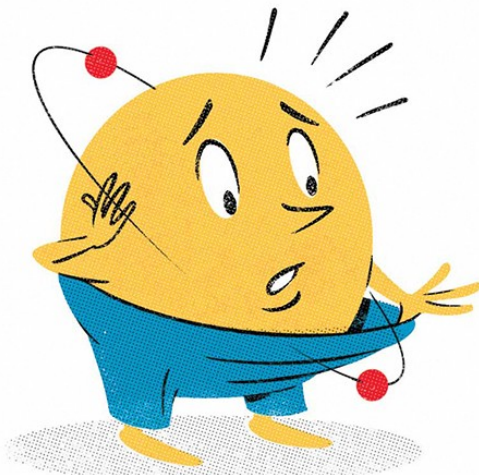
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ScientificAmerican.com

The Proton Problem

Could scientists be seeing signs of a whole new realm of physics?

Jan Bernauer & RP,
April 2014

INSIDE THE NEANDERTHAL BRAIN
First hints of how their minds differed from ours

NewScientist

APRIL 2014

ARTENBILDUNG
Buntbarsche: Evolution Im Zeitraffer

QUANTENTHEORIE
Ist die Natur digital oder analog?

KREBSTHERAPIE
Mit Stromstößen gegen Tumoren

ARCHÄOLOGIE
Die Erfindung der Landwirtschaft

Das Proton-Paradoxon

Widersprüchliche Größenmessungen deuten auf eine neue Physik

CAR HACKING
Could cyberattackers arrange a crash?

LONG STORY
How the Diplodocus got its neck

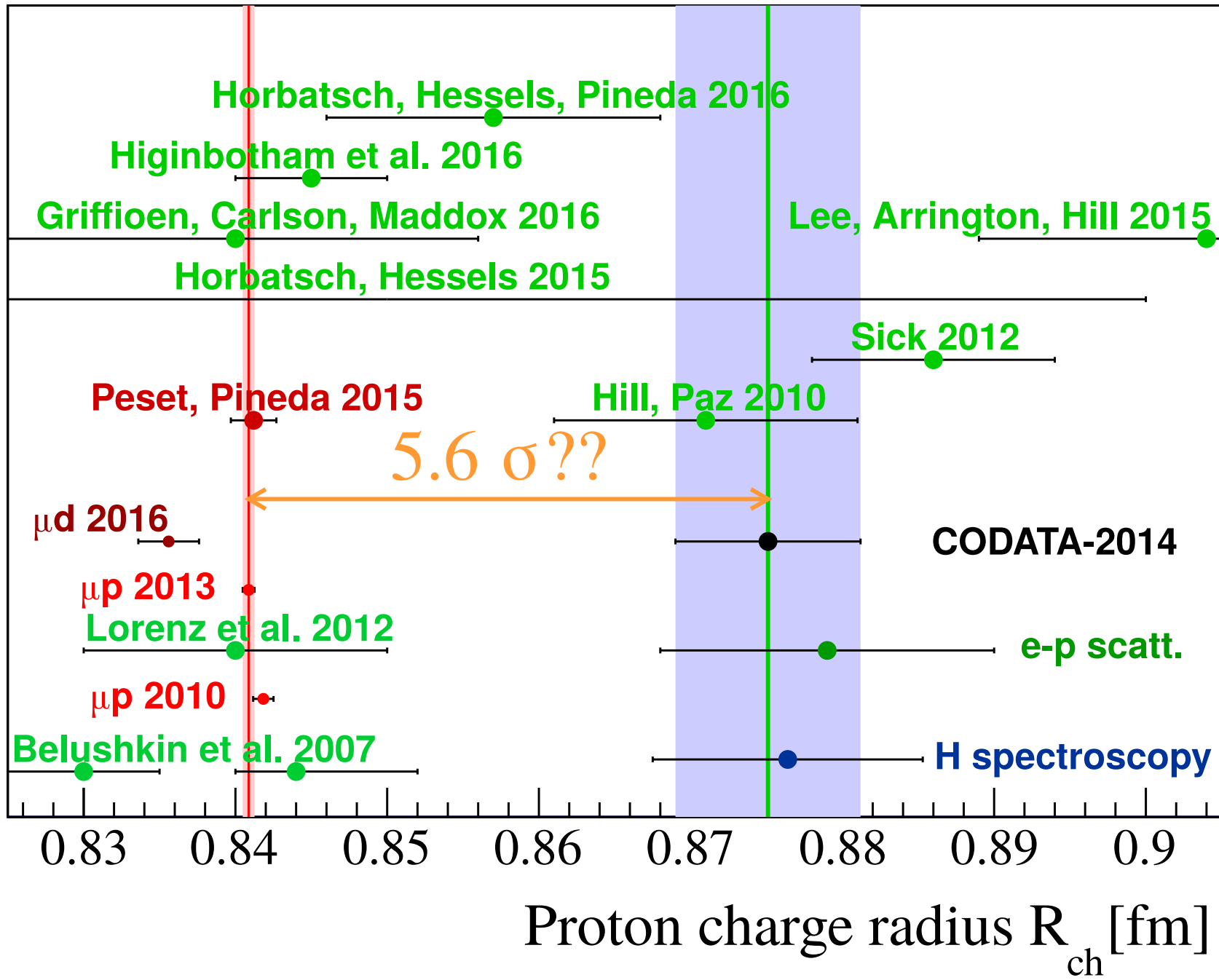
WINDS OF CHANGE
Gale-force warnings from Antarctica

Spektrum

DER WISSENSCHAFT

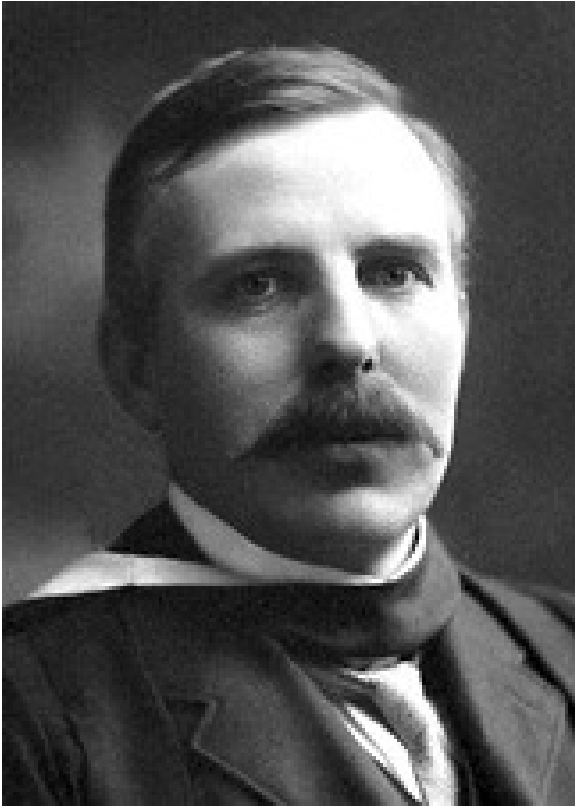
www.spektrum.de

A “Proton Radius Puzzle” ??



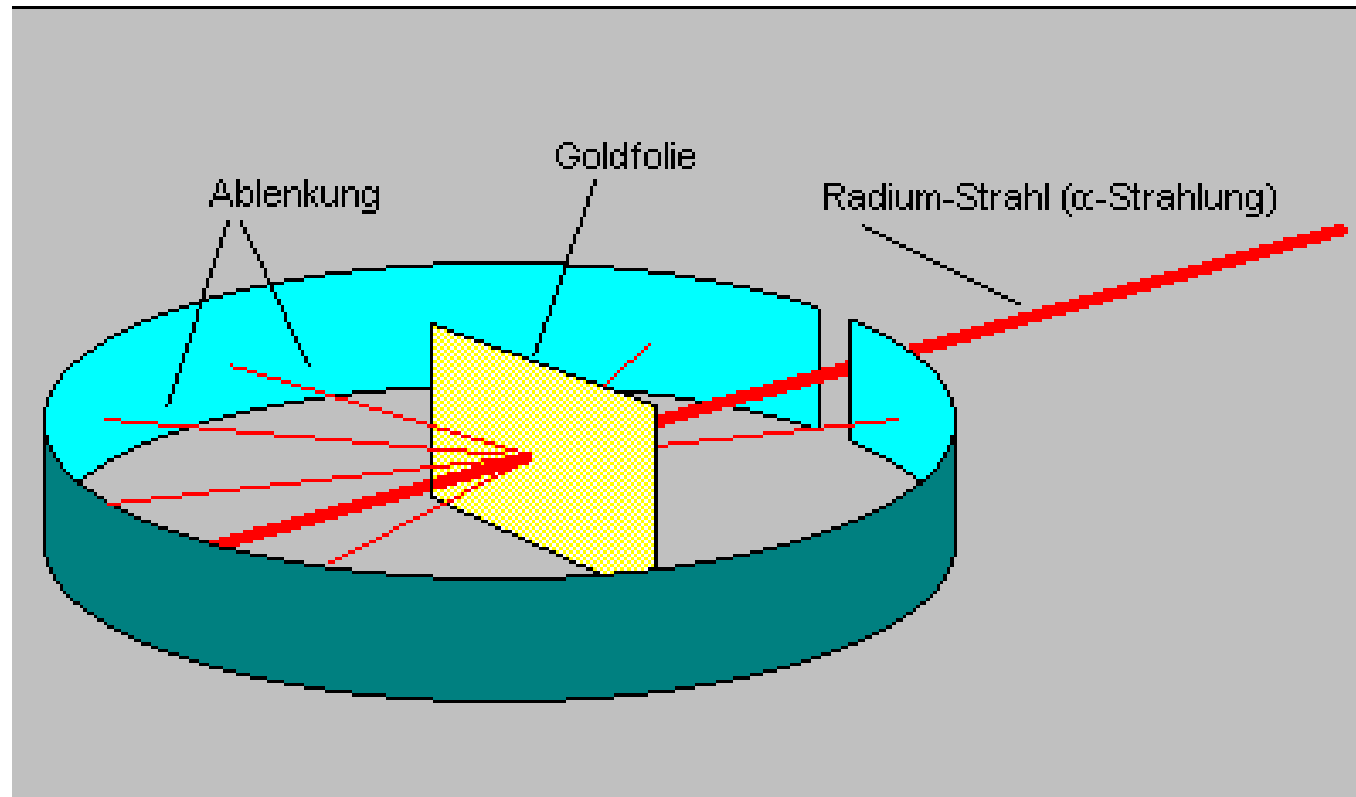
Intro: Atomic and nuclear physics

Ernest Rutherford – 1911



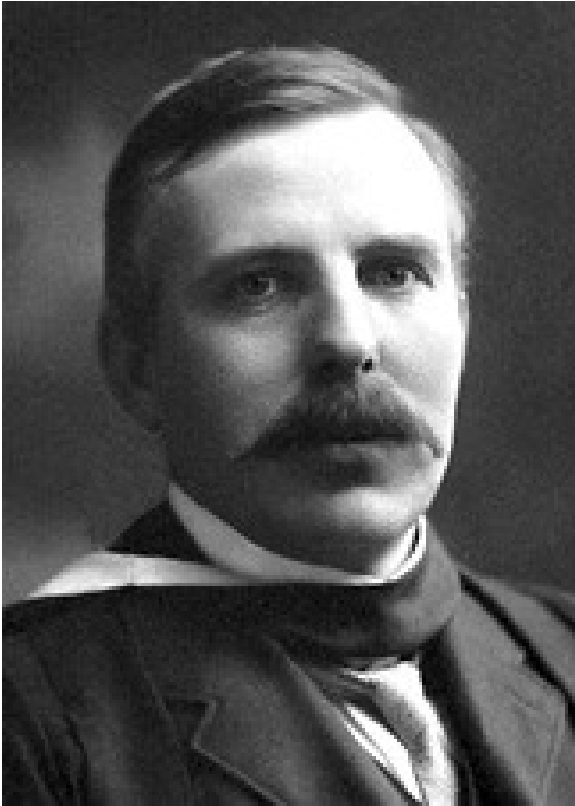
1871 – 1937
Nobel prize 1908

Rutherford shoots alpha particles onto a thin gold foil.

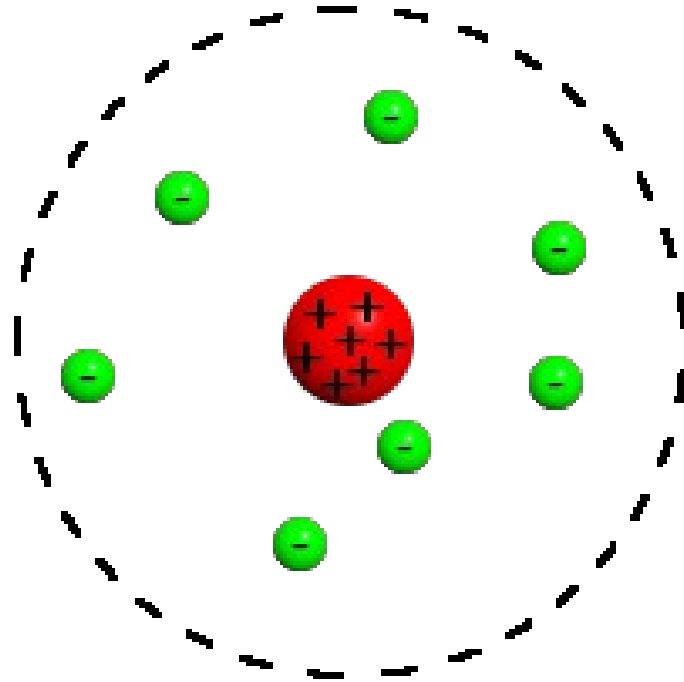


Most of the alpha particles pass the gold foil.
A few, however, are deflected by very large angles.

Ernest Rutherford – 1911

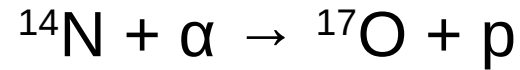
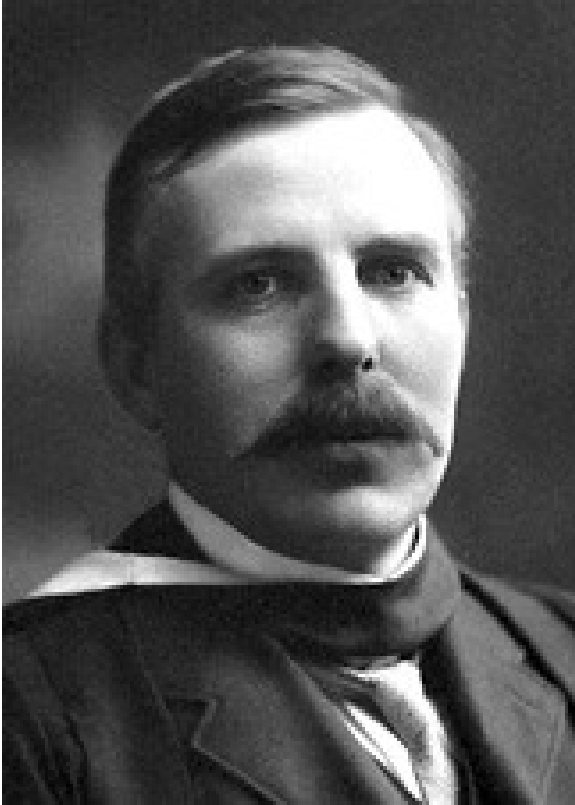


1871 – 1937
Nobel prize 1908



The Atom ist a
very small, heavy, positively charged **nucleus**
surrounded by negatively charged **electrons**

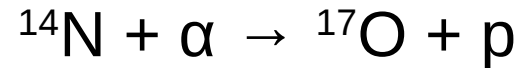
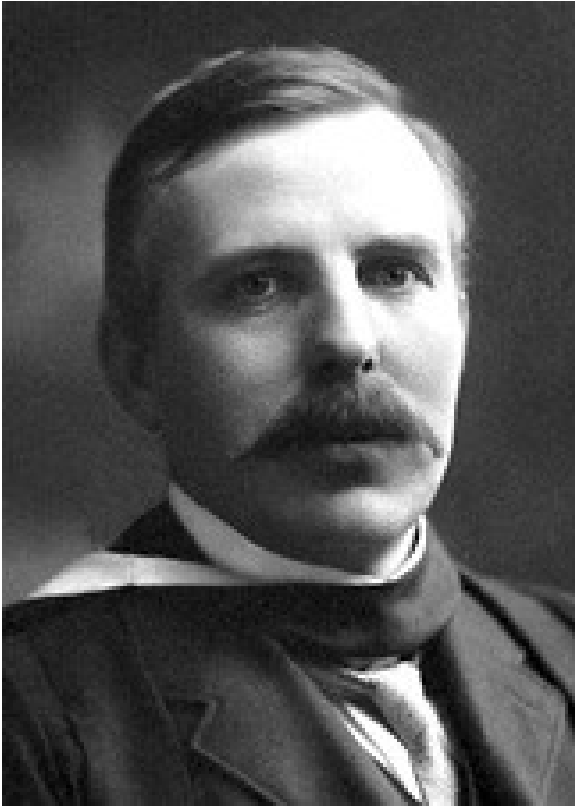
Ernest Rutherford – 1917



Rutherford shoots alpha particles at nitrogen. This creates the first man-made nuclear reaction.

He thereby discovers the **proton**.

Ernest Rutherford – 1917



Rutherford shoots alpha particles at nitrogen. This creates the first man-made nuclear reaction.

He thereby discovers the **proton**.

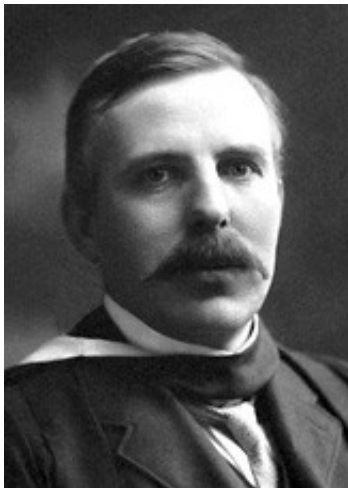
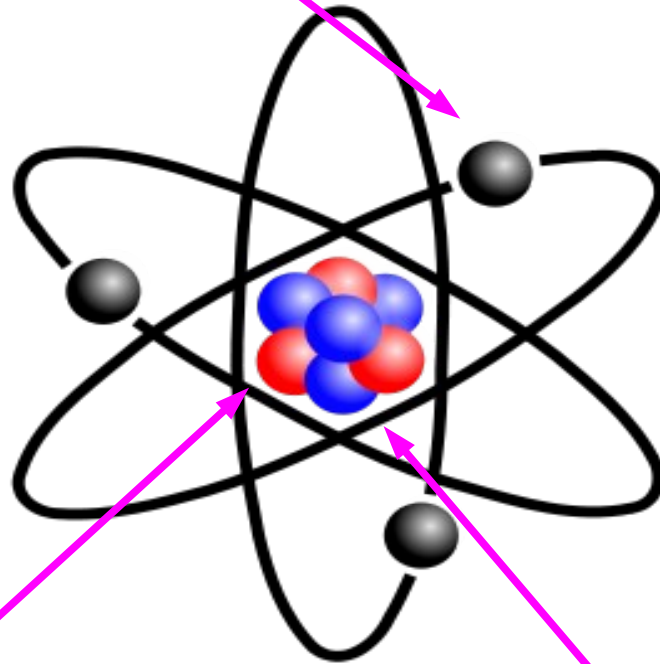
102nd birthday of the proton !!!



Constituents of matter



Electron: Joseph John Thomson
(1897)



Proton: Ernest Rutherford
(1917)

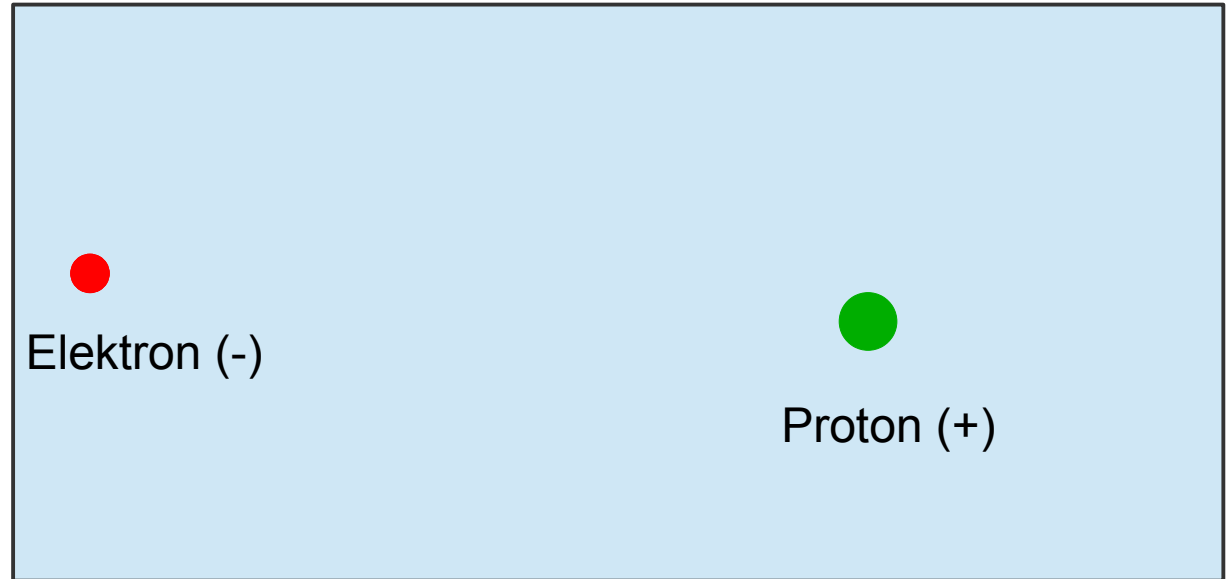


Neutron: James Chadwick
(1932)

Robert Hofstadter – 1955



1915 – 1990
Nobelpreis 1961

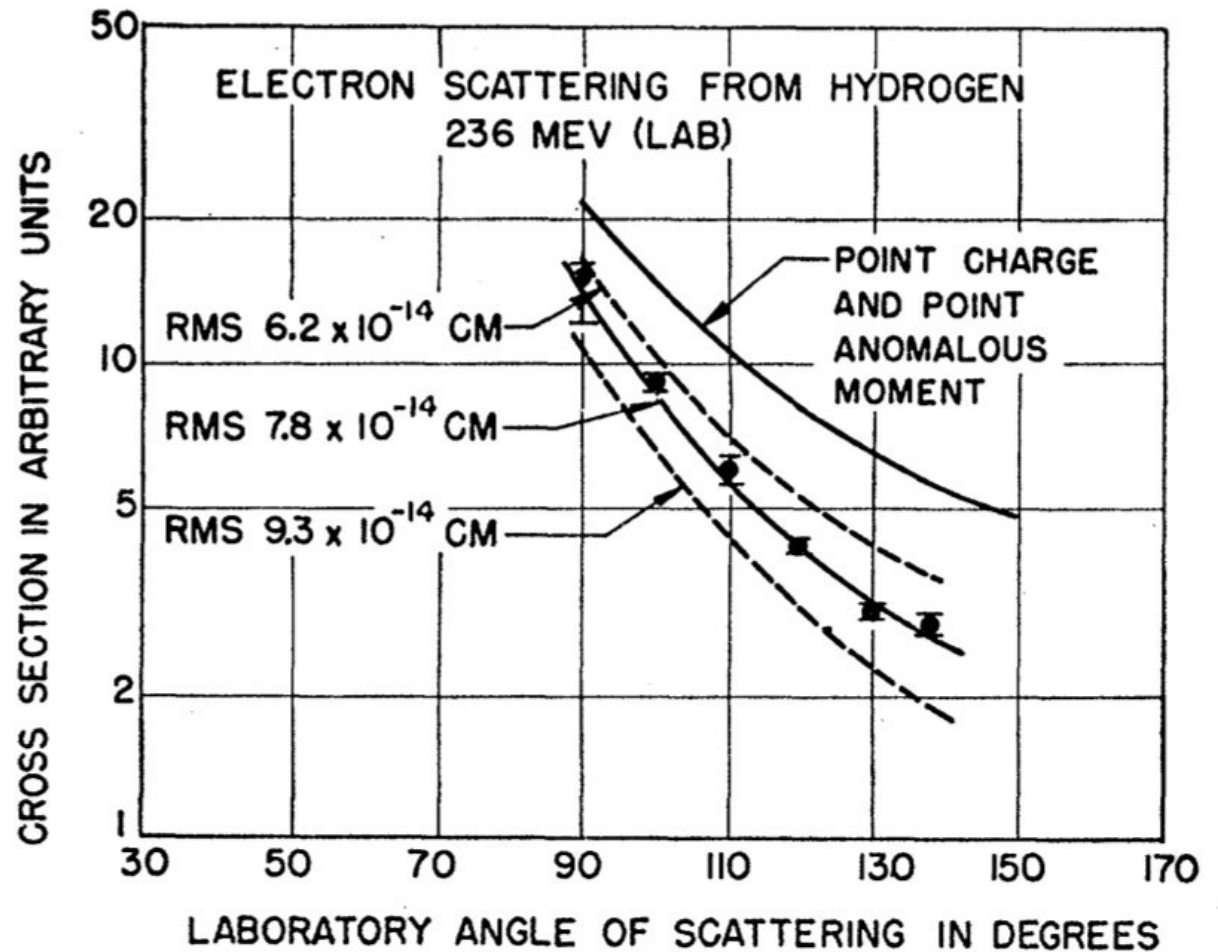


Streuung von (negativ geladenen) Elektronen
an (positiv geladenen) Protonen.

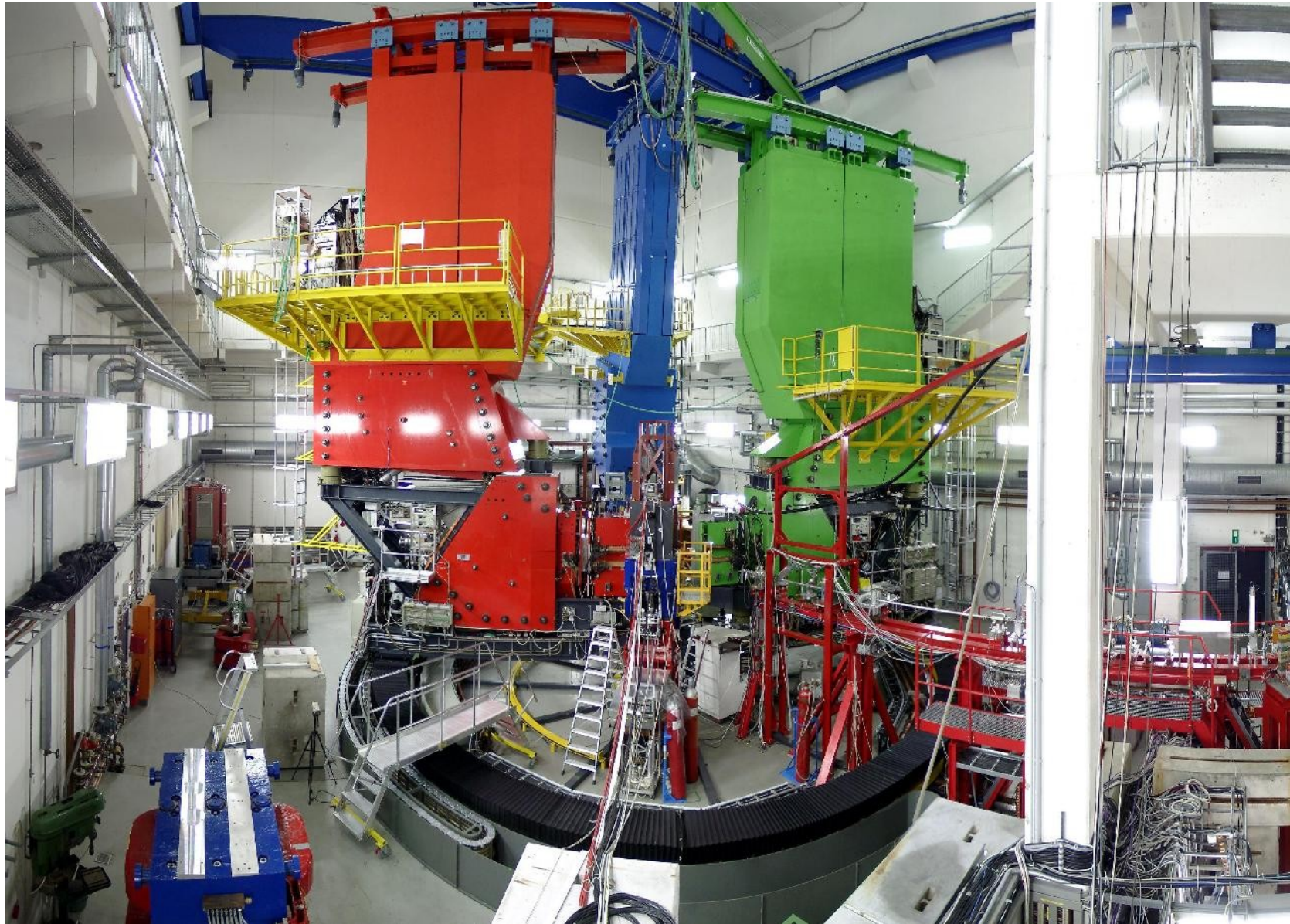
Robert Hofstadter – 1955



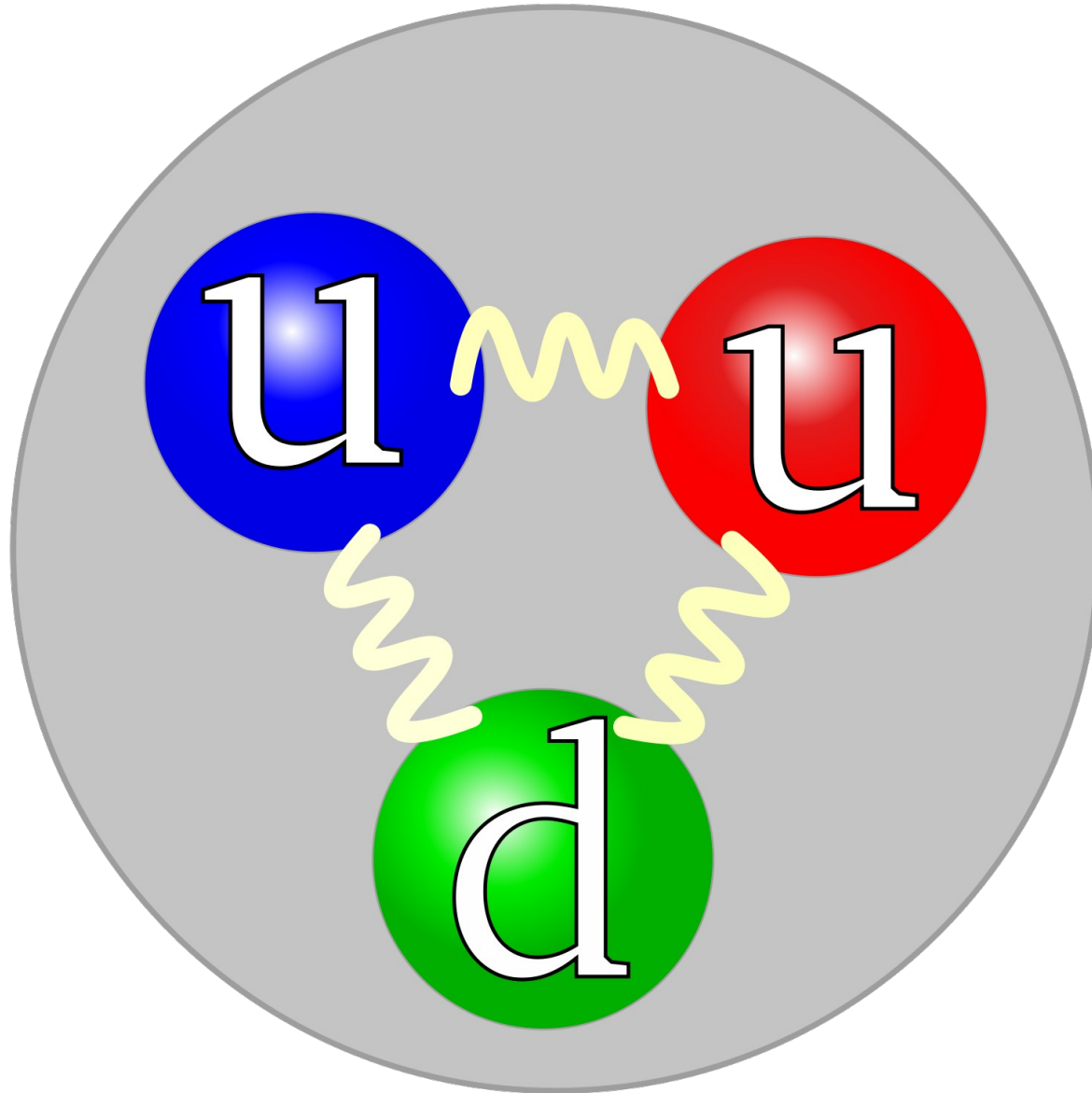
1915 – 1990
Nobelpreis 1961



Mainzer Microtron MAMI

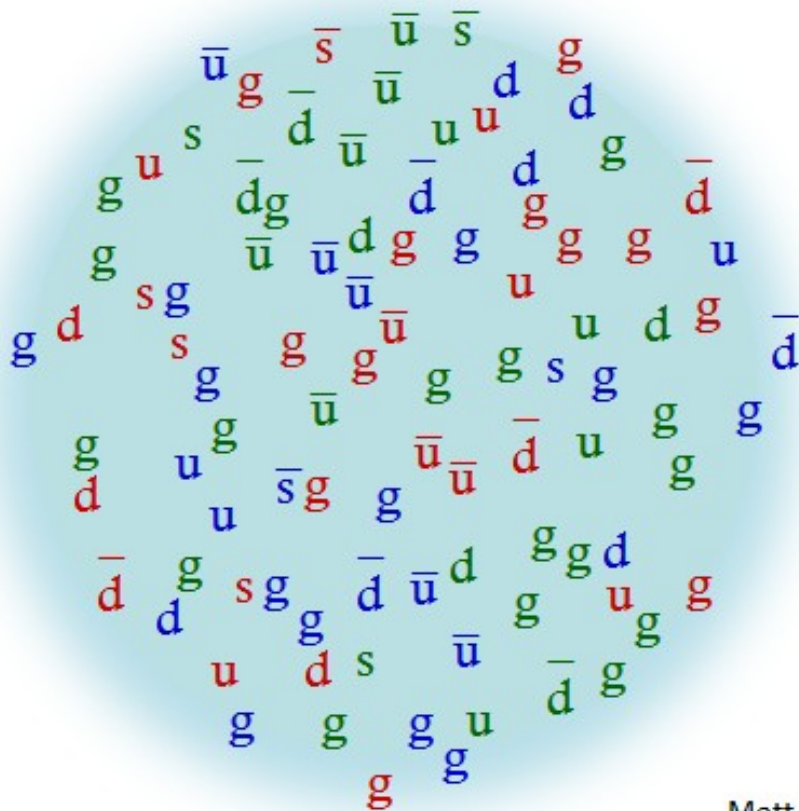


Proton – 3 Quarks

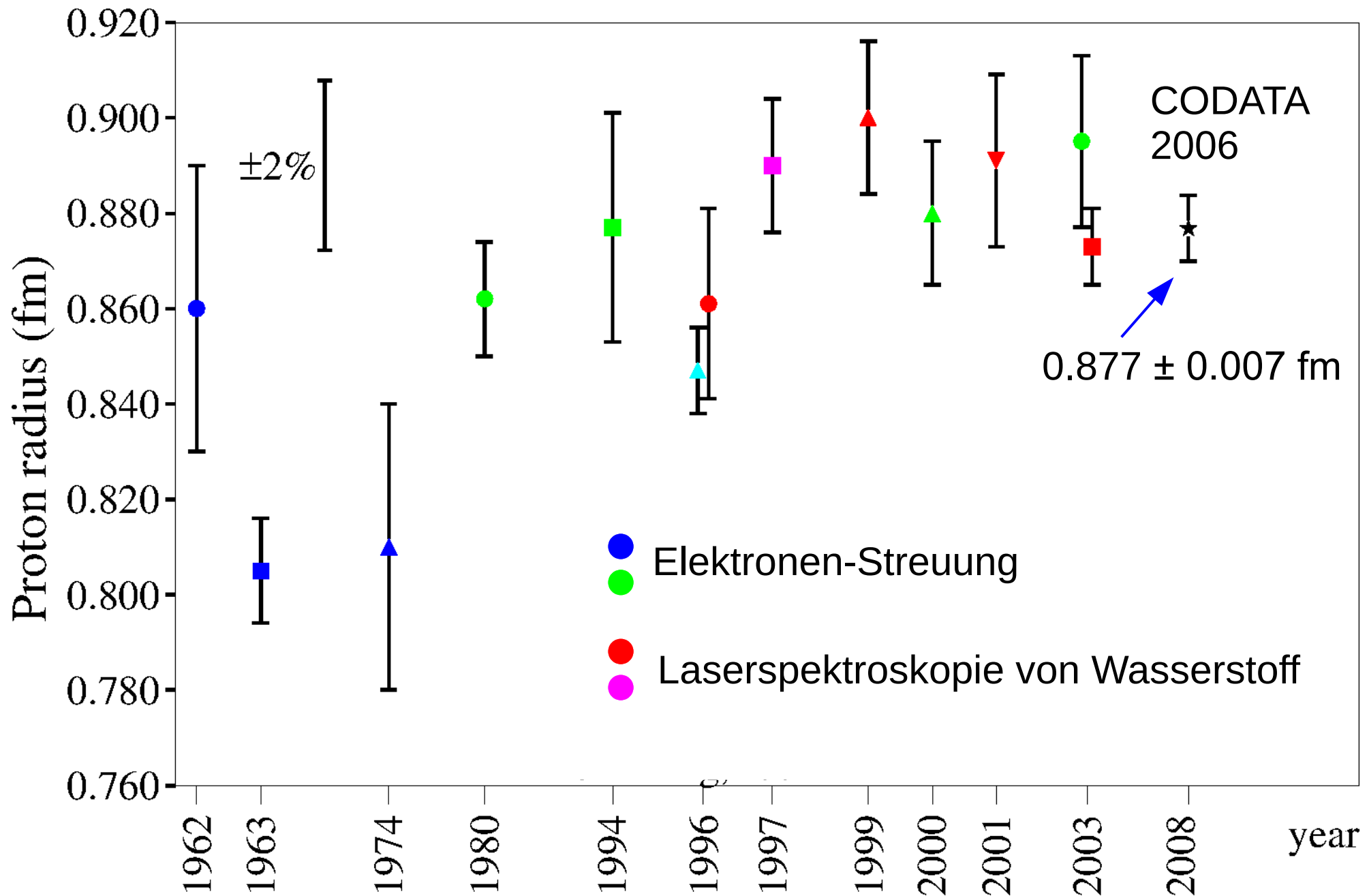


Proton – $\gg 3$ Quarks

proton



Wie gross ist das Proton?



The Hydrogen Atom



Discovers in 1947 (with Robert Retherford):

Energy levels “2S” and “2P” in hydrogen

do NOT have the same energy

Reason for **Lamb-Shift**

* Quantum fluctuations of the vacuum

* Proton charge radius

Willis E. Lamb, Jr.

1913 – 2008

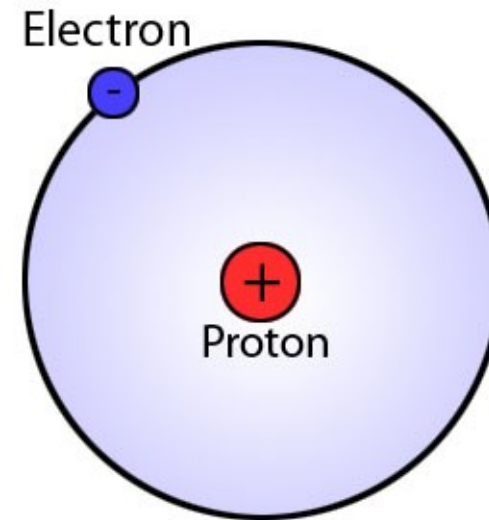
Nobel prize 1955

→ Development of

Quantum electrodynamics(QED)

The hydrogen atom

One Proton, orbited by one Electron.

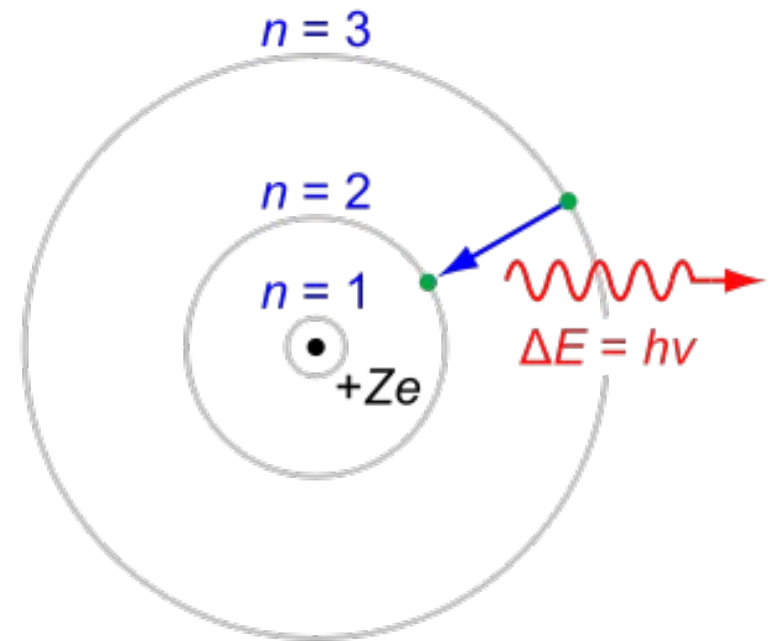


Nils Bohr

1885 – 1962
Nobel prize 1922

The hydrogen atom

One Proton, orbited by one Electron.

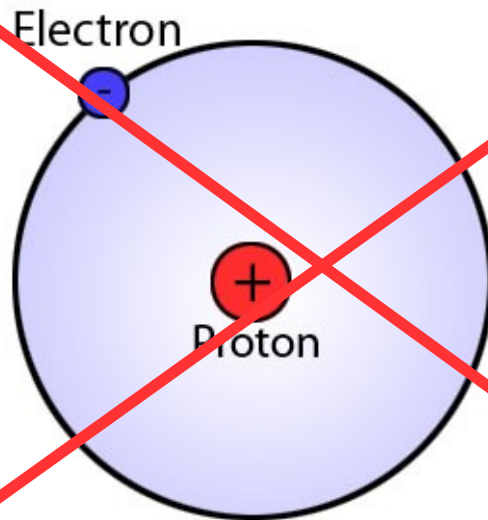


Nils Bohr

1885 – 1962

Nobel prize 1922

The hydrogen atom



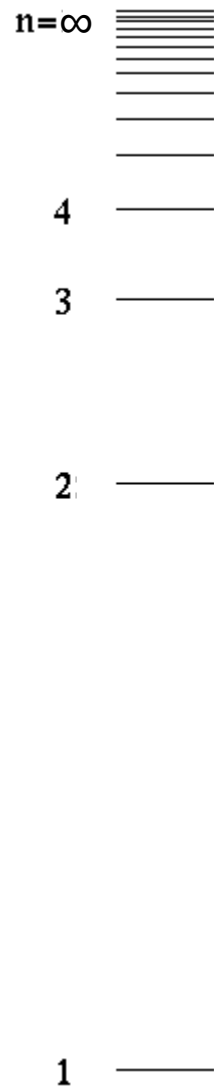
The atom is NOT a planetary system.

→ Quantum mechanics

→ Wave functions

→ Probability amplitudes

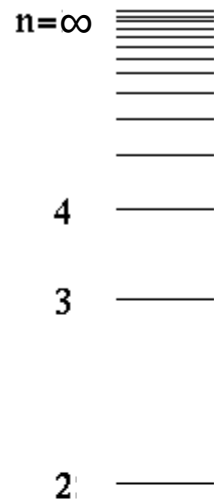
Energy levels of hydrogen



$$E_n \approx -\frac{R_\infty}{n^2}$$

Bohr formula

Energy levels of hydrogen



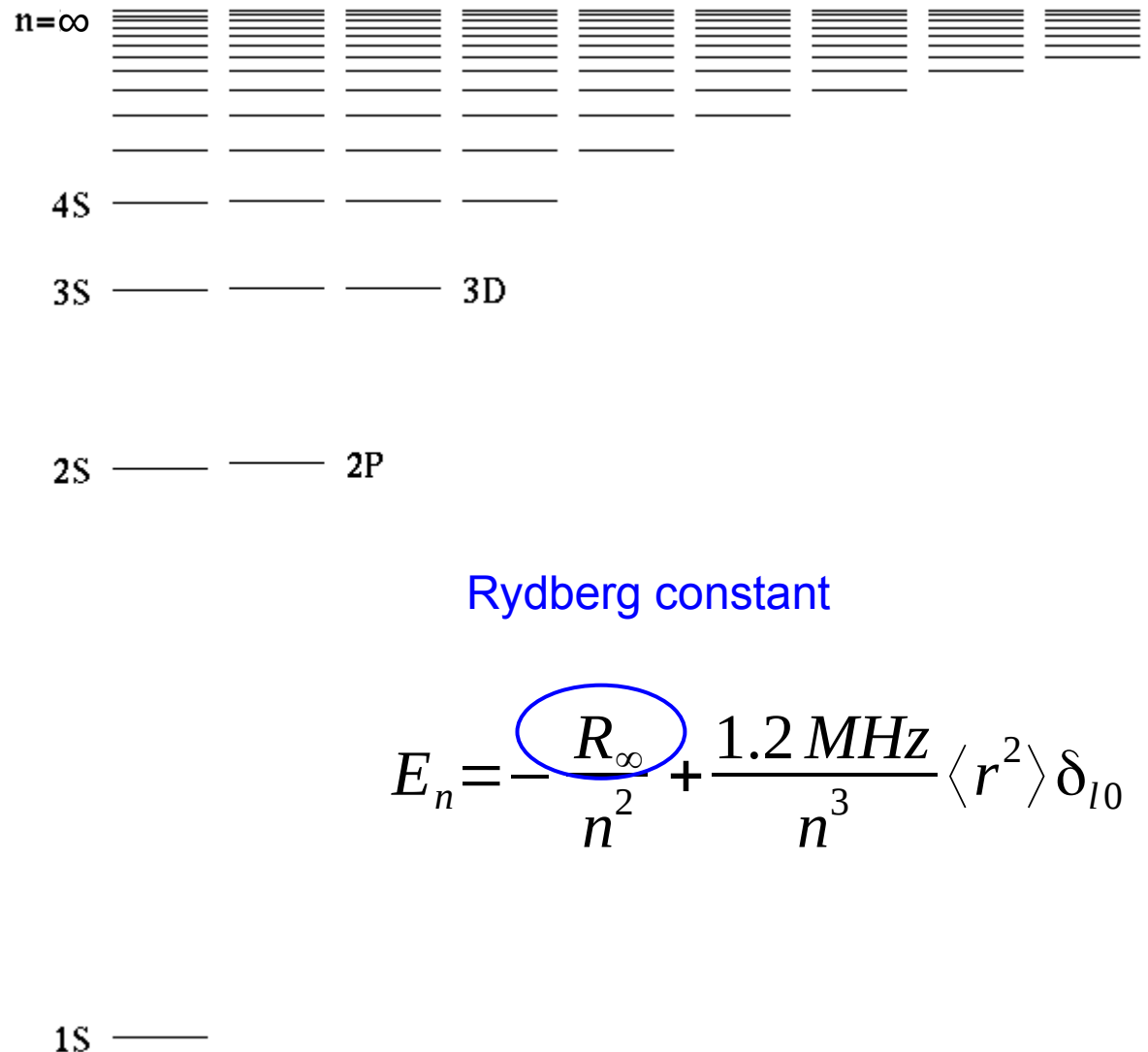
Rydberg constant

$$E_n \approx -\frac{R_\infty}{n^2}$$

Bohr formula

1 —

Energy levels of hydrogen

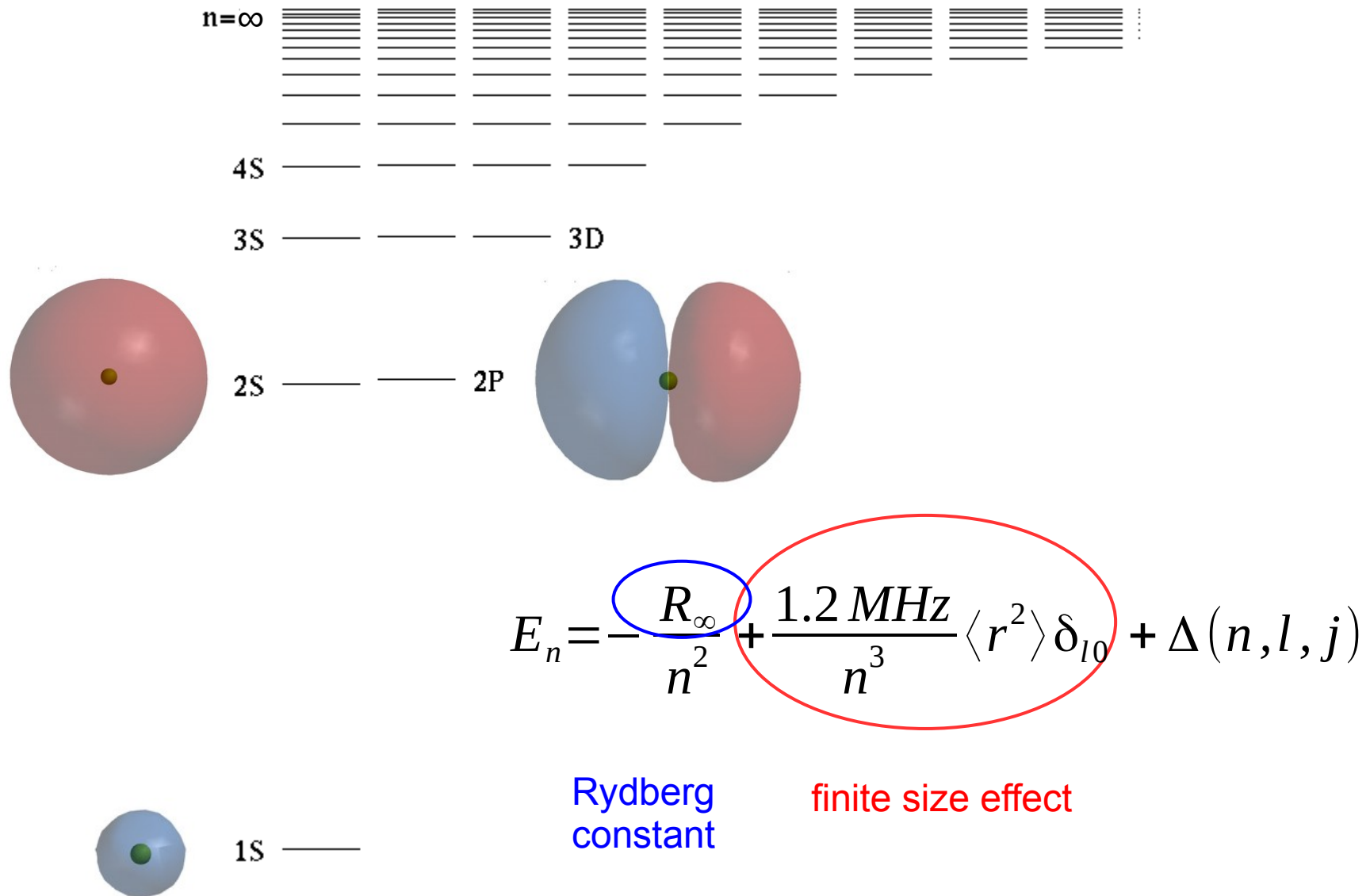


Rydberg constant

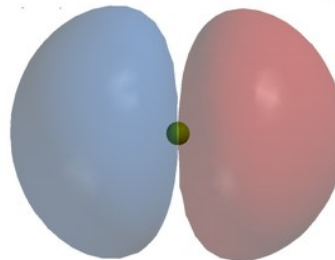
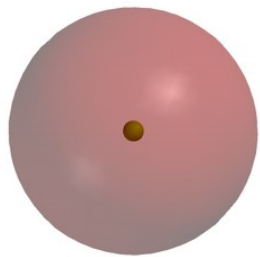
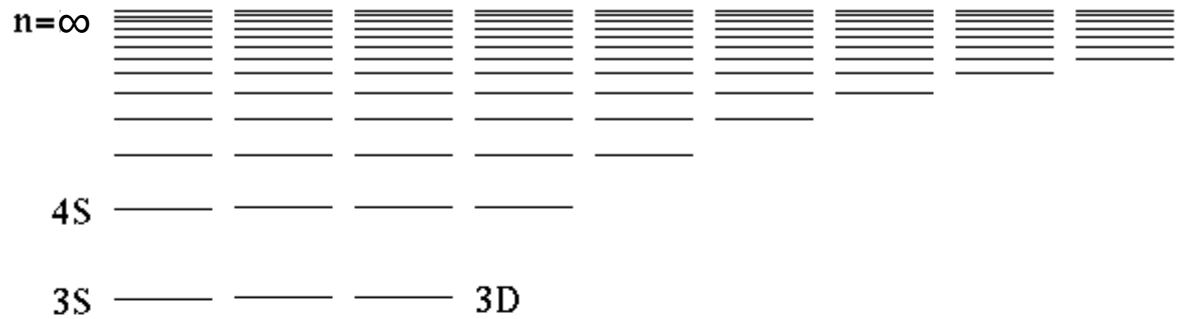
$$E_n = -\frac{R_\infty}{n^2} + \frac{1.2 \text{ MHz}}{n^3} \langle r^2 \rangle \delta_{l0} + \Delta(n, l, j)$$

1S —

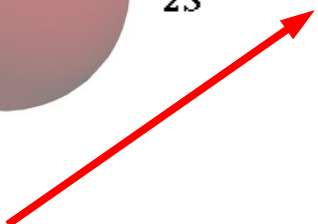
Energy levels of hydrogen



Energy levels of hydrogen



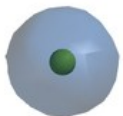
2S-2P Lamb shift



$$E_n = -\frac{R_\infty}{n^2} + \frac{1.2 \text{ MHz}}{n^3} \langle r^2 \rangle \delta_{l0} + \Delta(n, l, j)$$

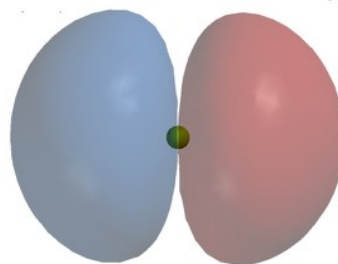
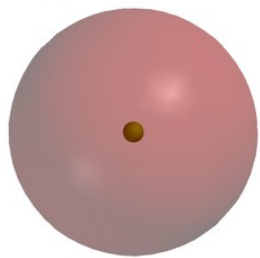
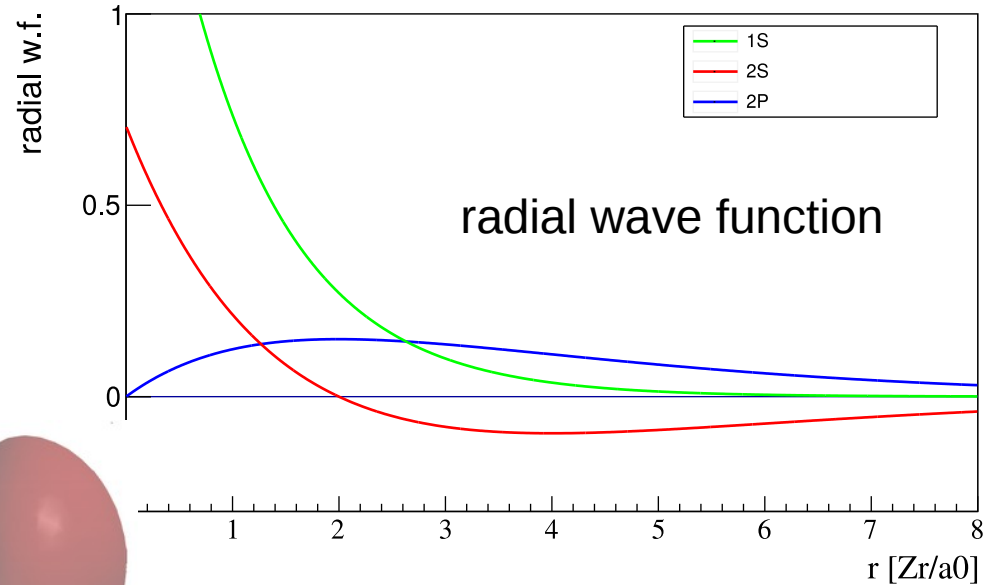
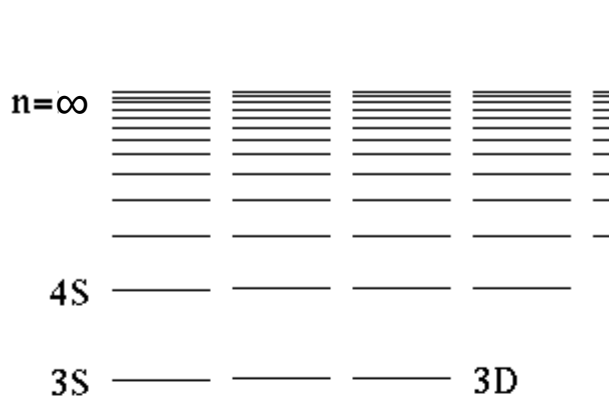
Rydberg constant

finite size effect



1S

Energy levels of hydrogen

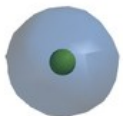


2S-2P Lamb shift

$$E_n = -\frac{R_\infty}{n^2} + \frac{1.2 \text{ MHz}}{n^3} \langle r^2 \rangle \delta_{l0} + \Delta(n, l, j)$$

Rydberg constant

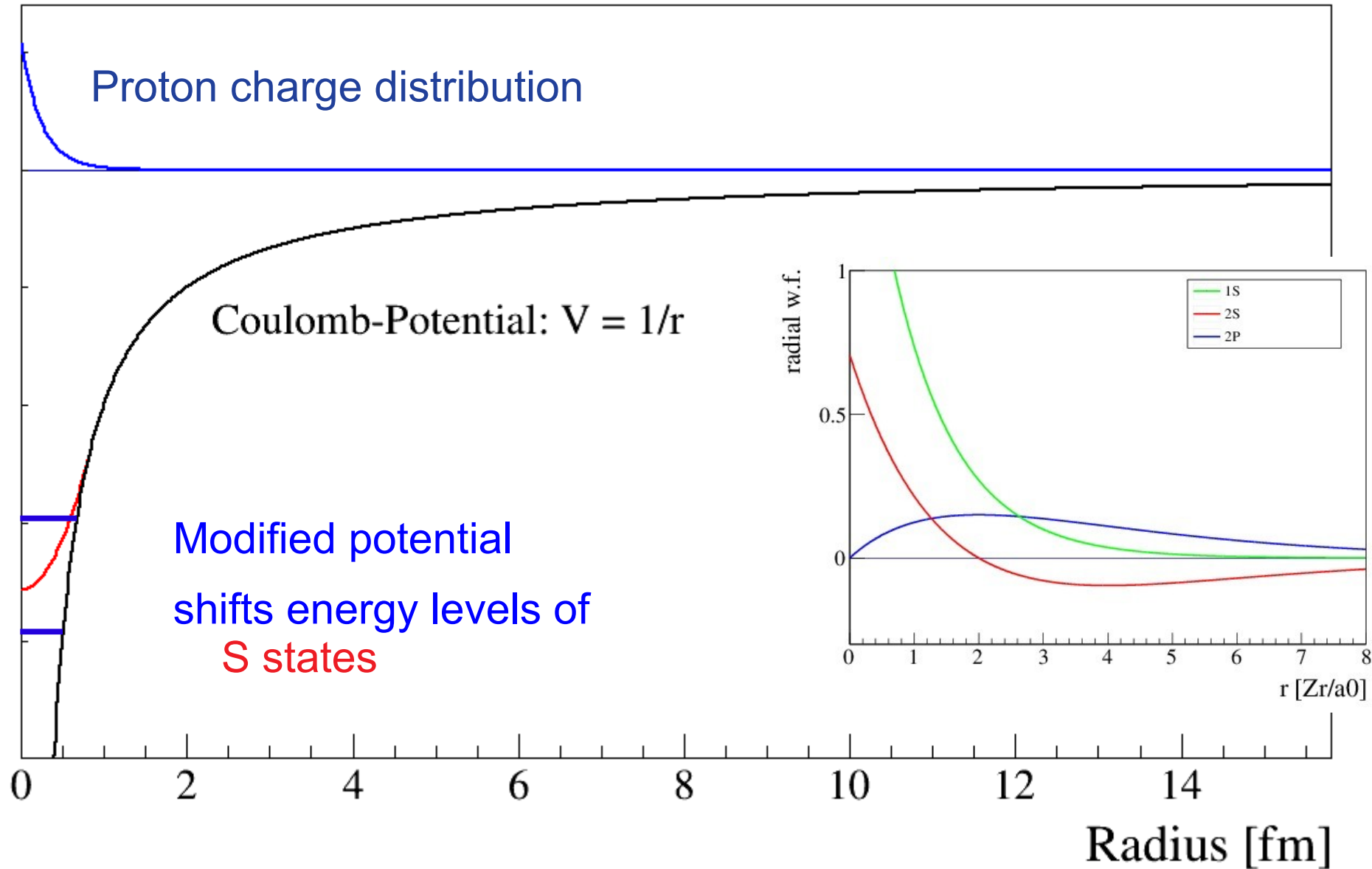
finite size effect
(enters at the 10th digit)



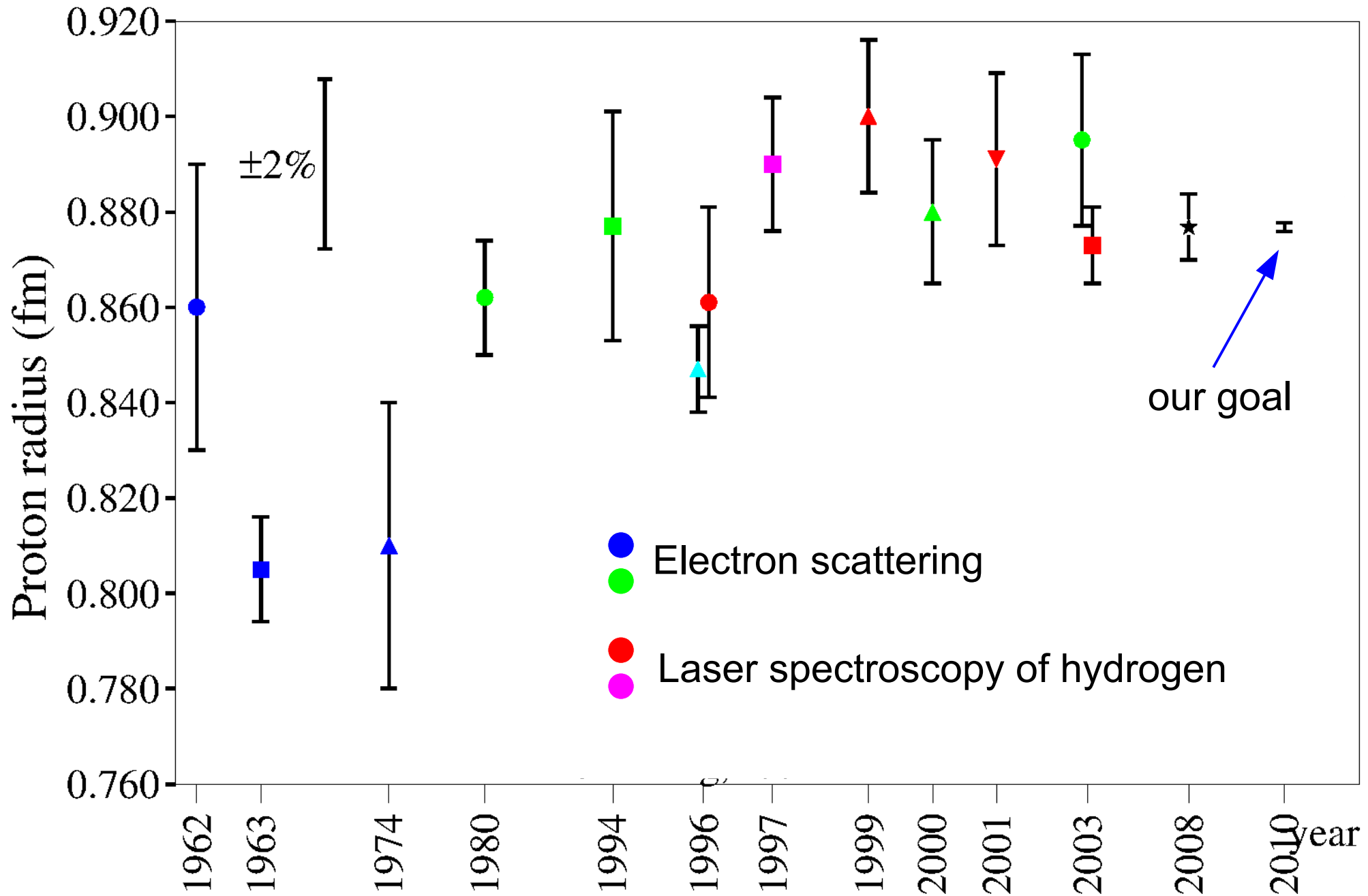
1S

Proton radius and hydrogen

wilk. Einh.



How large is a Proton?



A 10fold more precise measurement of the proton radius!?

Proposal for an experiment at PSI

Laser spectroscopy of the Lamb Shift in muonic hydrogen

P. Hauser, C. Petitjean, L.M. Simons, D. Taqqu
Paul Scherrer Institute, CH-5232 Villigen PSI, Switzerland

F. Kottmann, R. Pohl
Institut für Teilchenphysik, ETHZ, CH-8093 Zürich, Switzerland

C. Donche-Gay, O. Huot, P. Knowles, F. Mulhauser, L.A. Schaller, H. Schneuwly
Institut de Physique de l'Université, CH-1700 Fribourg, Switzerland

F.J. Hartmann, W. Schott
Physik-Department, Technische Universität München, D-85747 Garching, Germany

F. Biraben, F. Nez, P. Indelicato
Laboratoire Kastler Brossel, F-75252 Paris CEDEX 05, France

C.A.N. Conde, J.M.F. Santos, J.F.C.A. Veloso
Department of Physics, Coimbra University, P-3000 Coimbra, Portugal

T.W. Hänsch
Max-Planck-Institut für Quantenoptik, D-85747 Garching, Germany

P. Rabinowitz
Department of Chemistry, Princeton University, Princeton, NJ08544-1009, USA

Proposal 1998:
3: 1%

Measure the

Lamb shift

in

muonic hydrogen

Goal:

10 time more precise

Muonic Hydrogen

A proton, orbited by a **negative muon**.

What is

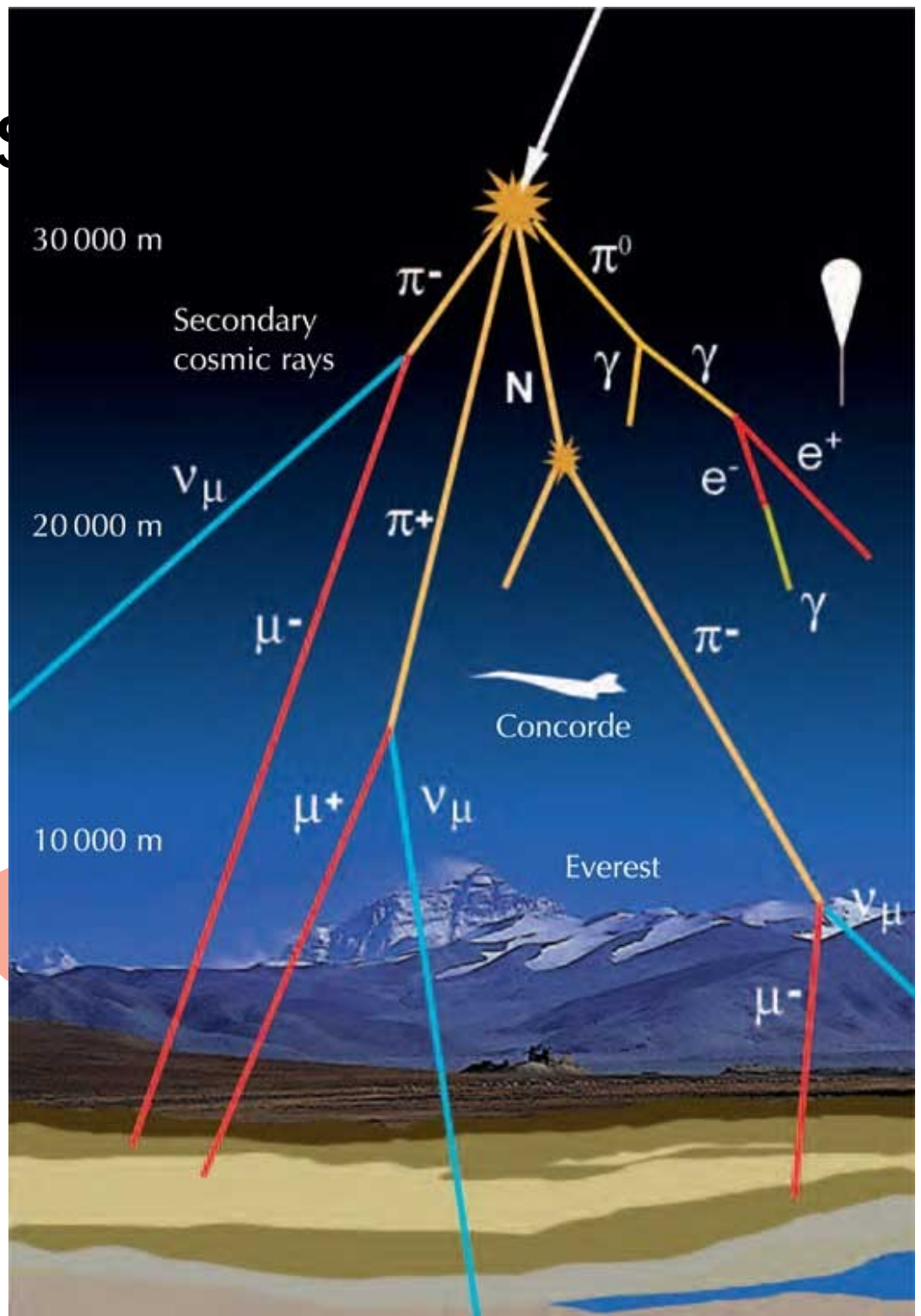


Carl David Anderson

Nobel prize 1936
(for the Positron!)

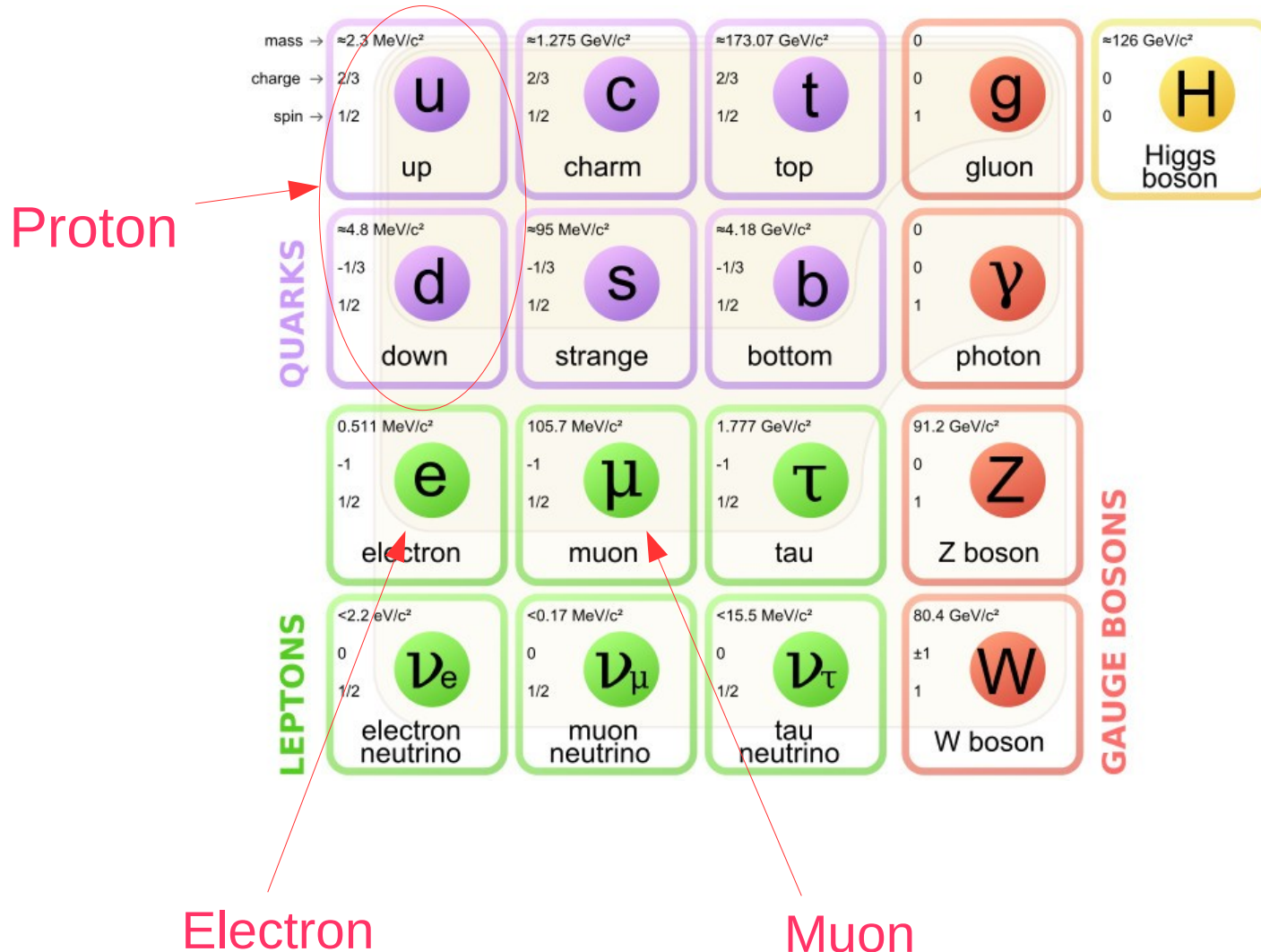


Seth Neddermeyer



The muon and its place in the world

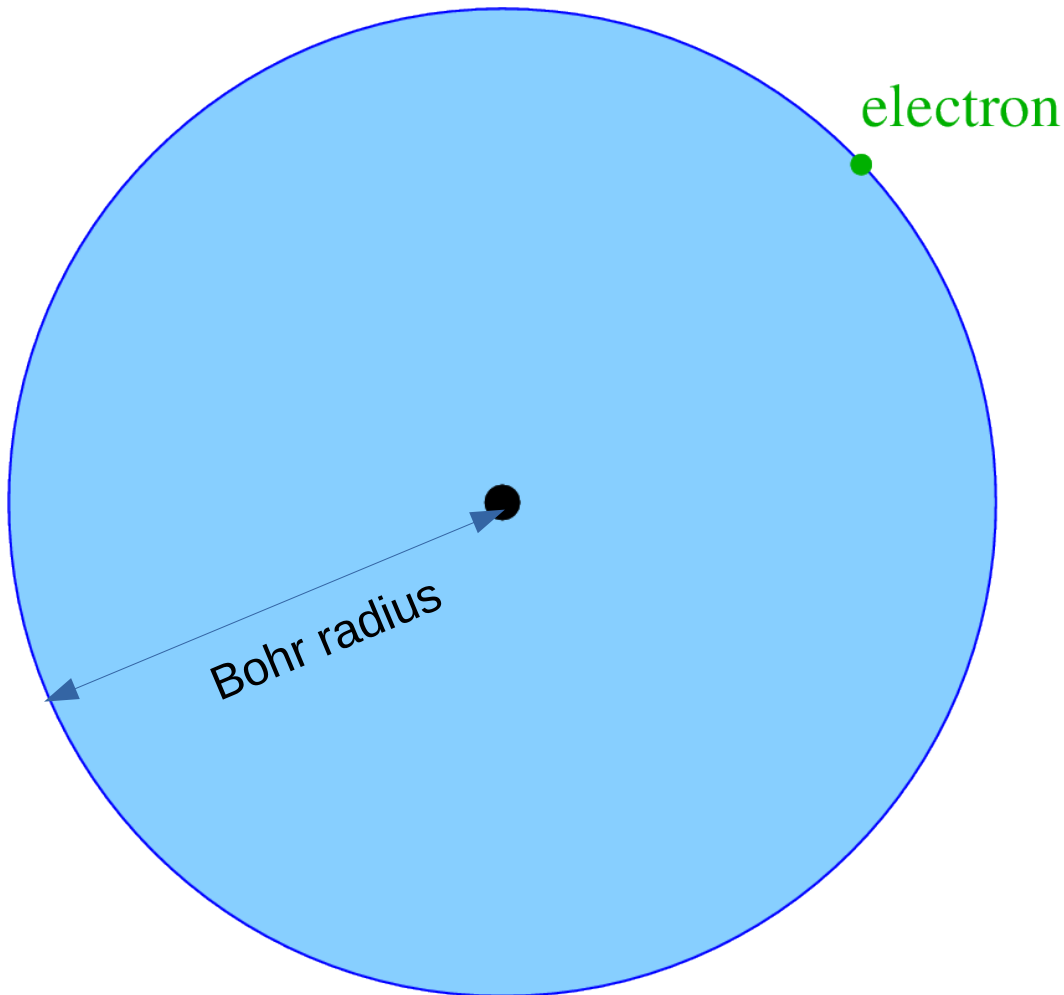
Standard Model of Particle Physics



Electronic and muonic atoms

Regular hydrogen:

Proton + **Electron**



Muonic hydrogen:

Proton + **Muon**

Muon **mass** = 200 * electron mass

Bohr **radius** = 1/200 of H

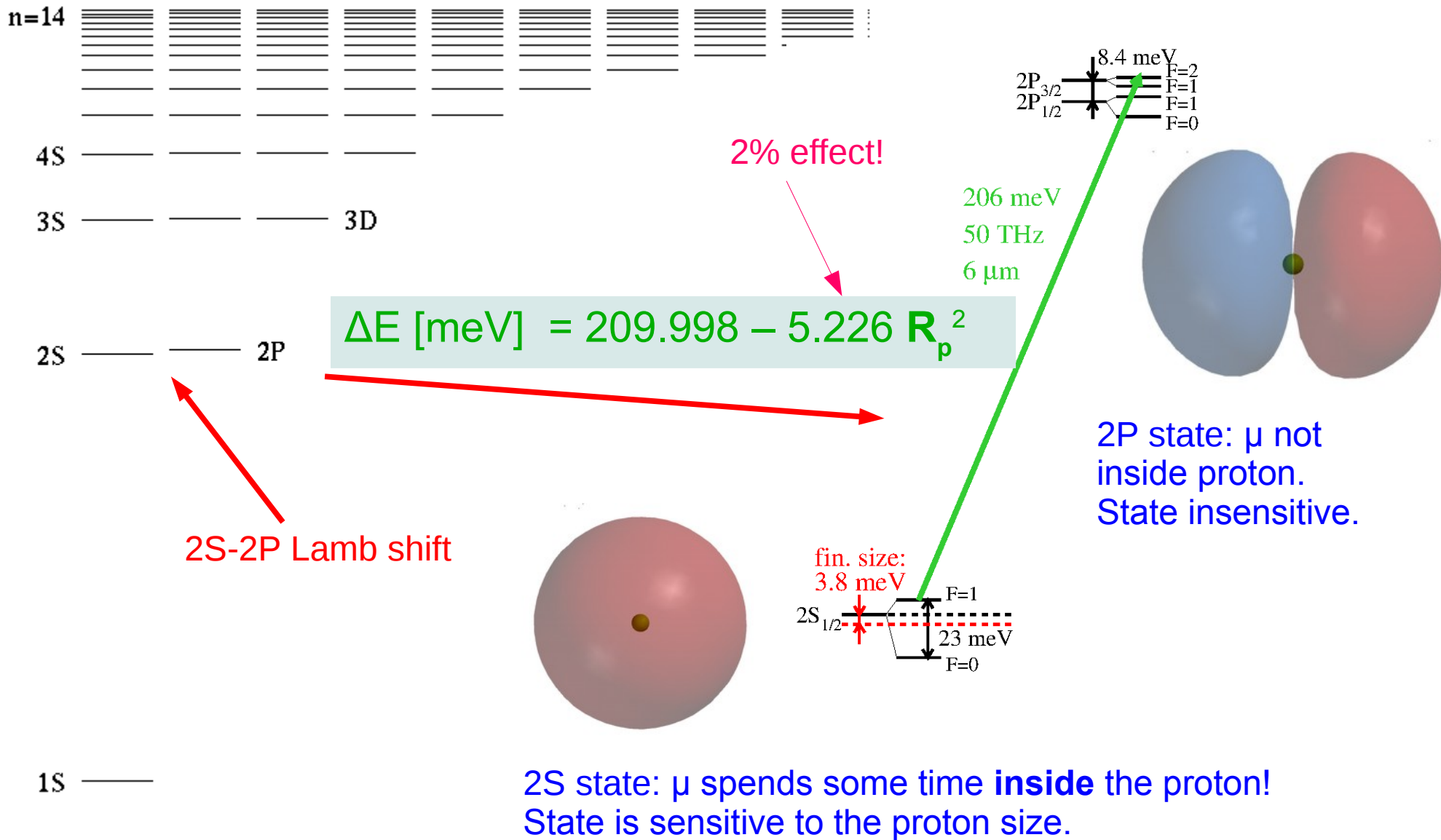
Wave function overlap:

$200^3 = 10 \text{ million !}$

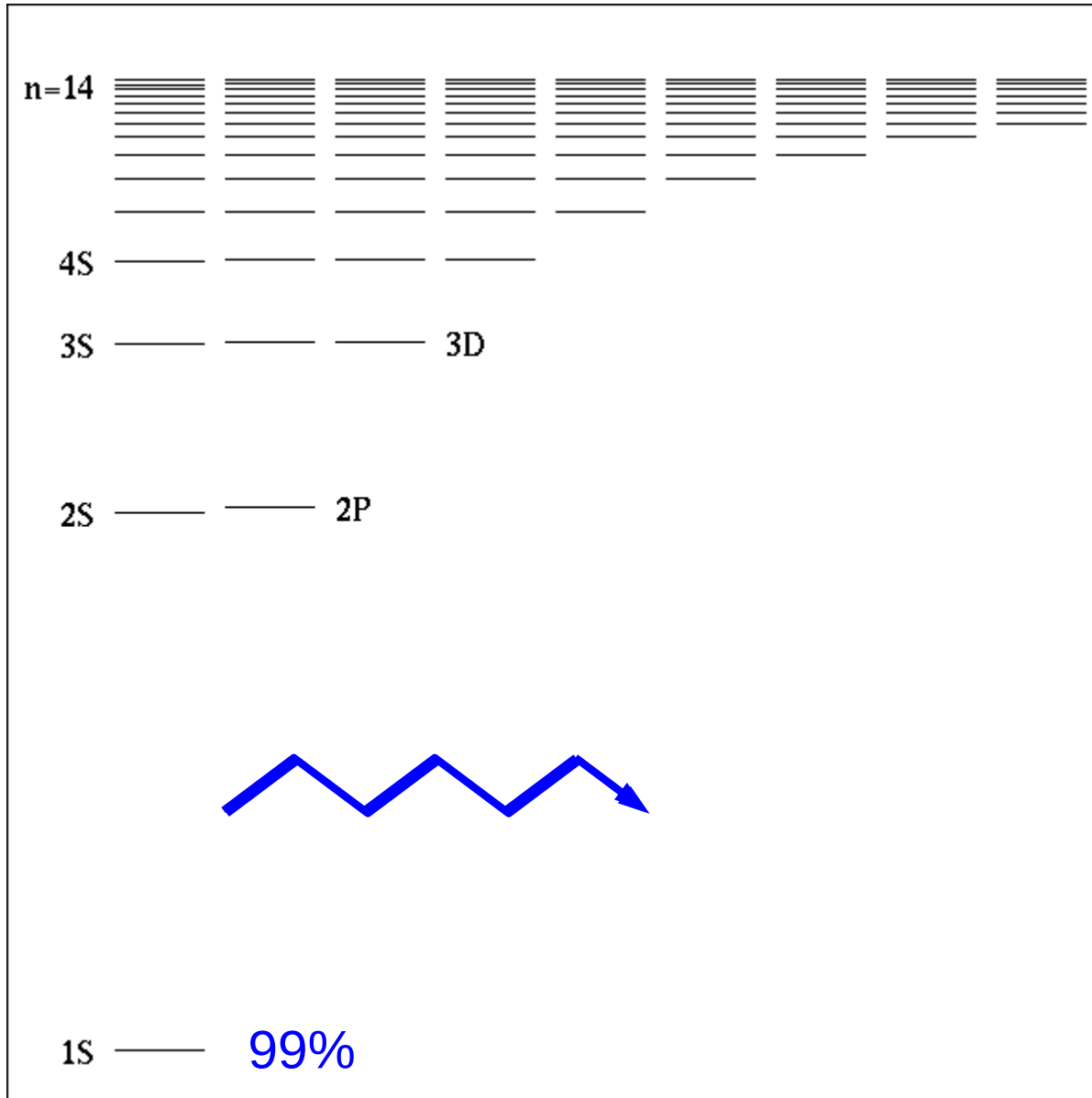


muonic hydrogen is a **few million times** more sensitive to proton size

Muonic Hydrogen



Principle of the measurement



* Muons stop in H₂

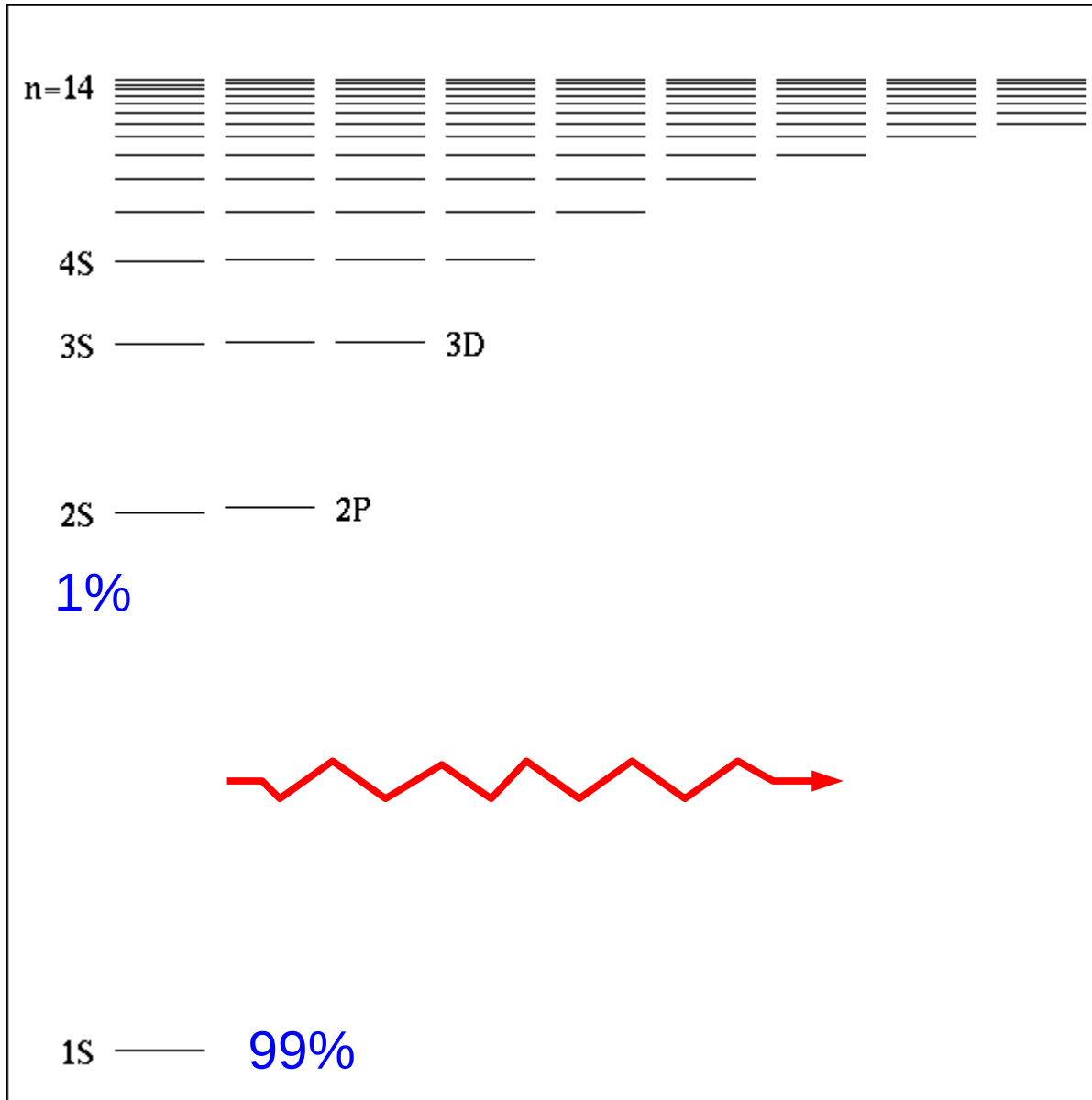
* Initial capture into states with n~14

* cascade to lower n

* 99% end in 1S ground-state

* X-ray photons

Principle of the measurement



* Muons stop in H₂

* Initial capture into states with n~14

* cascade to lower n

* 1% reach the long-lived 2S state

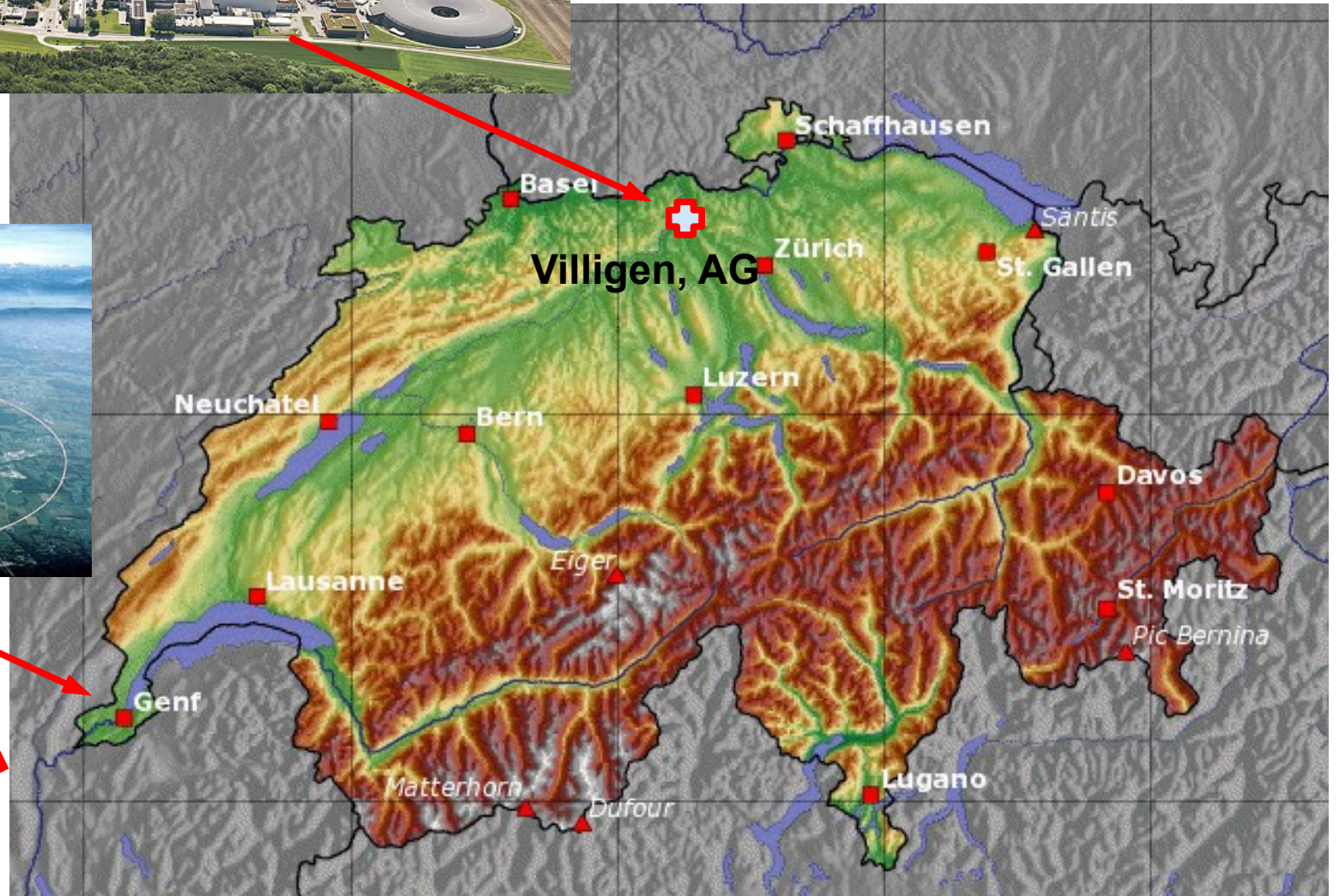
* Laser on resonance



The accelerator at PSI



PAUL SCHERRER INSTITUT



Paul-Scherrer-Institut



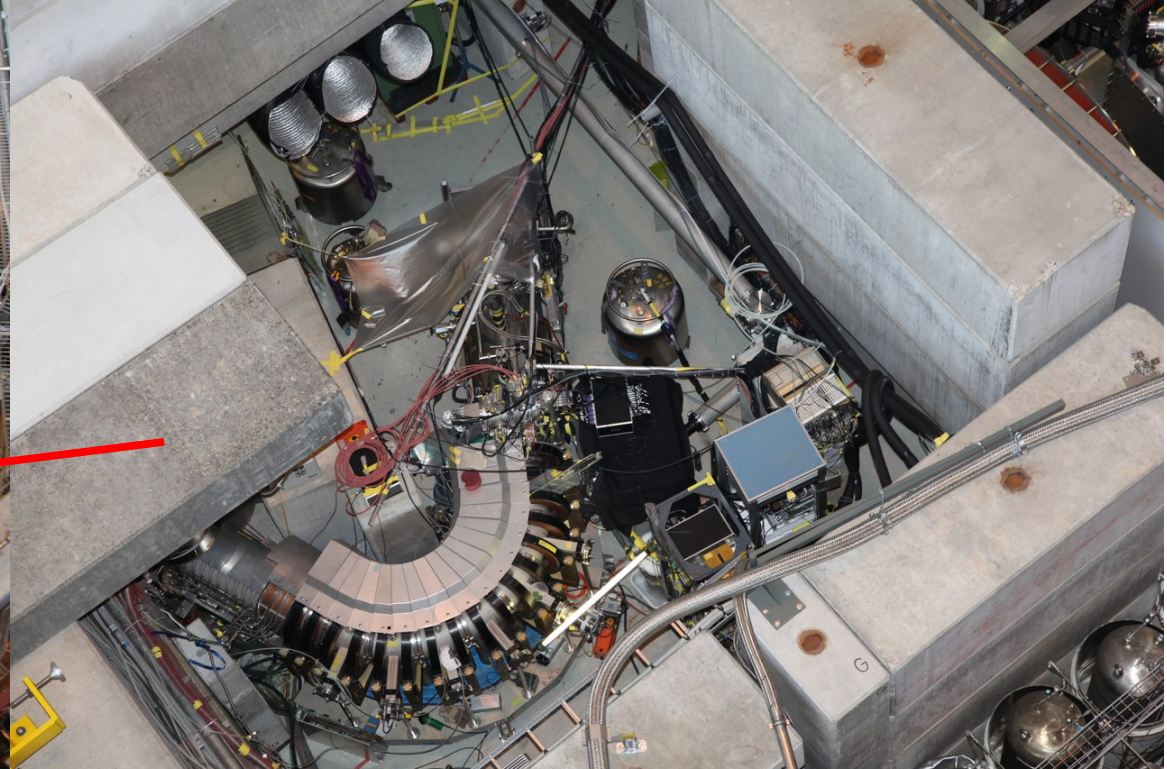
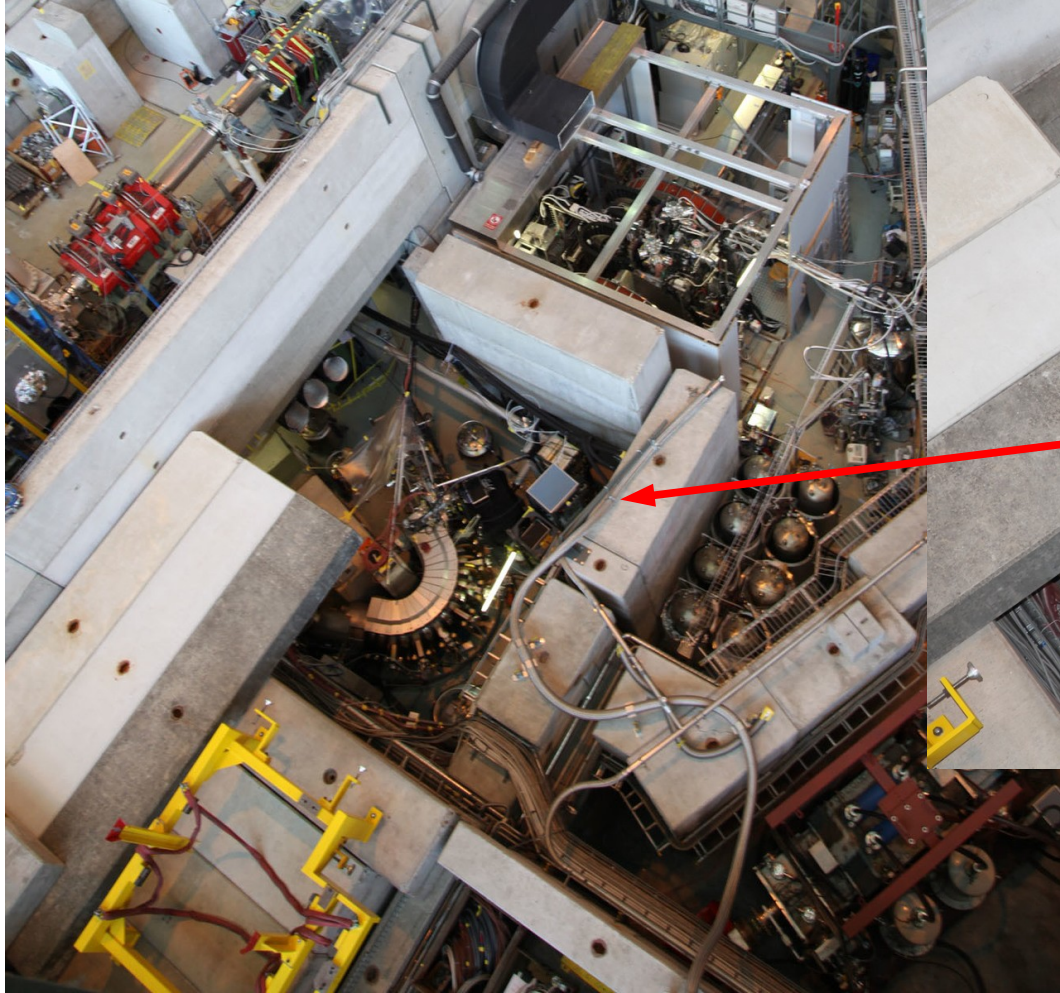
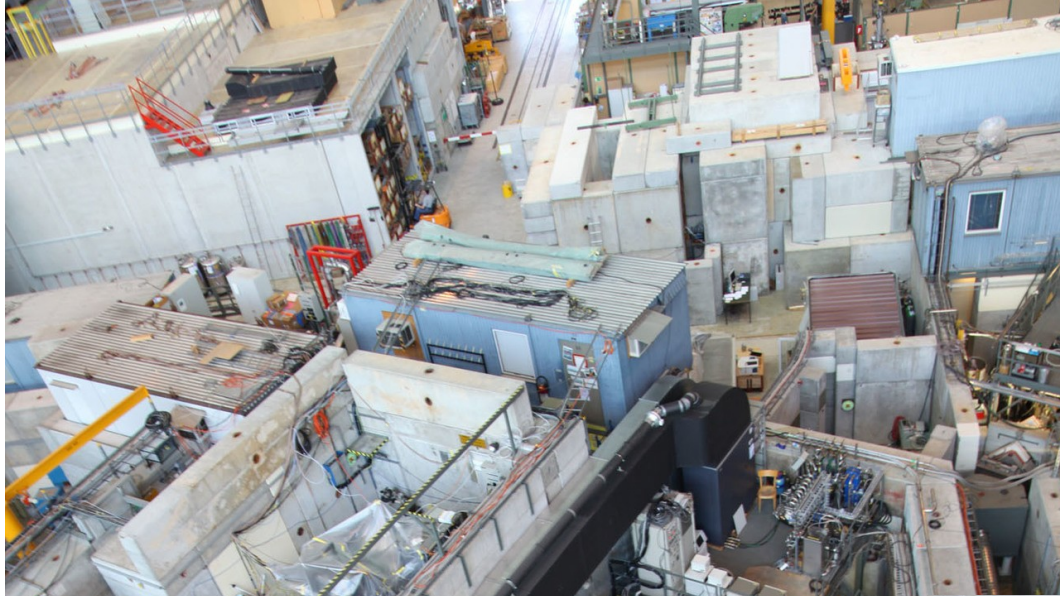
Paul-Scherrer-Institut



Experimental hall



Experimental hall from above



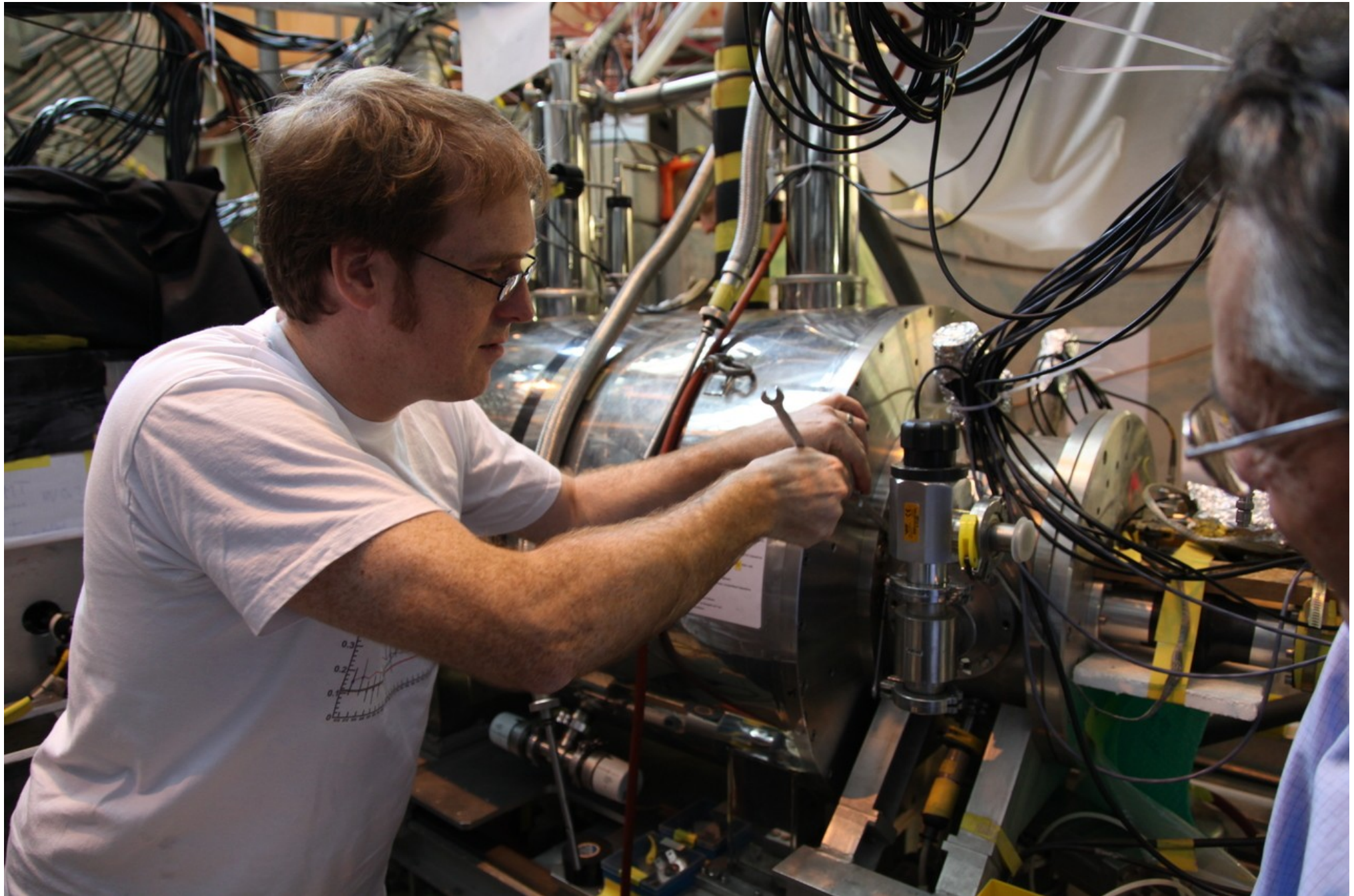
Beam area $\pi E5$



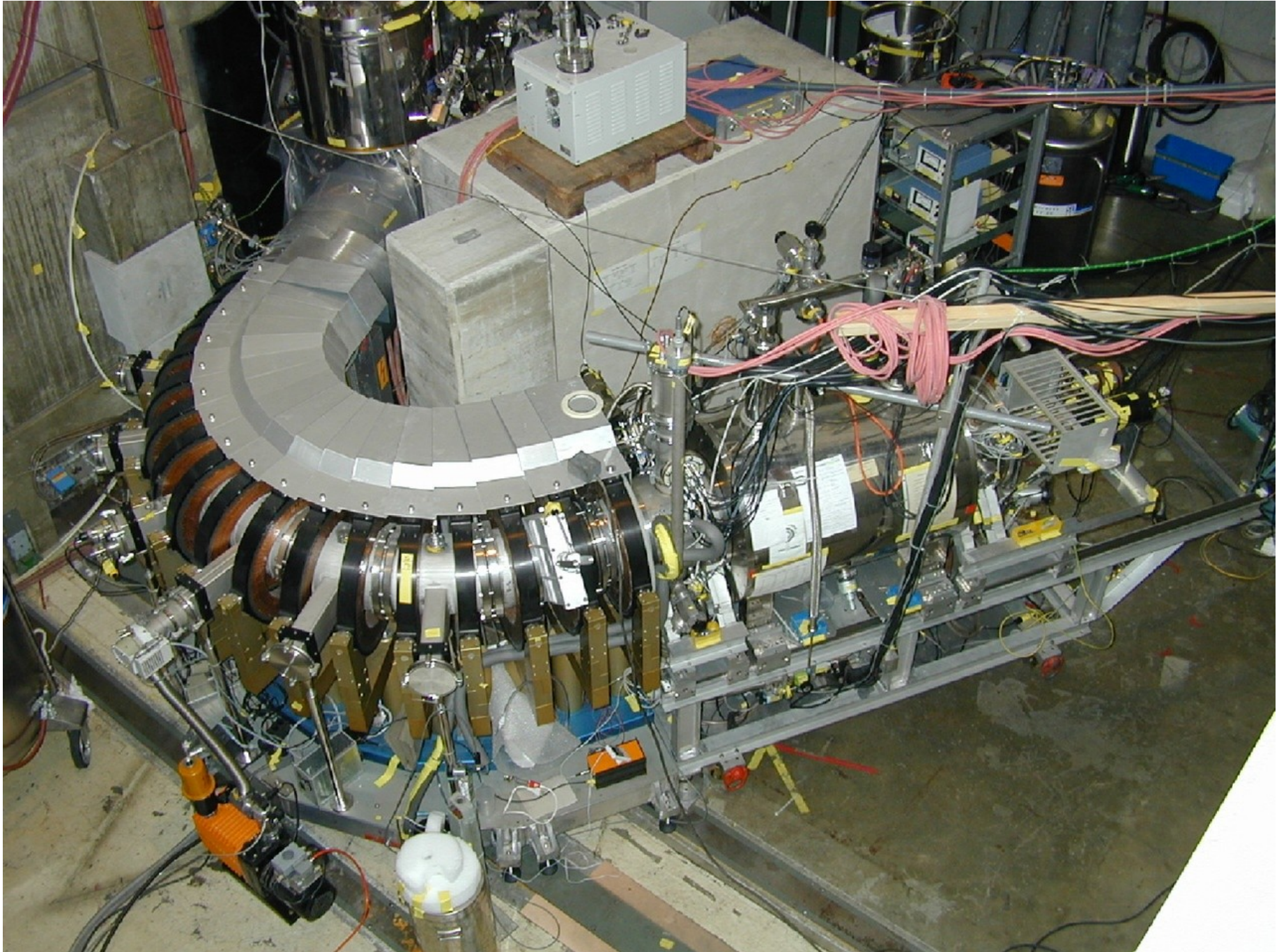
Muon beam line in $\pi E5$



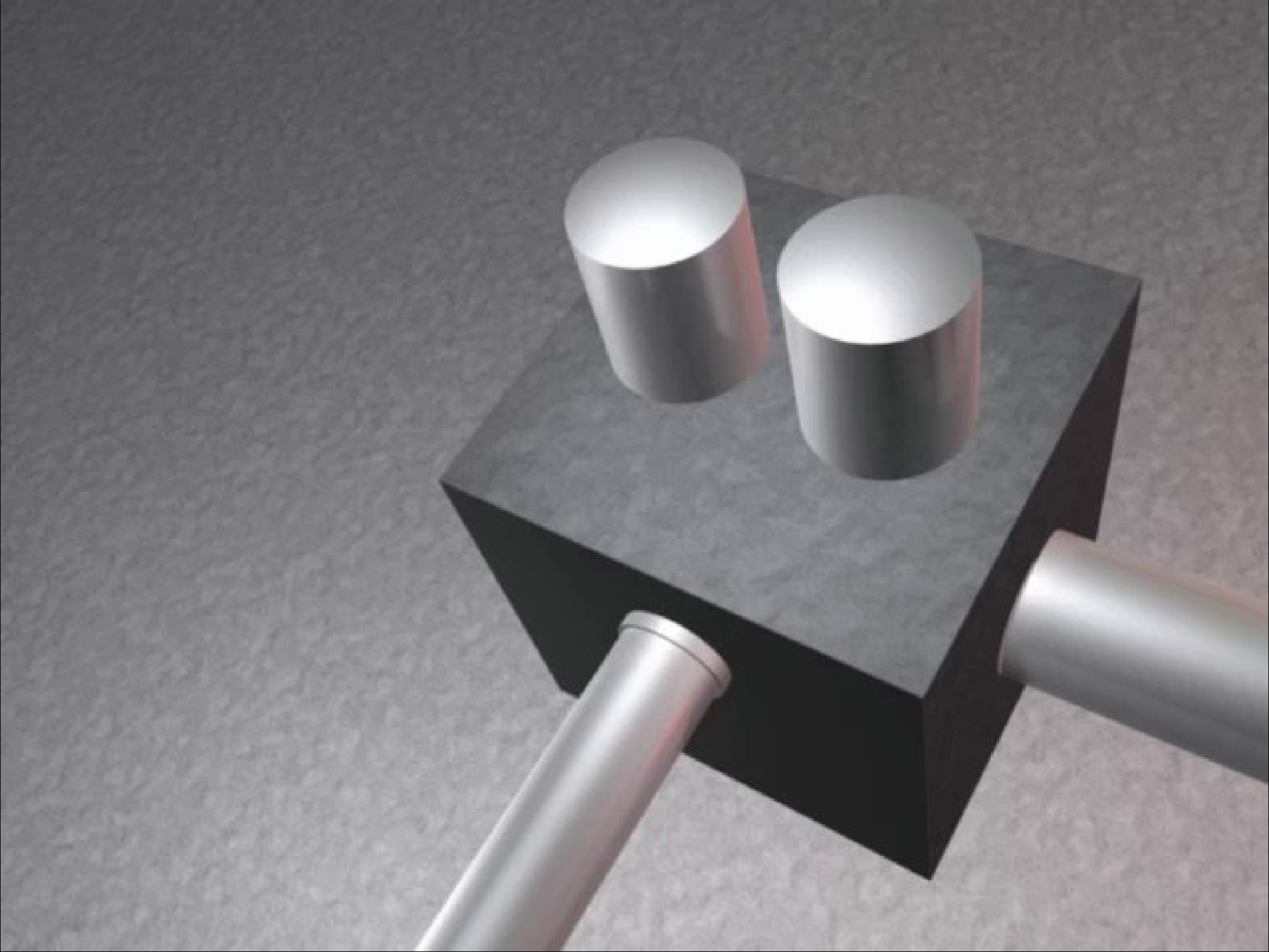
Final preparations



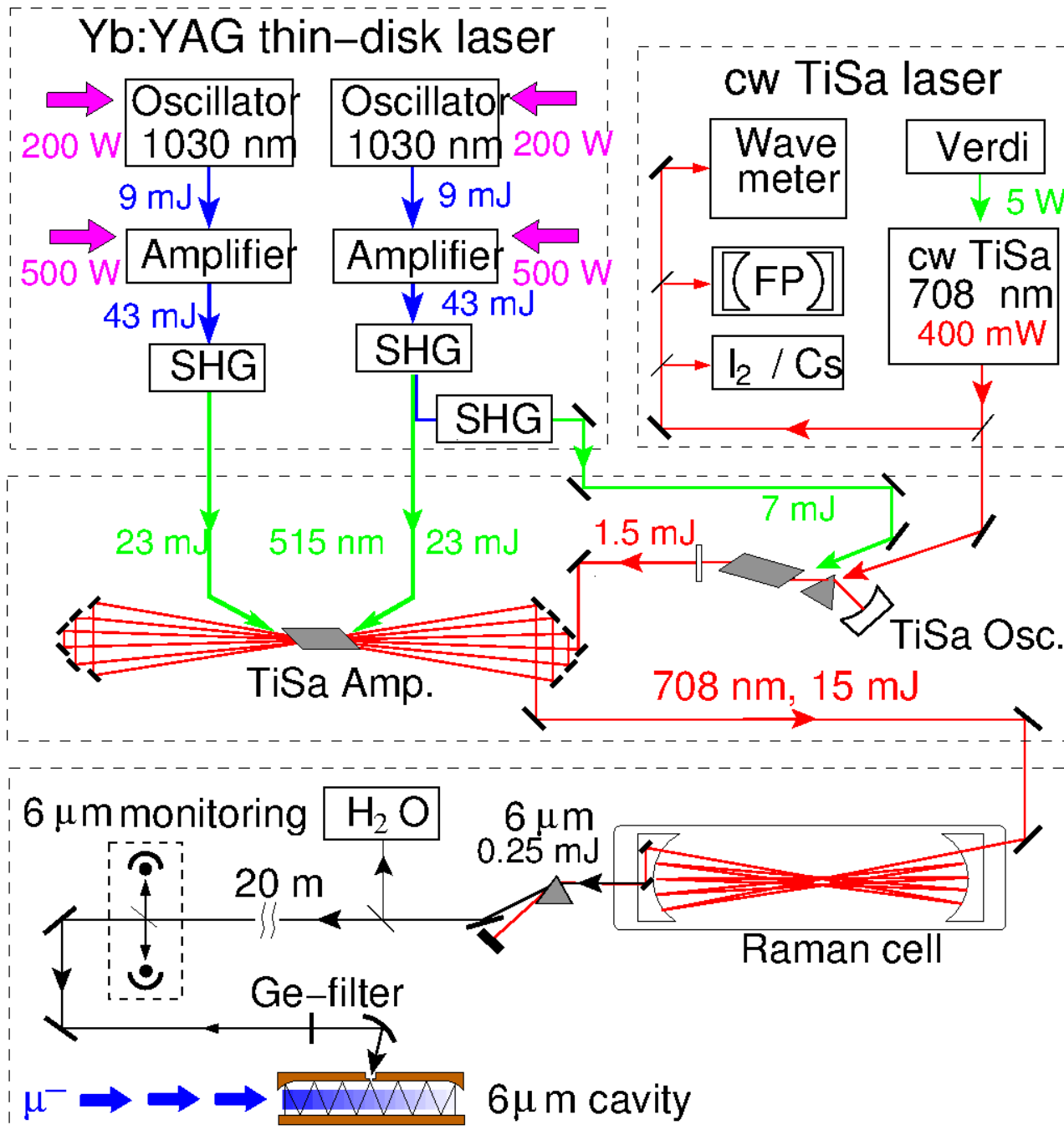
The muon beam line in $\pi E5$



Movie: Beam Line



The laser system



Yb:YAG Disk laser

→ fast response on μ

Frequency doubling (SHG)

→ green light to pump
Ti:sapphire laser

Ti:sapphire cw laser

→ determines laser frequency

Ti:sapphire MOPA

→ high pulse energy (15 mJ)

Raman cell

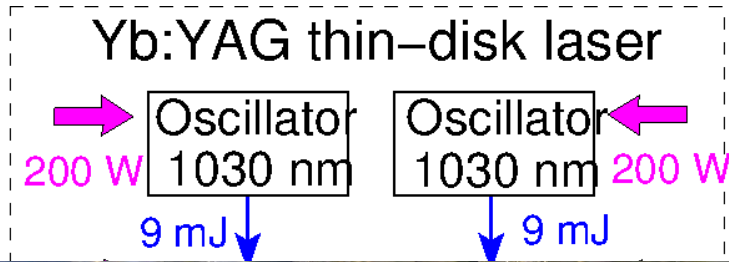
→ 3 sequential stimulated
Raman Stokes shifts

Laser wave length → 6 μ m

Target Cavity

→ Mirror system to fill the
muon stop volume (H₂)

Laser system: Yb:YAG Disk Osci



Yb:YAG Disk laser
→ fast response on μ

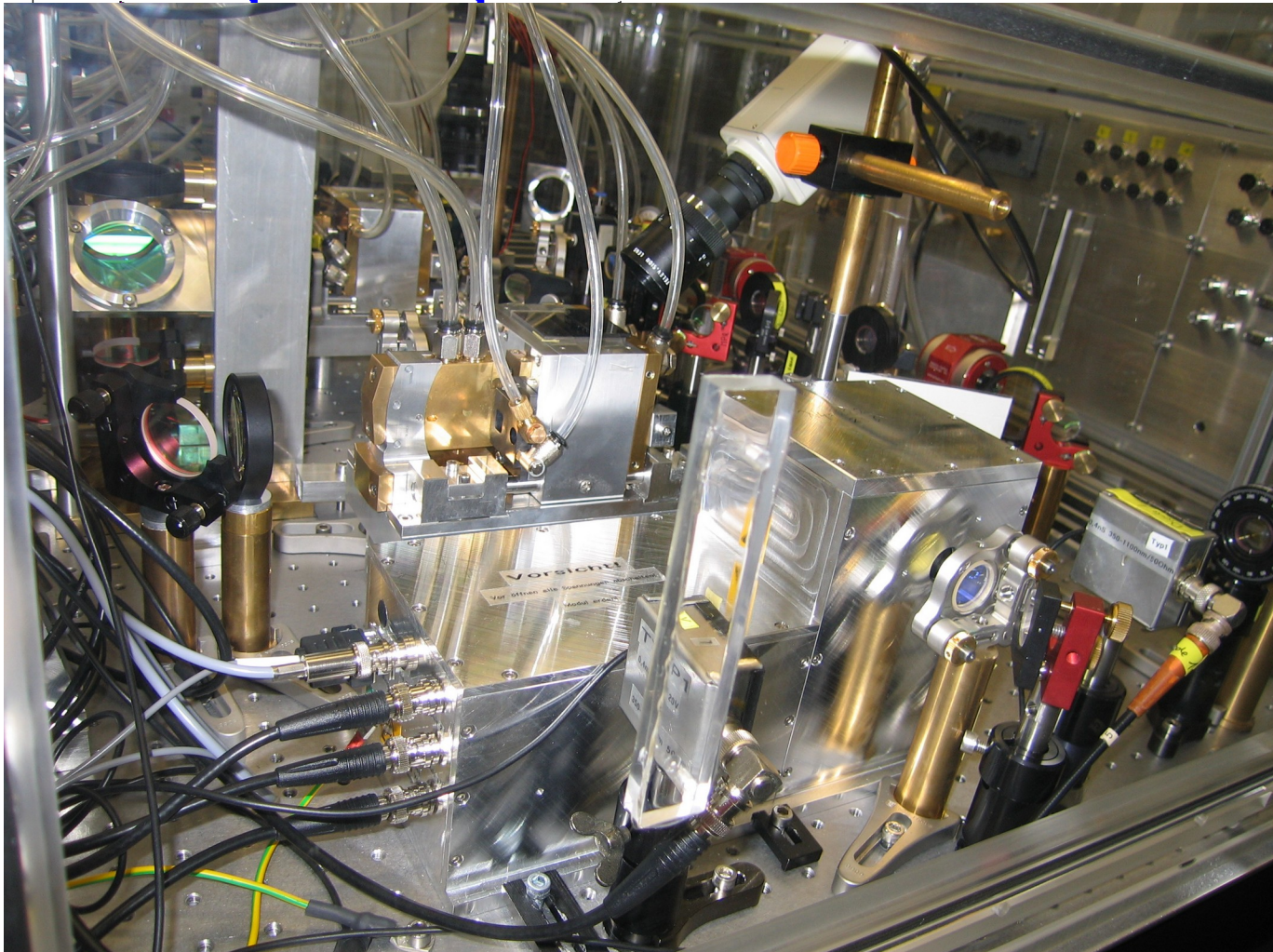
Frequency doubling (SHG)
→ green light to pump
Ti:sapphire laser

Ti:sapphire cw laser
→ determines laser frequency

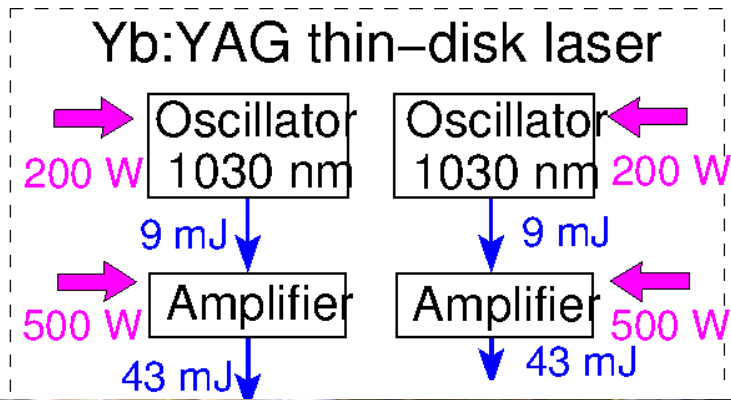
Ti:sapphire MOPA
→ high pulse energy (15 mJ)

Raman cell
→ 3 sequential stimulated
Raman Stokes shifts
Laser wave length → 6 μ m

Target Cavity
→ Mirror system to fill the
muon stop volume (H_2)



Laser system: Yb:YAG Disk Ampli



Yb:YAG Disk laser
→ fast response on μ

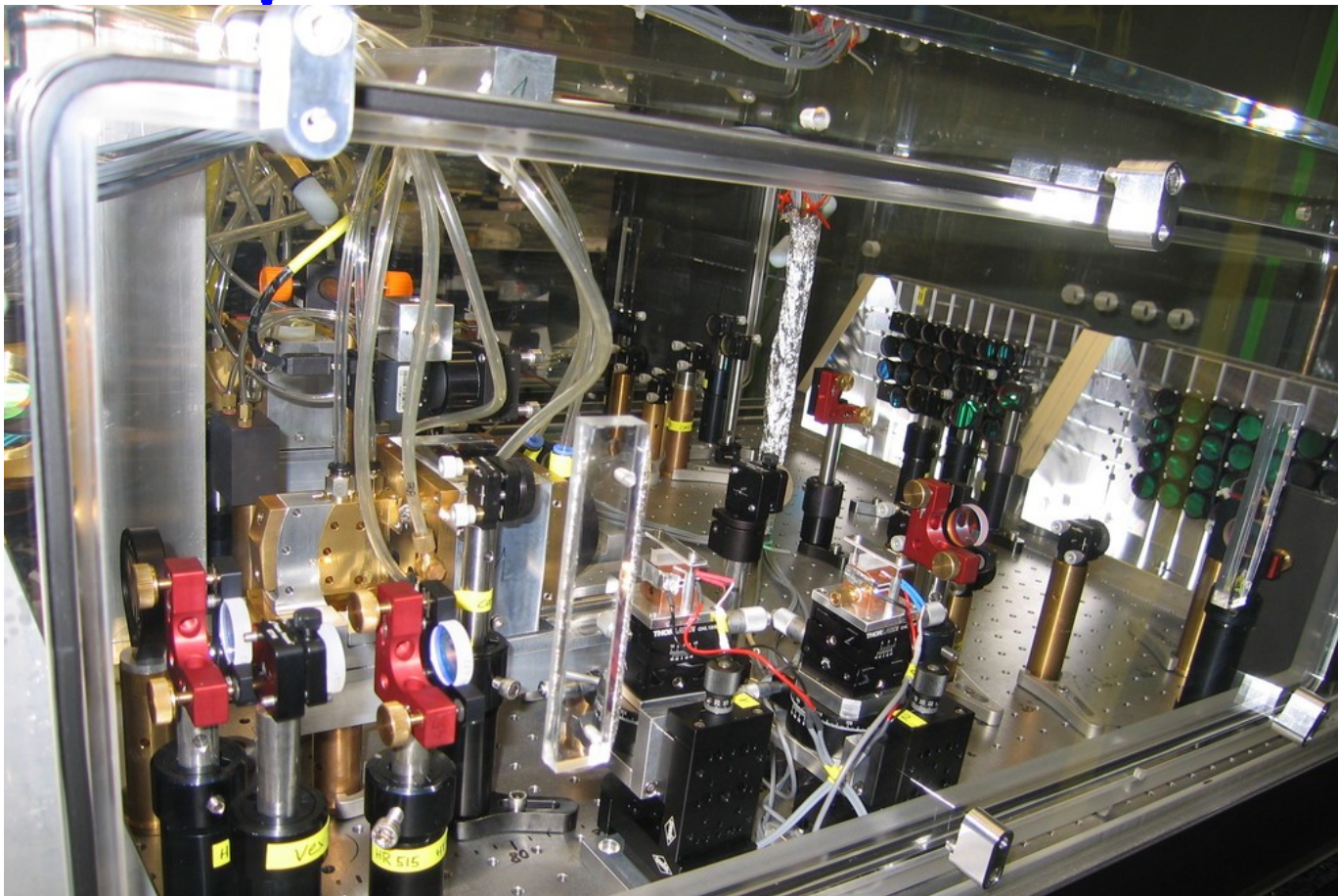
Frequency doubling (SHG)
→ green light to pump
Ti:sapphire laser

Ti:sapphire cw laser
→ determines laser frequency

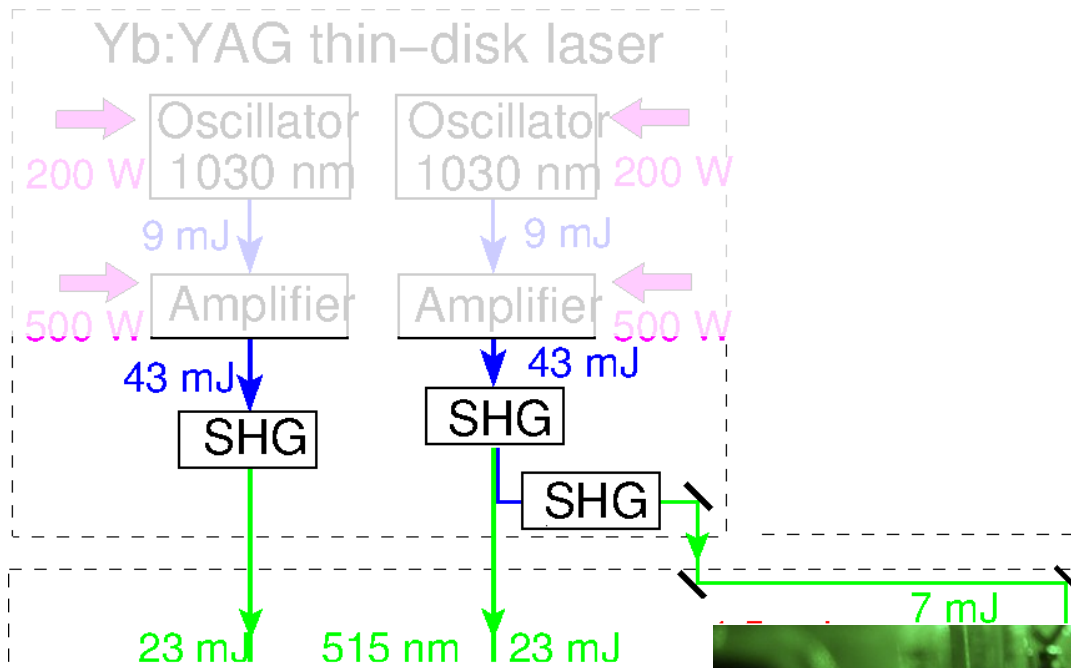
Ti:sapphire MOPA
→ high pulse energy (15 mJ)

Raman cell
→ 3 sequential stimulated
Raman Stokes shifts
Laser wave length → 6 μ m

Target Cavity
→ Mirror system to fill the
muon stop volume (H_2)



Laser system: SHG

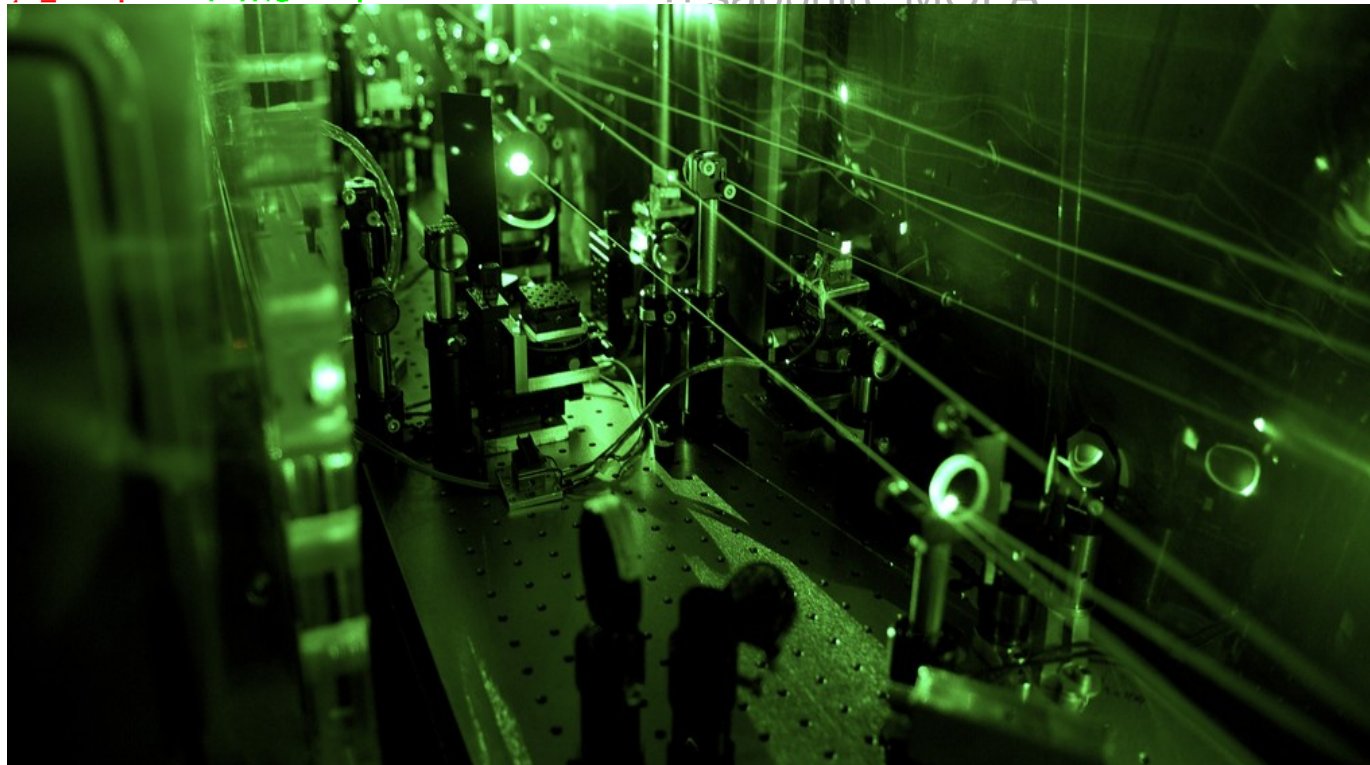


Yb:YAG Disk laser
→ fast response on μ

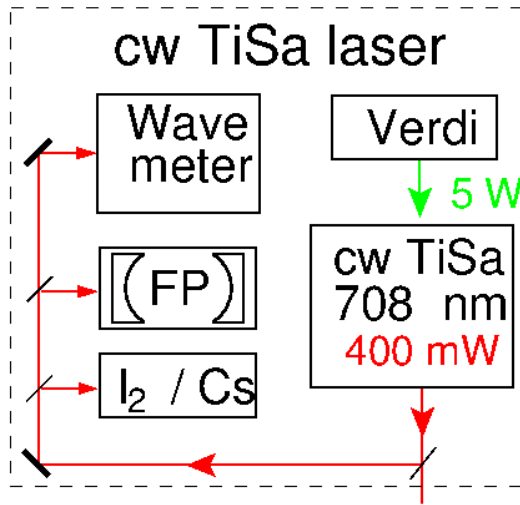
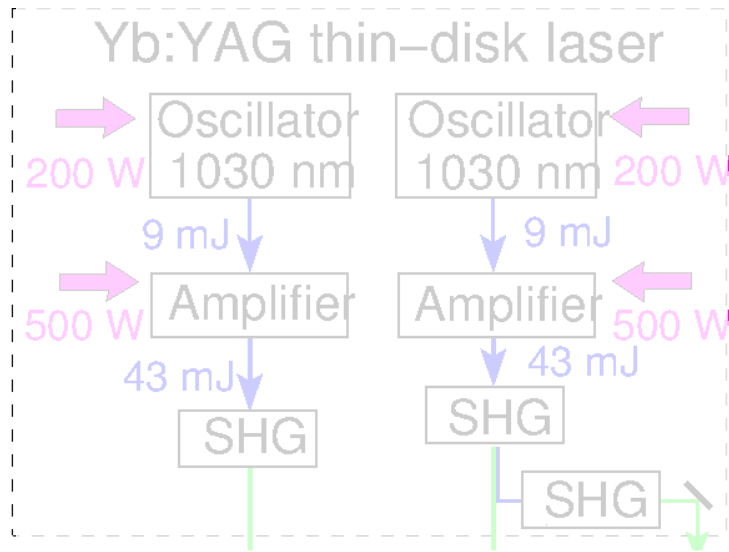
Frequency doubling (SHG)
→ green light to pump
Ti:sapphire laser

Ti:sapphire cw laser
→ determines laser frequency

Ti:sapphire MOPA



Laser system: cw Ti:sapphire



Yb:YAG Disk laser
→ fast response on μ

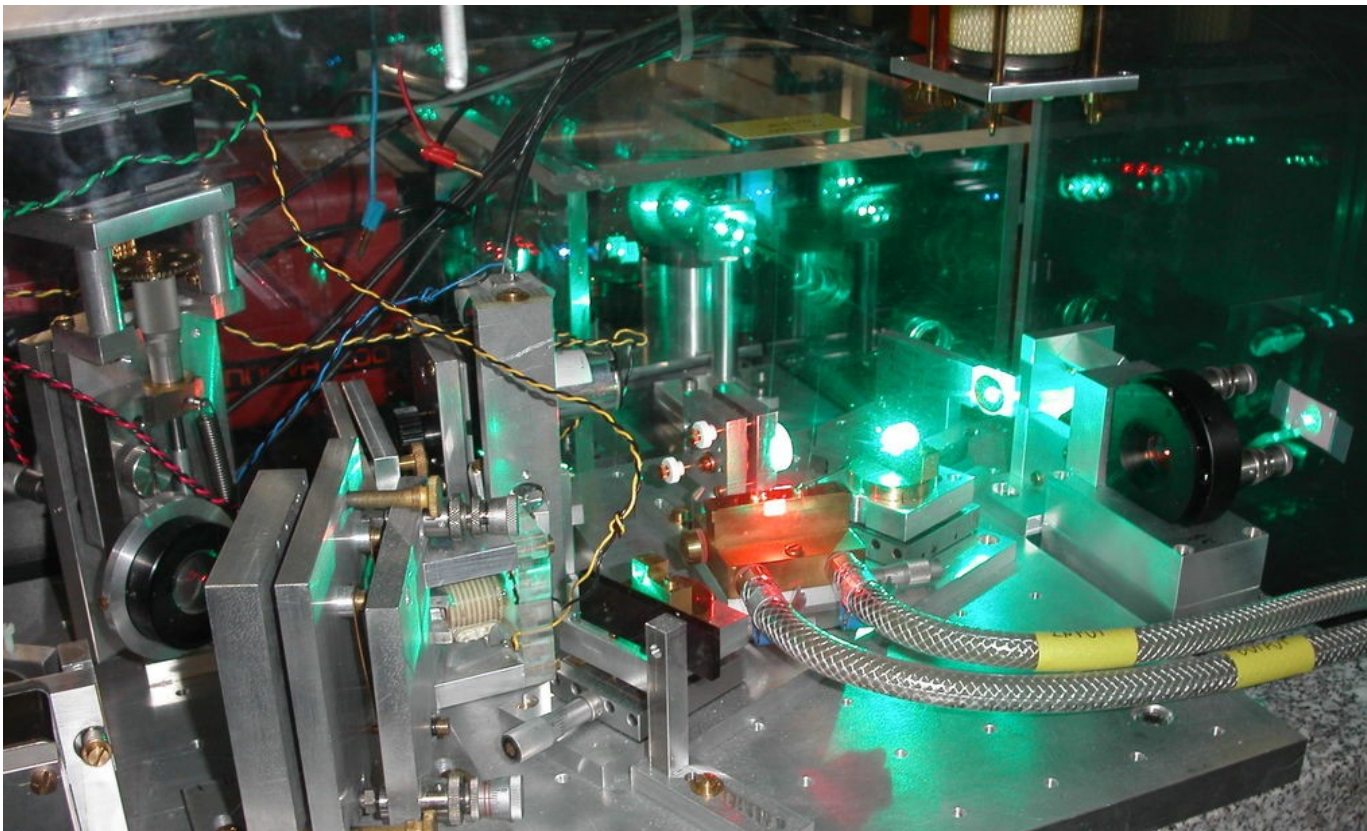
Frequency doubling (SHG)
→ green light to pump
Ti:sapphire laser

Ti:sapphire cw laser
→ determines laser frequency

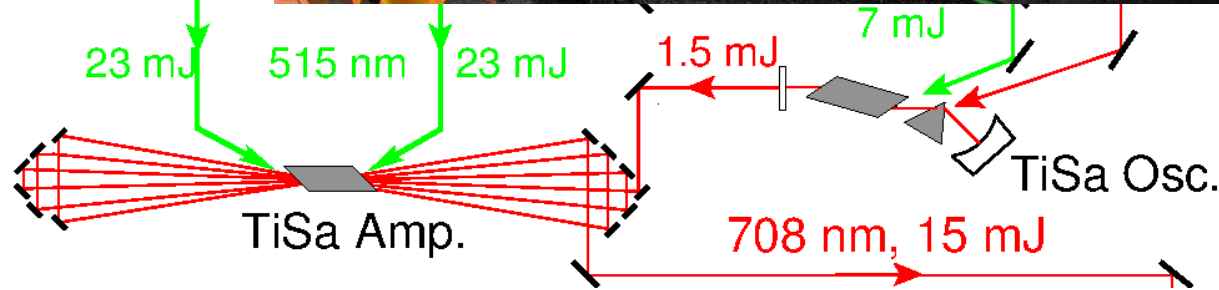
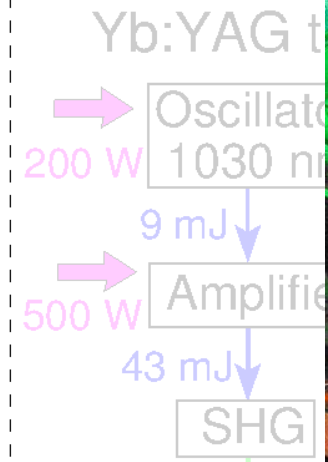
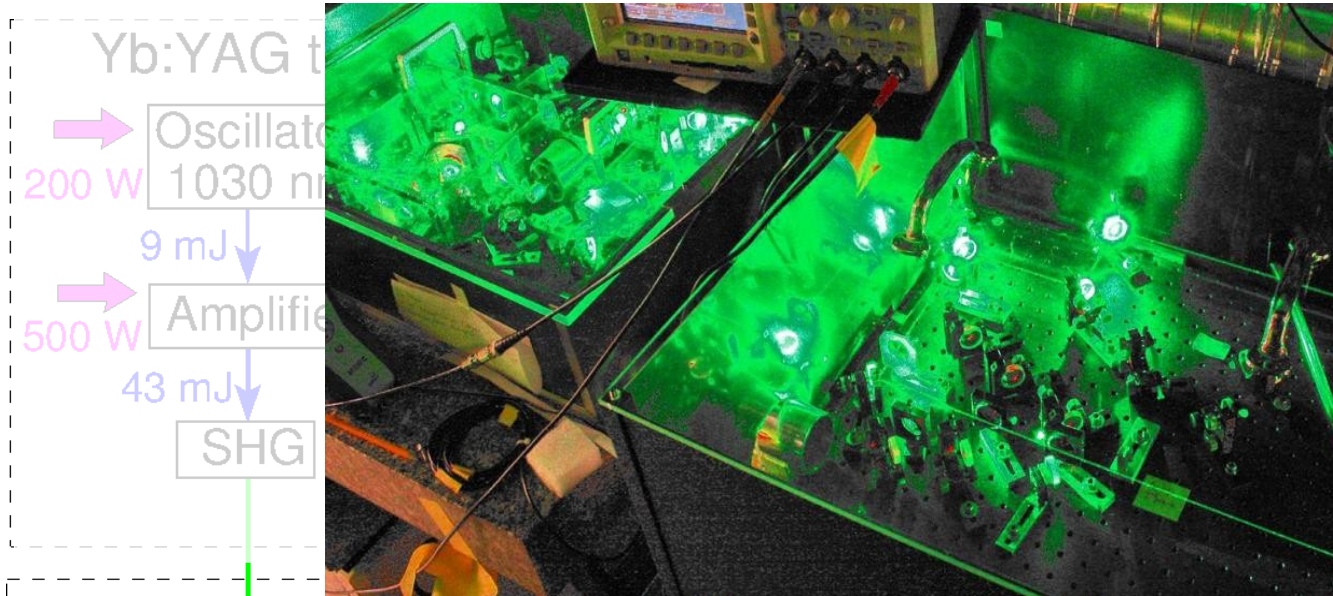
Ti:sapphire MOPA
→ high pulse energy (15 mJ)

Raman cell
→ 3 sequential stimulated
Raman Stokes shifts
Laser wave length → 6 μ m

Target Cavity
→ Mirror system to fill the
muon stop volume (H₂)



Laser system: pulsed Ti:sapphire



Yb:YAG Disk laser
→ fast response on μ

Frequency doubling (SHG)
→ green light to pump
Ti:sapphire laser

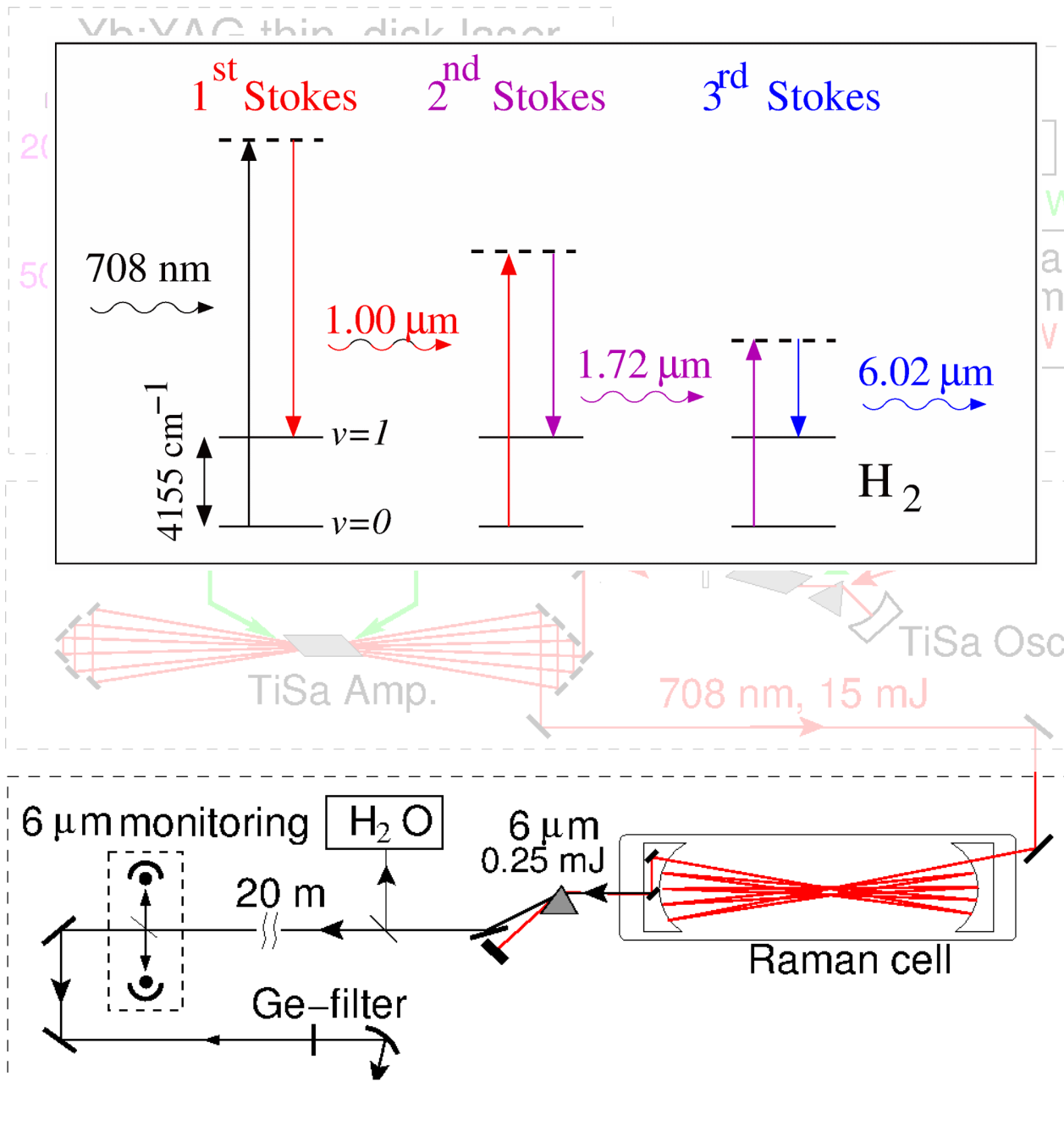
Ti:sapphire cw laser
→ determines laser frequency

Ti:sapphire MOPA
→ high pulse energy (15 mJ)

Raman cell
→ 3 sequential stimulated
Raman Stokes shifts
Laser wave length → 6 μ m

Target Cavity
→ Mirror system to fill the
muon stop volume (H_2)

Laser system: Raman cell



Yb:YAG Disk laser
 → fast response on μ

Frequency doubling (SHG)
 → green light to pump
 Ti:sapphire laser

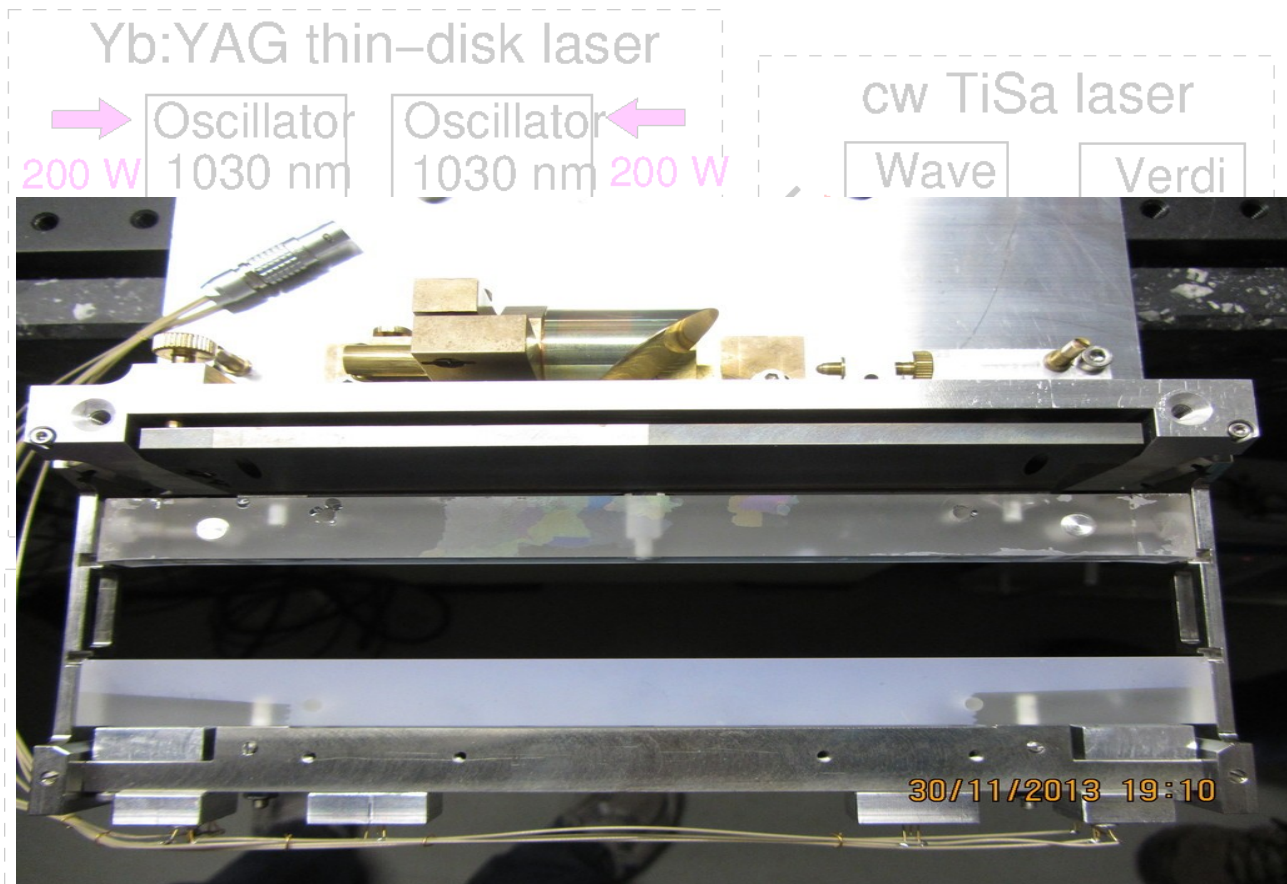
Ti:sapphire cw laser
 → determines laser frequency

Ti:sapphire MOPA
 → high pulse energy (15 mJ)

Raman cell
 → 3 sequential stimulated
 Raman Stokes shifts
 Laser wave length → 6 μm

Target Cavity
 → Mirror system to fill the
 muon stop volume (H_2)

Laser system: Target cavity



Yb:YAG Disk laser
→ fast response on μ

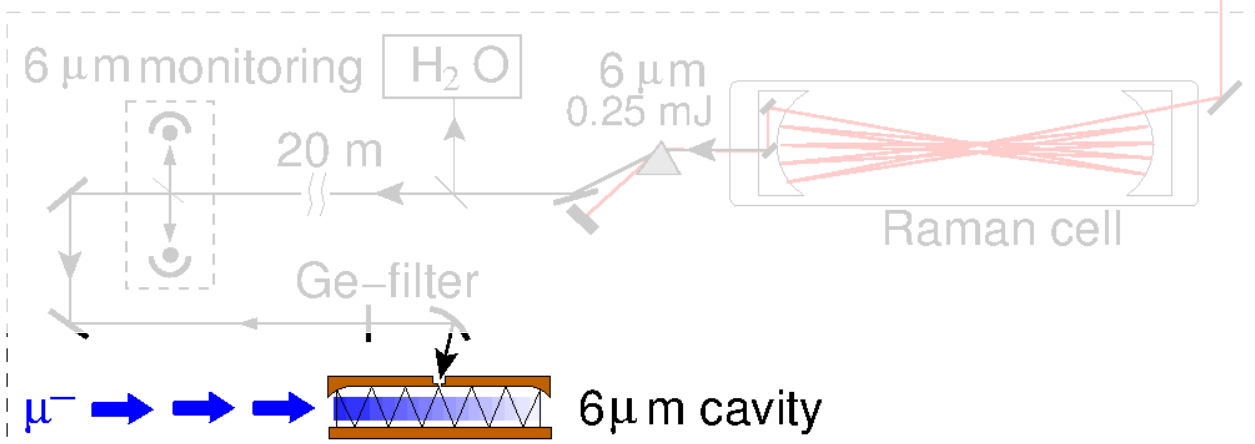
Frequency doubling (SHG)
→ green light to pump
Ti:sapphire laser

Ti:sapphire cw laser
→ determines laser frequency

Ti:sapphire MOPA
→ high pulse energy (15 mJ)

Raman cell
→ 3 sequential stimulated
Raman Stokes shifts
Laser wave length → 6 μ m

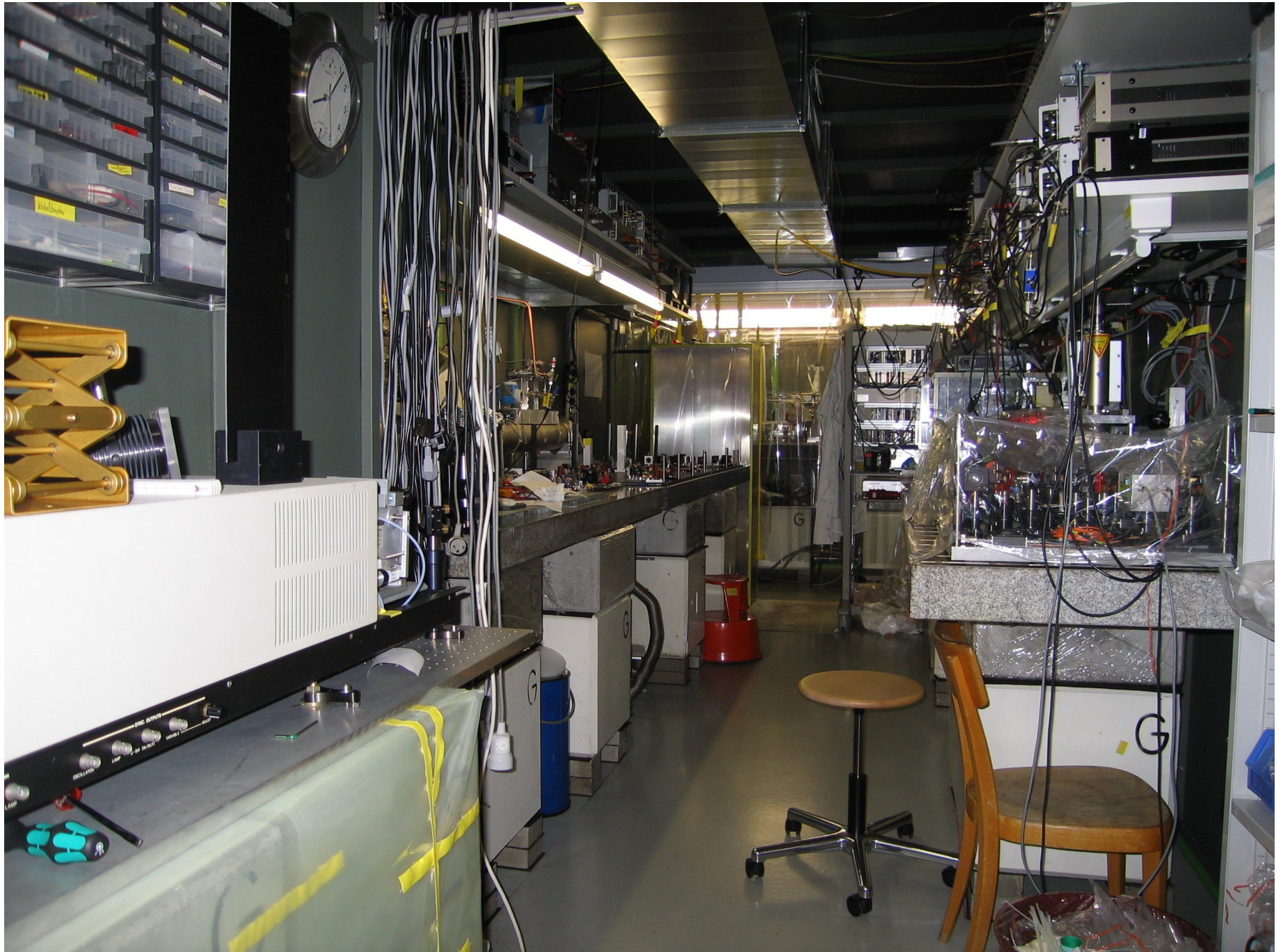
Target Cavity
→ Mirror system to fill the
muon stop volume (H_2)



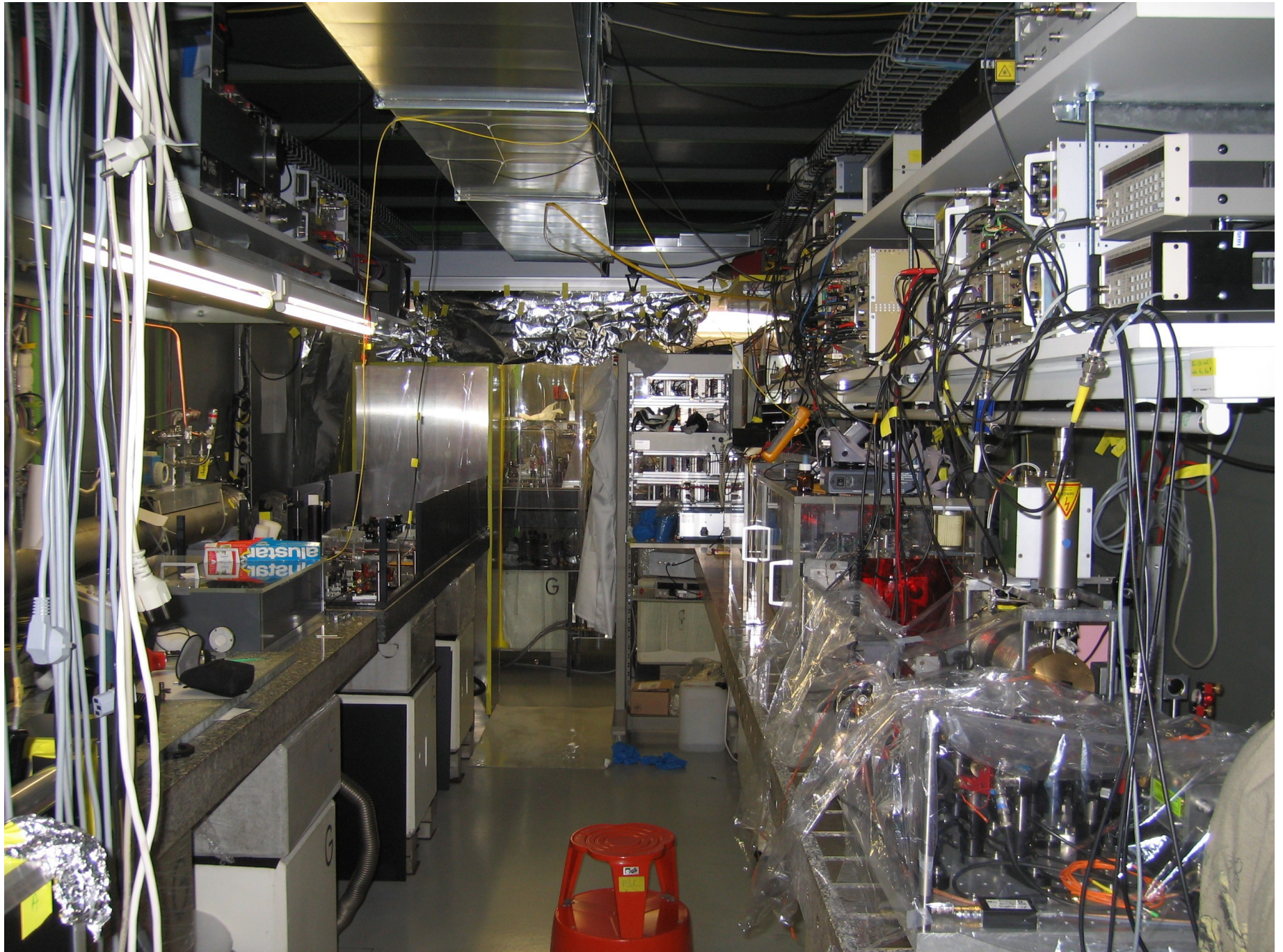
In der Laserhütte



In der Laserhütte



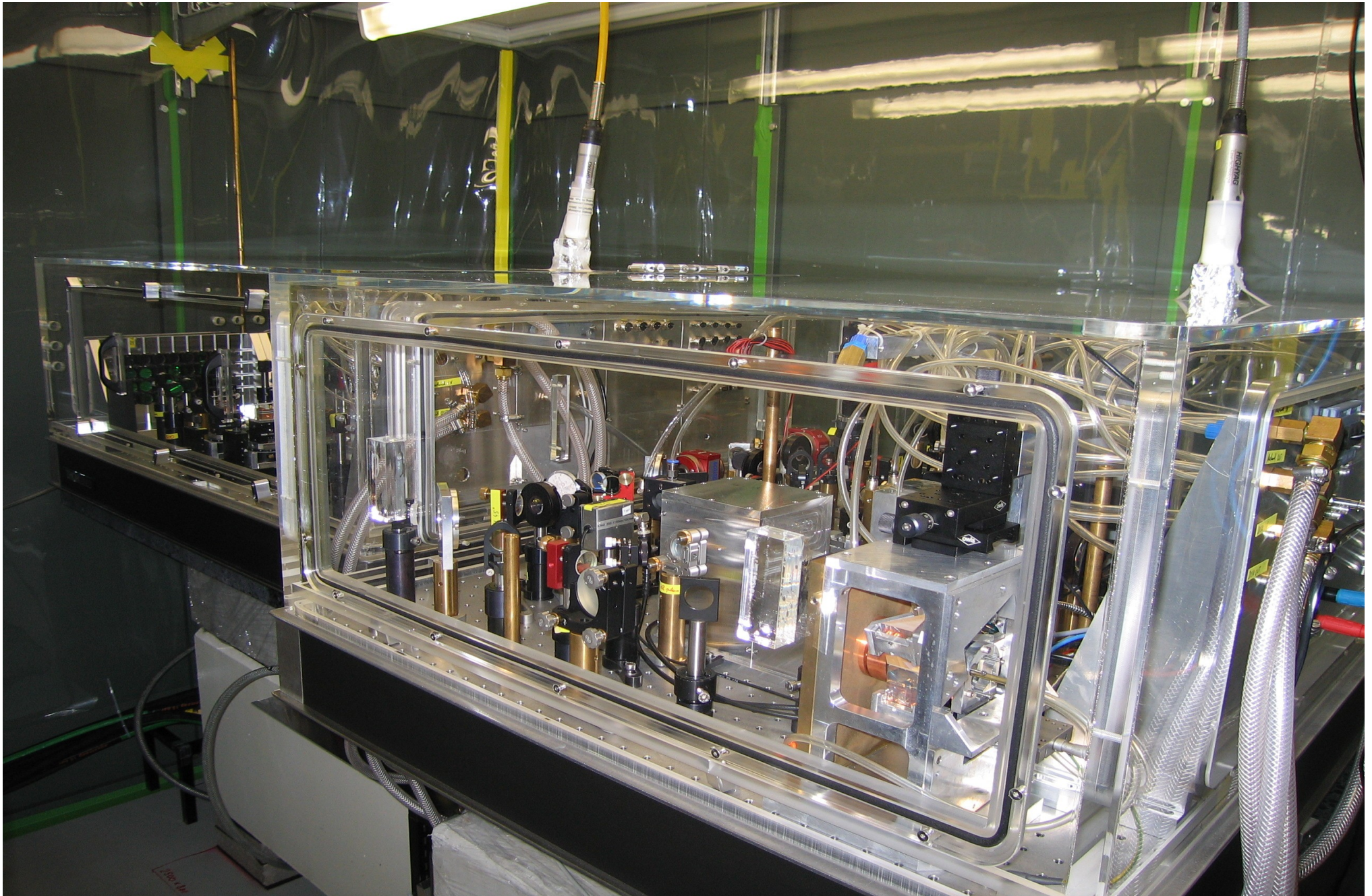
Inside the laser hut at PSI



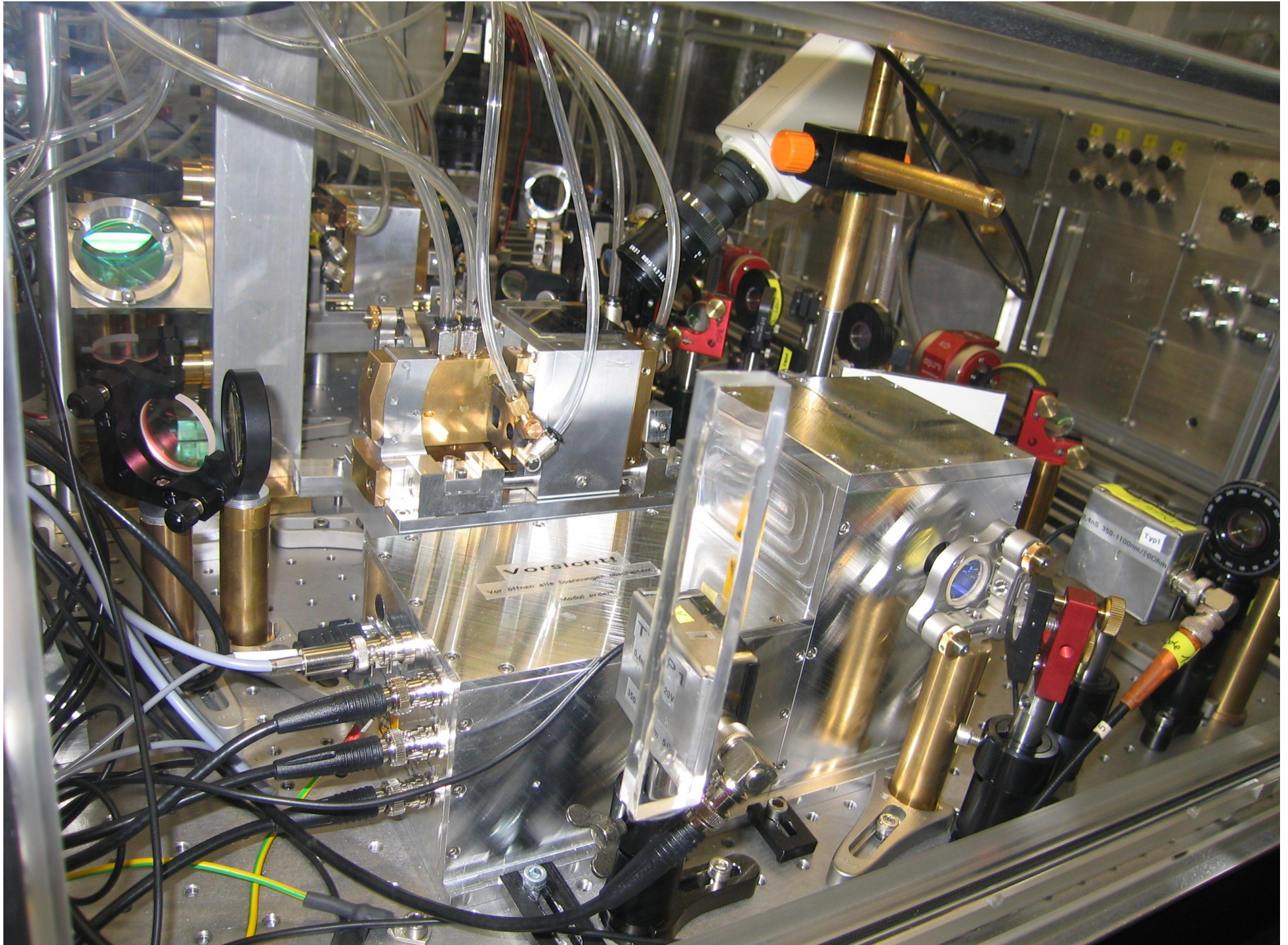
The laser hut at PSI



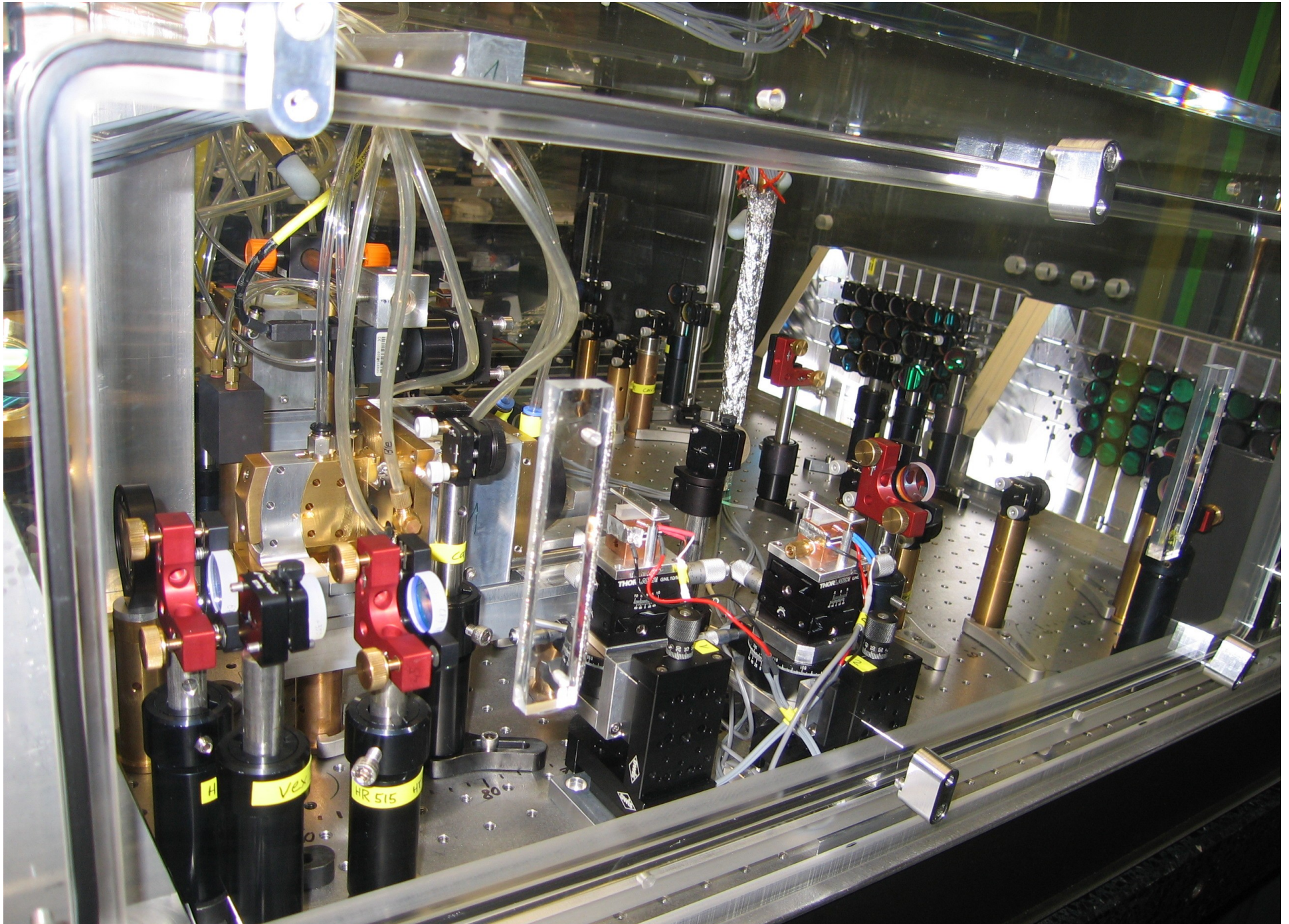
Yb:YAG thin-disk lasers



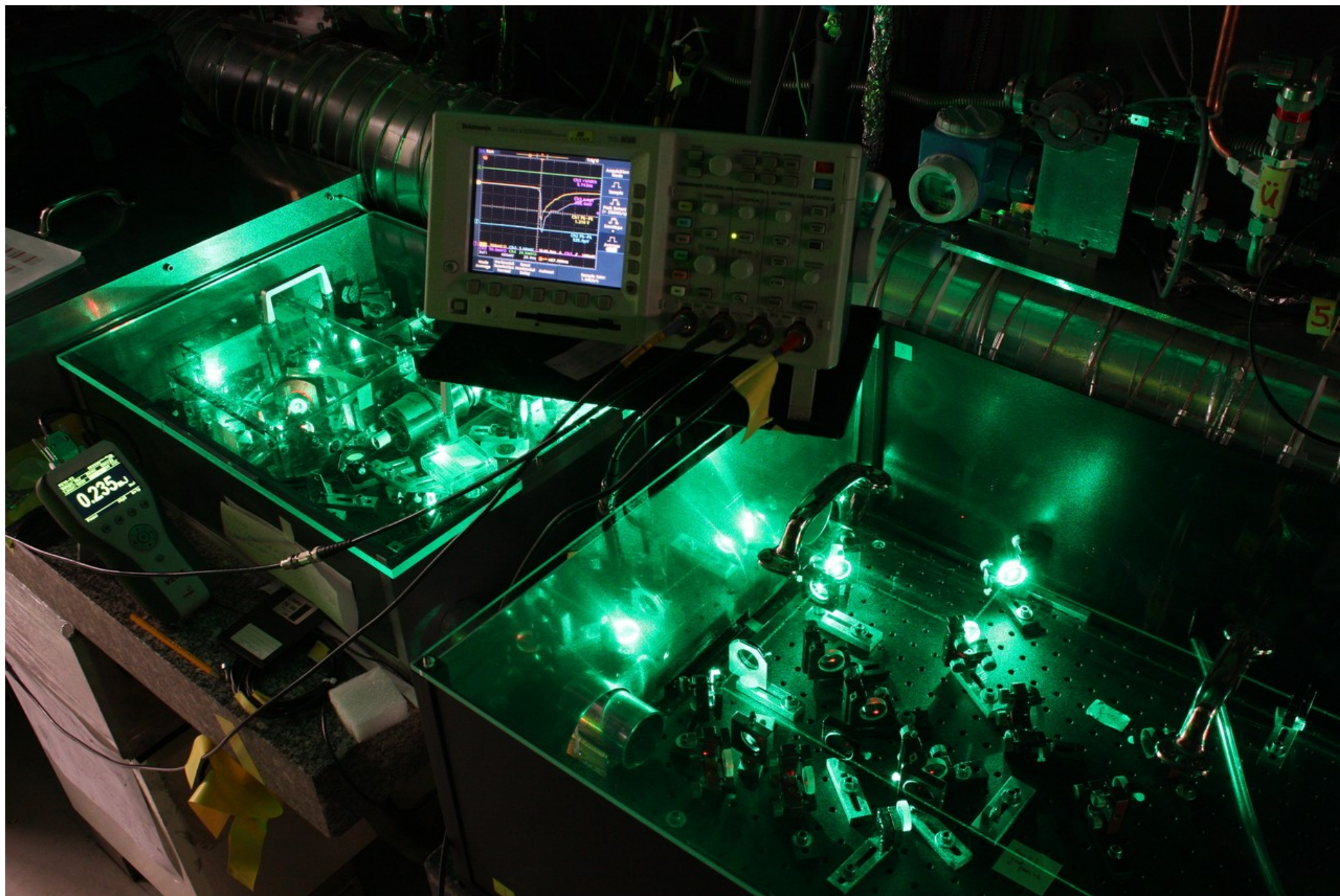
Yb:YAG Disk Oscillators



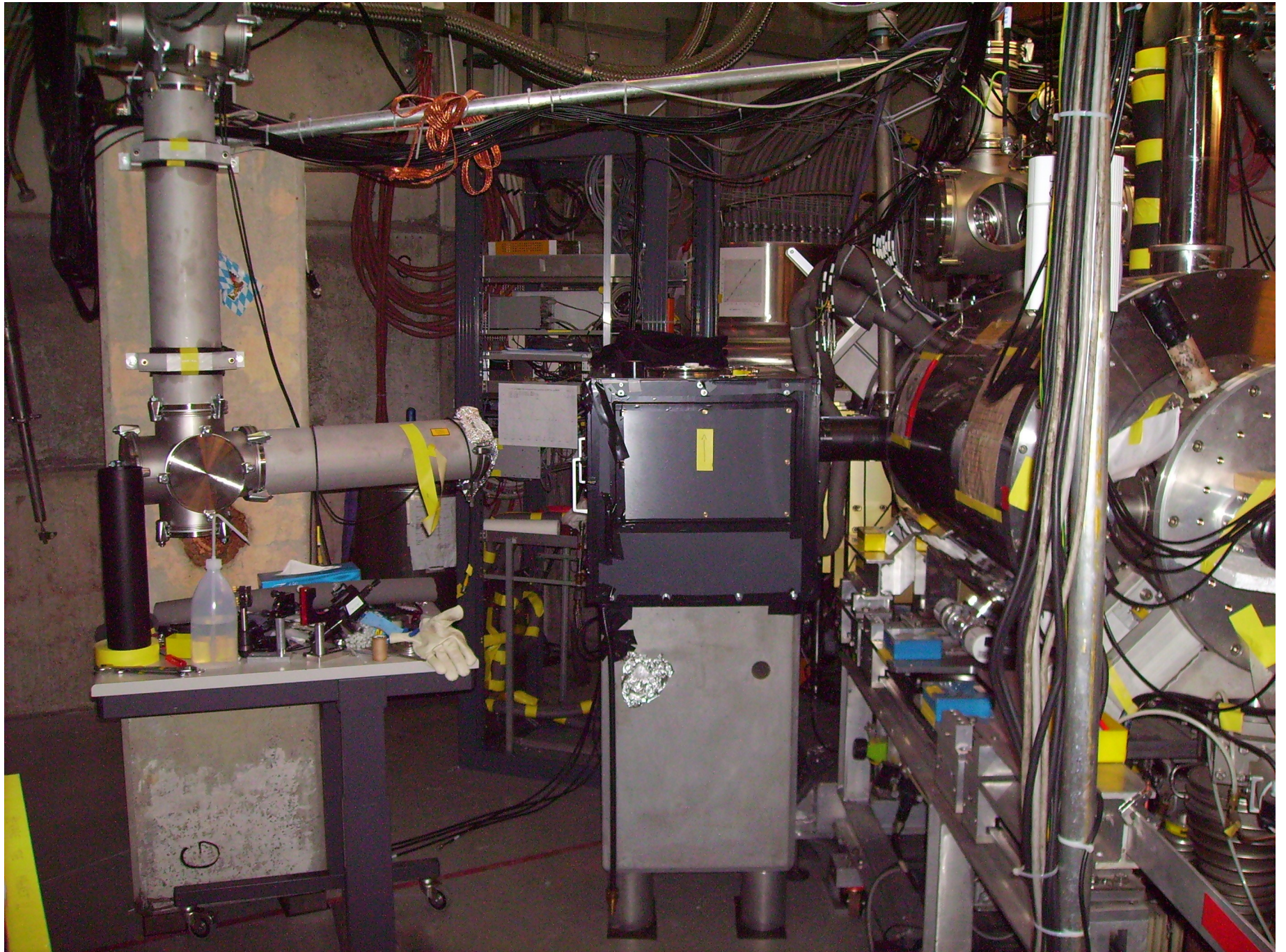
Yb:YAG Disk Amplifiers



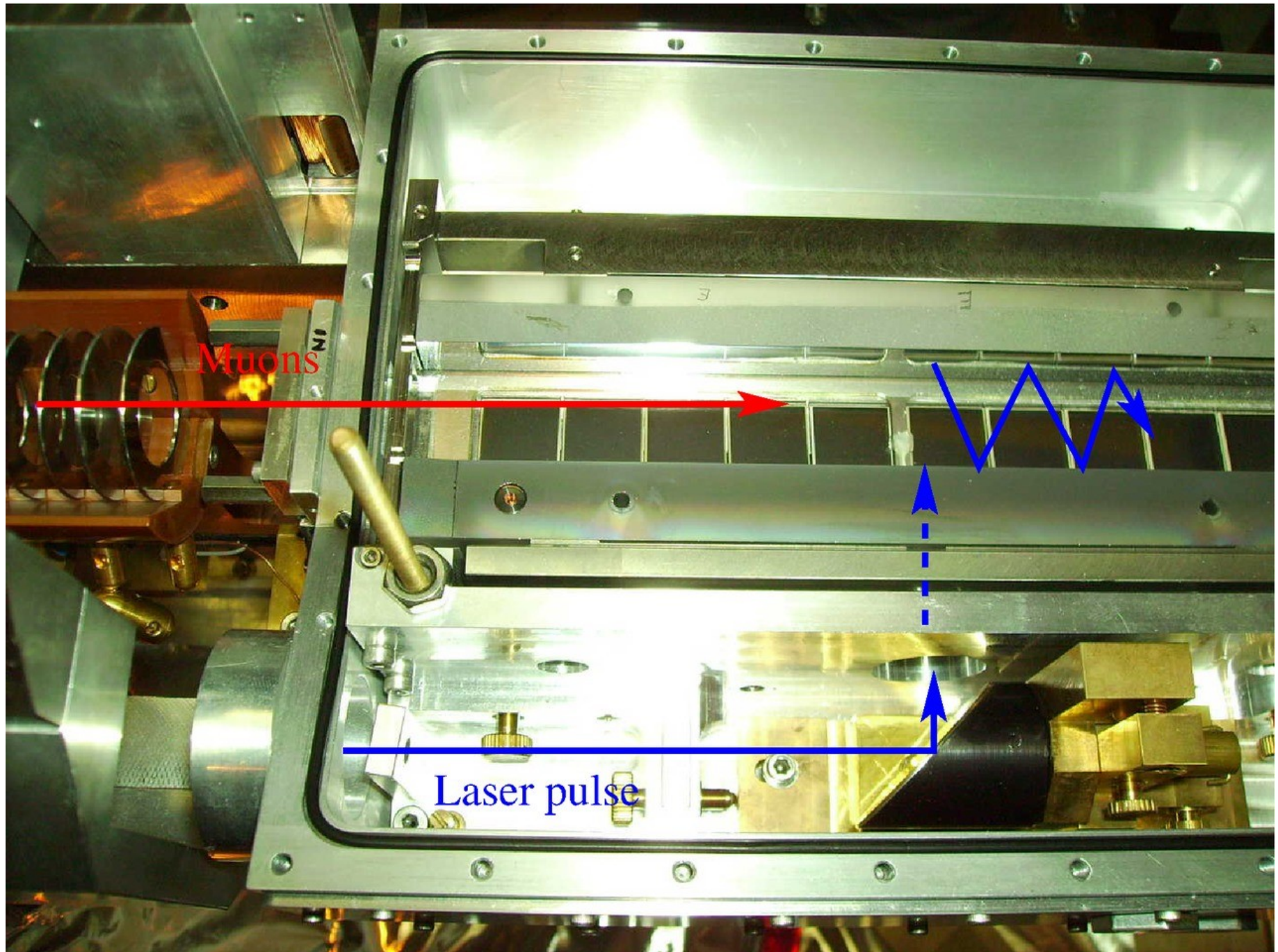
Ti:sapphire lasers



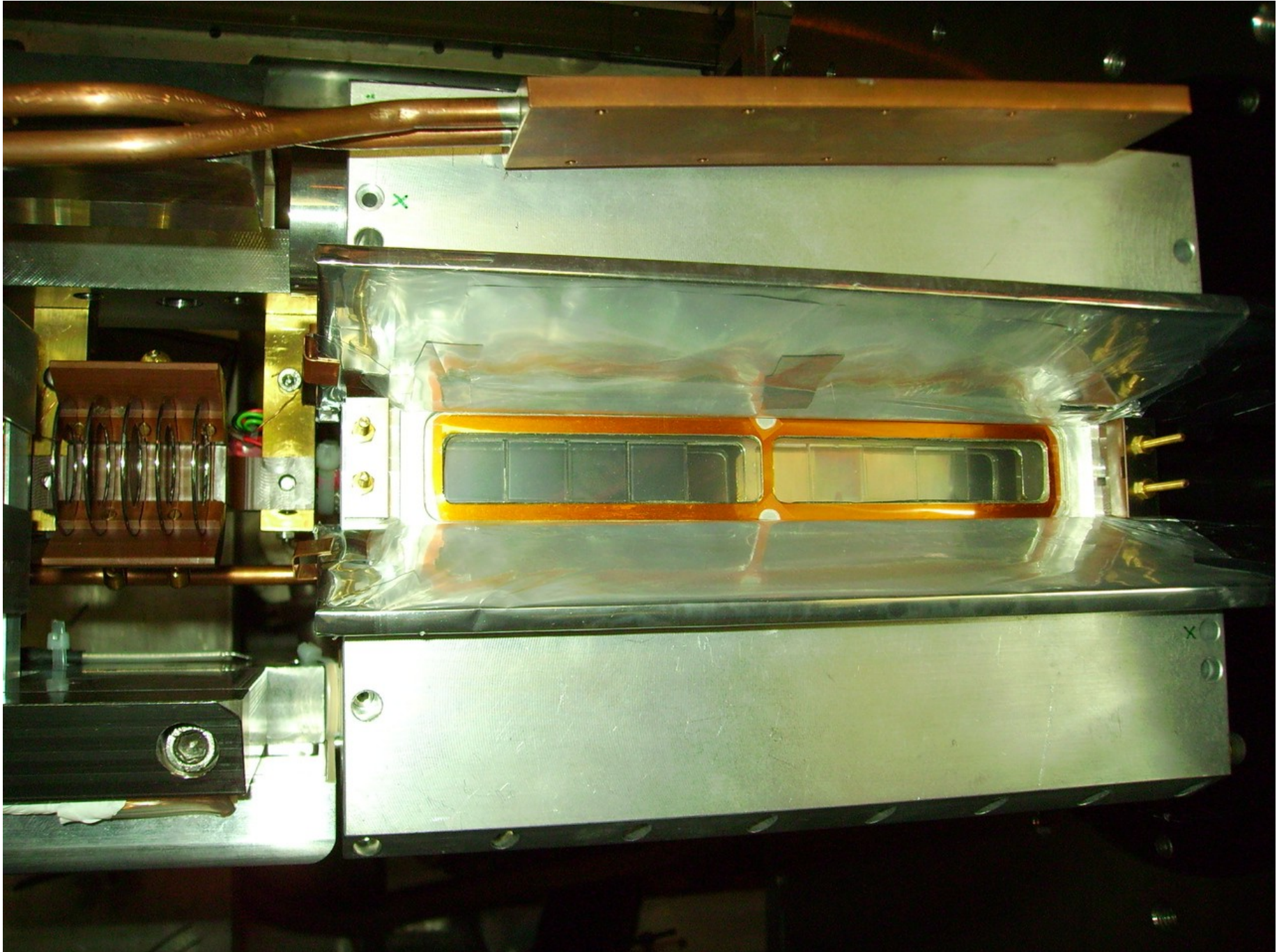
Light at the end of the tunnel



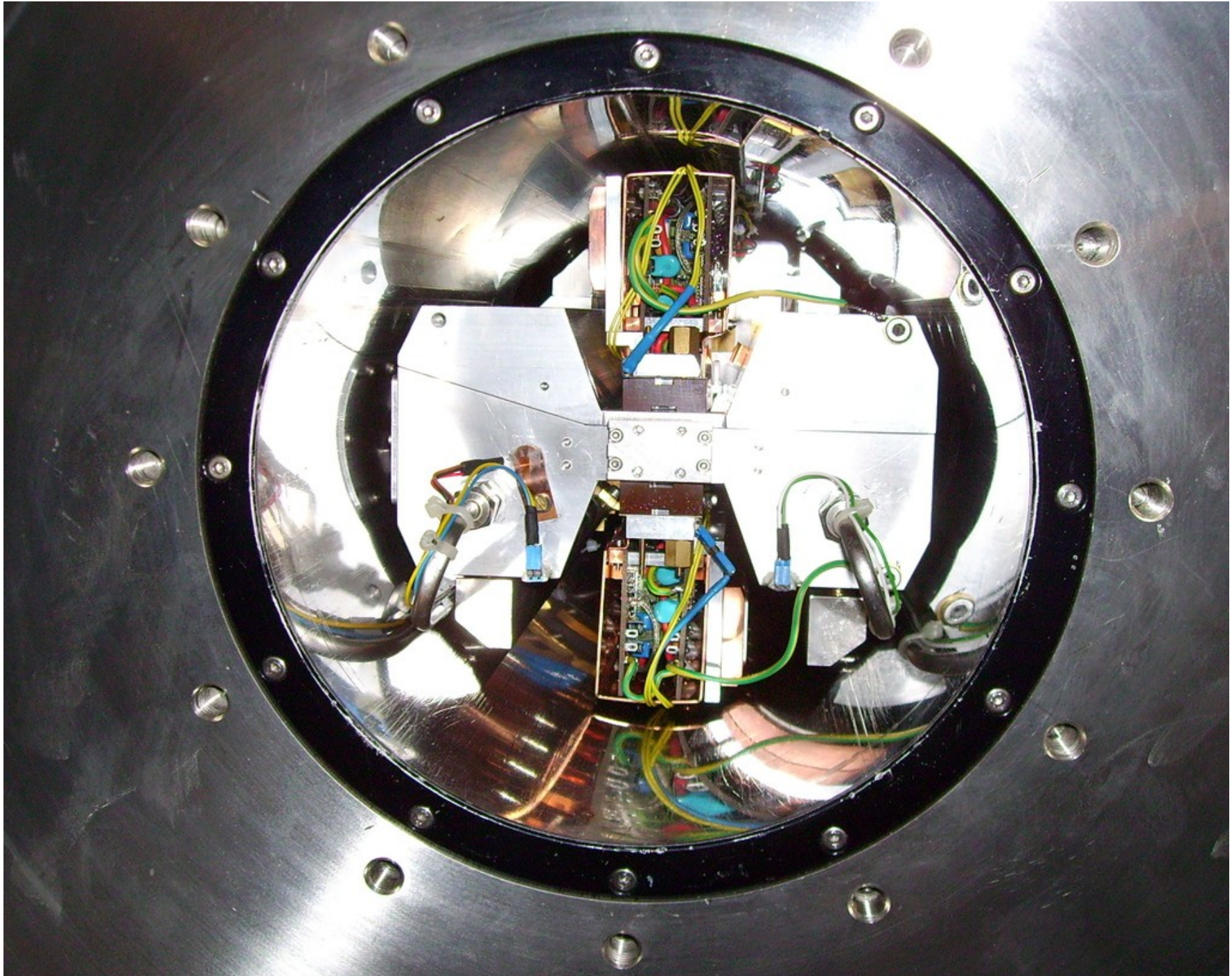
The hydrogen target



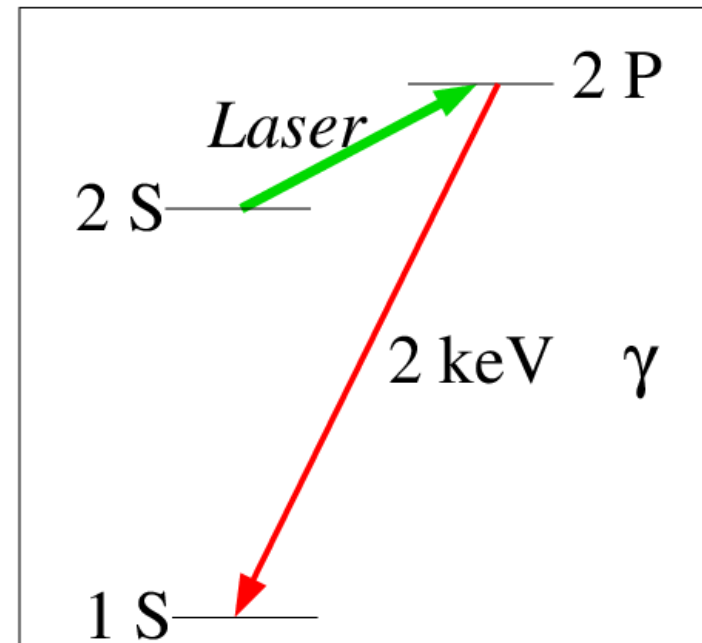
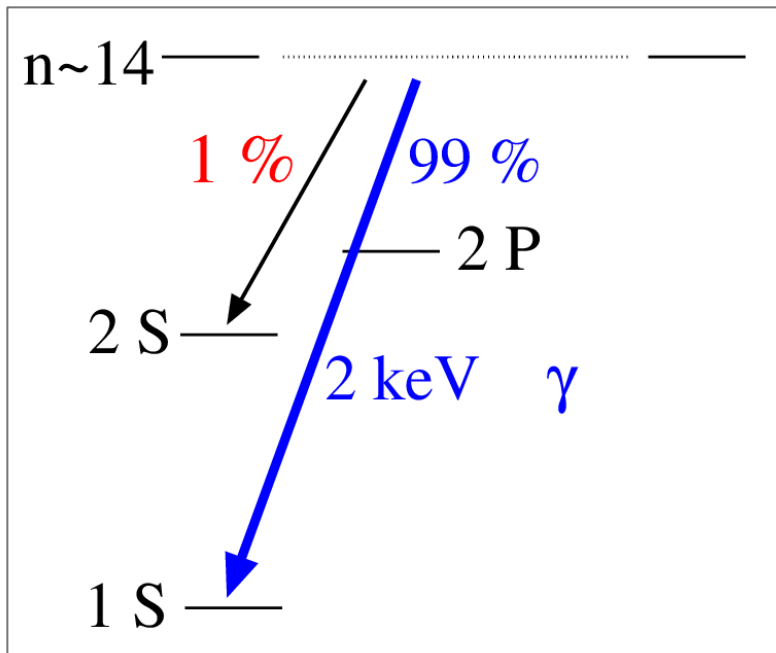
Das Herzstück -- Target



Das Herzstück -- Target



Prinzip der Messung



“prompt” ($t=0$):

- * Einfang des Myons bei $n \sim 14$
- * Kaskade
- * 99% enden im Grundzustand

→ “prompte” Röntgenquanten

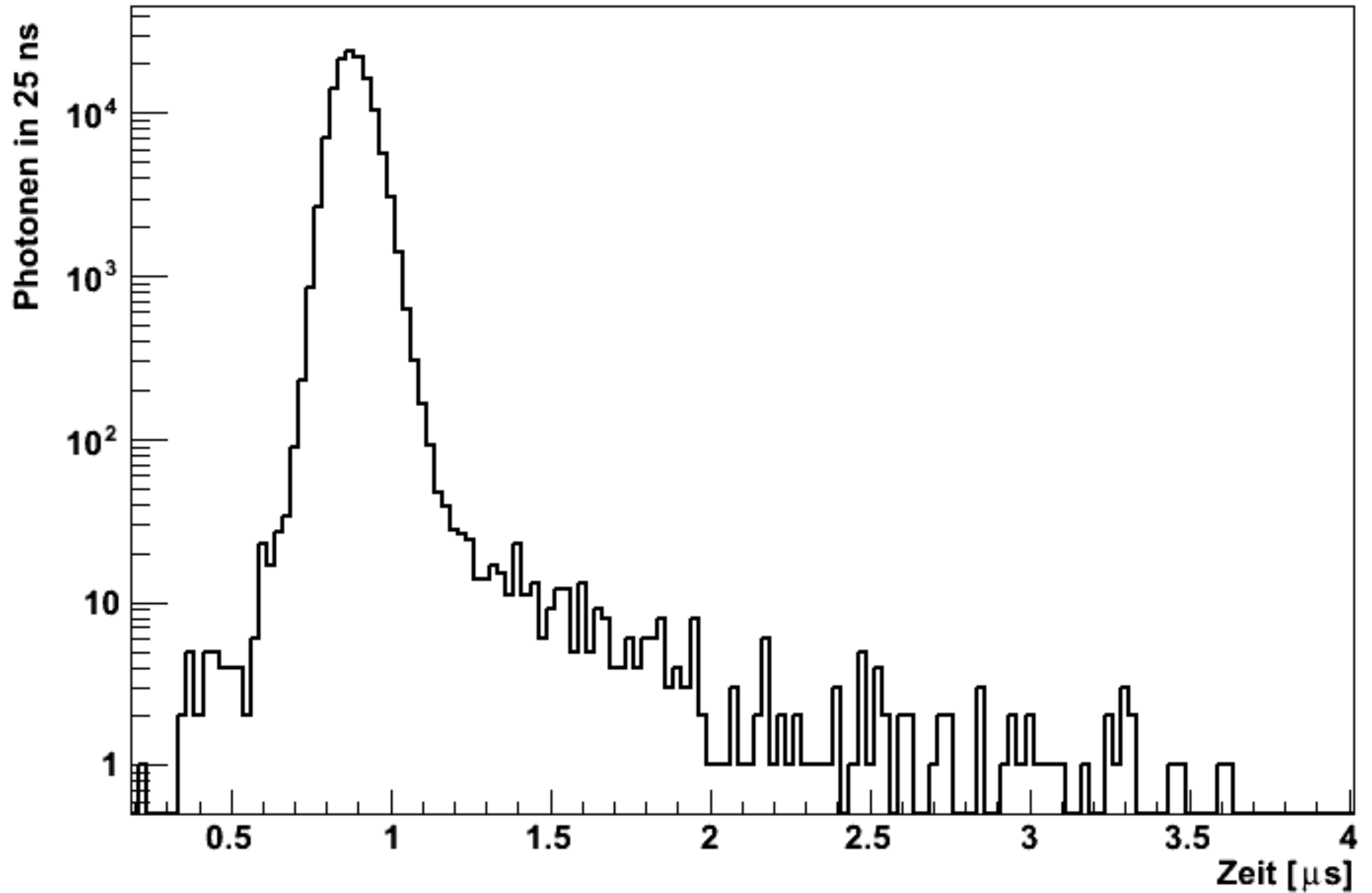
“später” ($t \sim 1 \mu\text{s}$):

- * 1% der Myonen sind im $2S$ -Zustand
- * Laser auf Resonanz ($\lambda=6 \mu\text{m}$)
- * $2S \rightarrow 2P \rightarrow 1S$

→ “verzögerte” Röntgenquanten

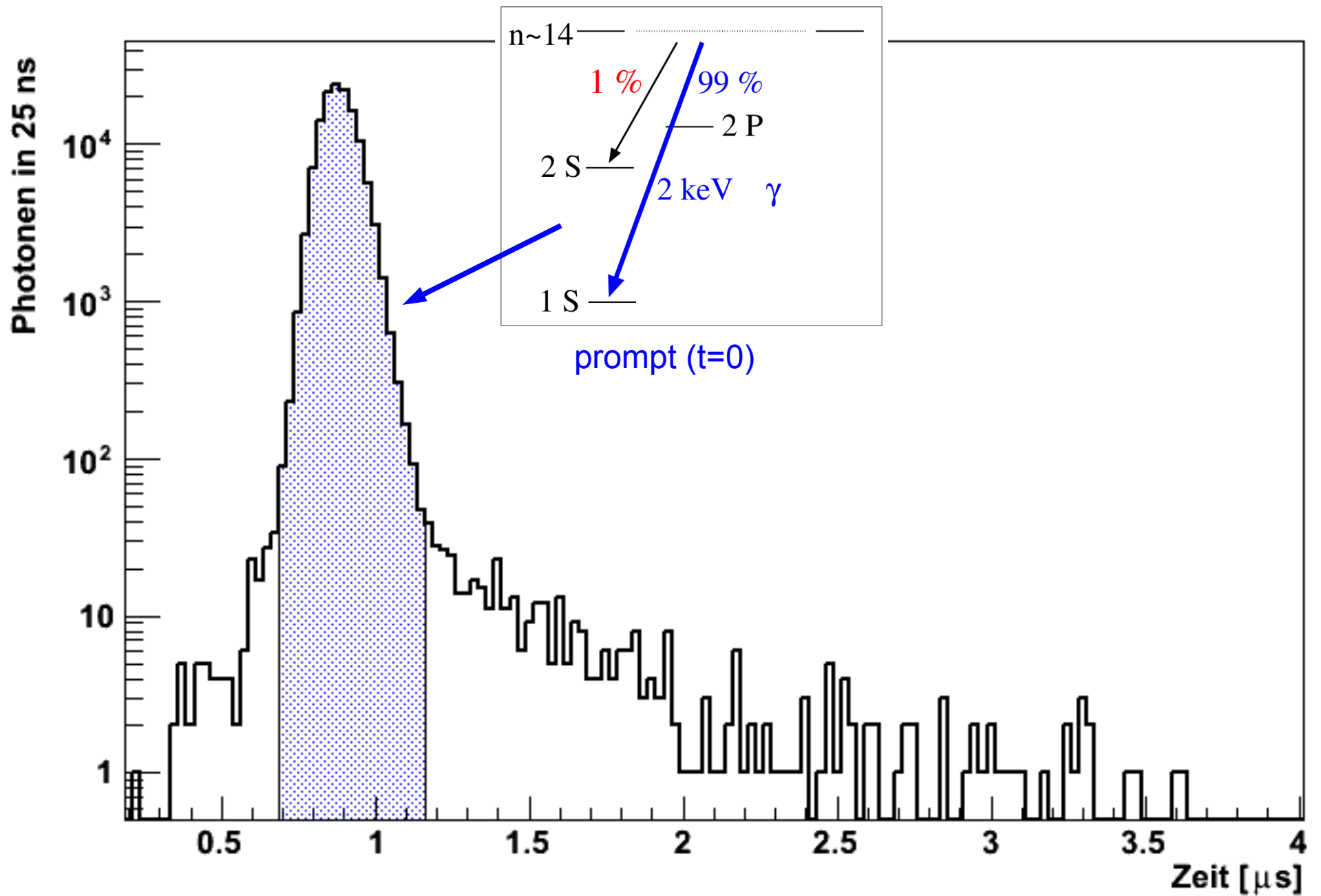
Time Spectra

13 hours of data

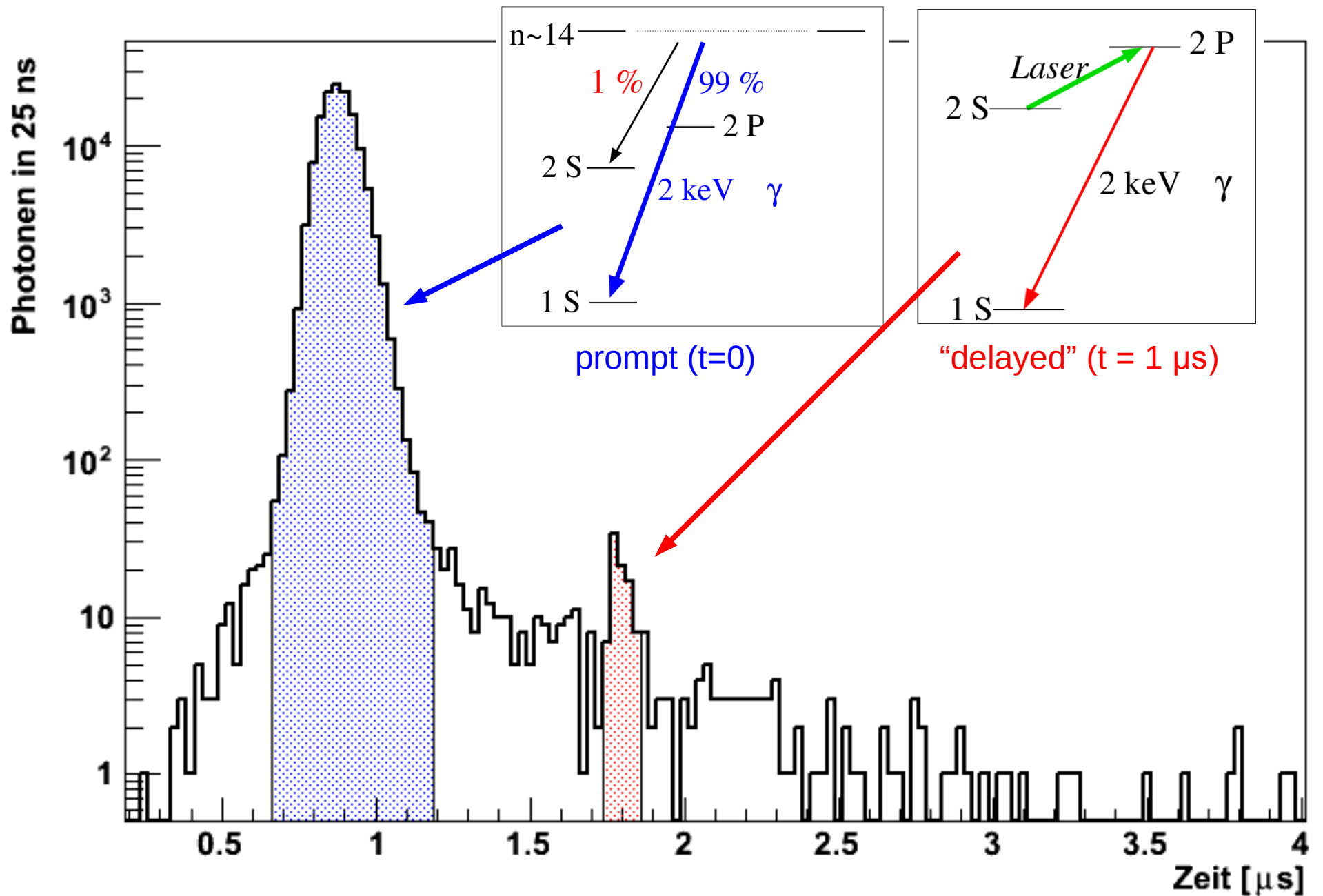


Time Spectra

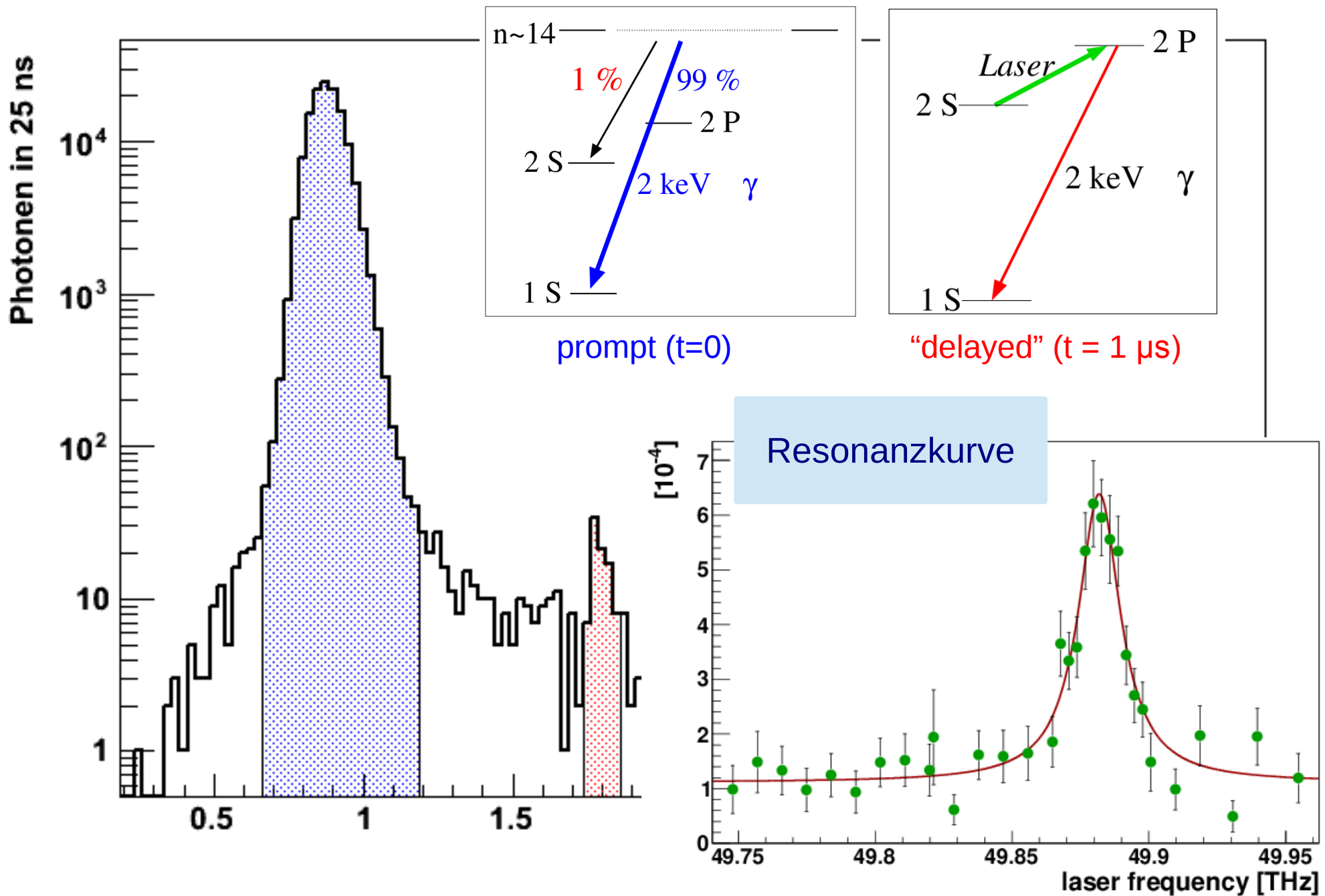
13 hours of data



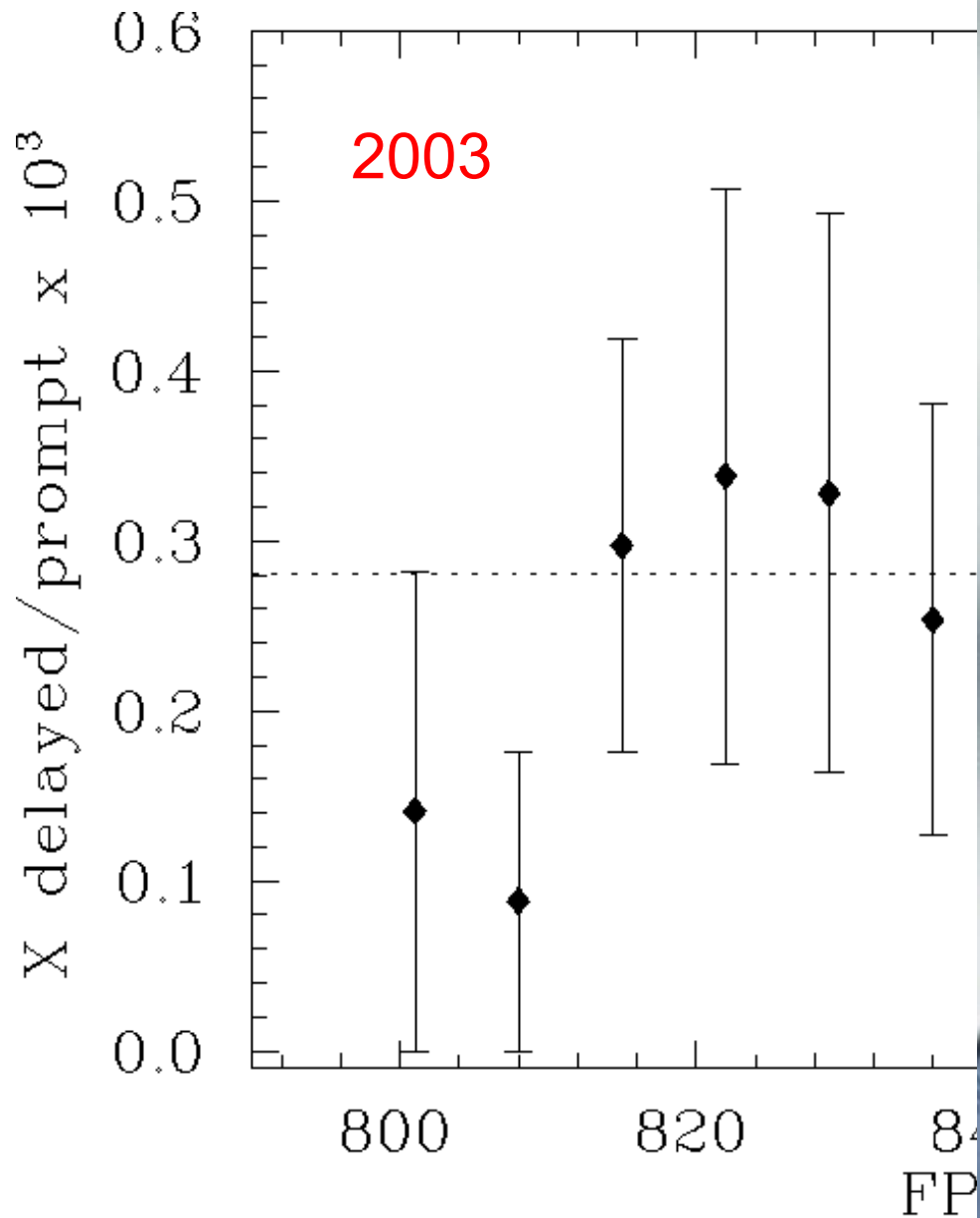
Time Spectra



Time Spectra



Eine lange C



8 July 2010 | www.nature.com/nature \$10

THE INTERNATIONAL WEEKLY JOURNAL OF SCIENCE

nature

OIL SPILLS
There's more
to come

PLAGIARISM
It's worse than
you think

CHIMPANZEES
The battle for
survival

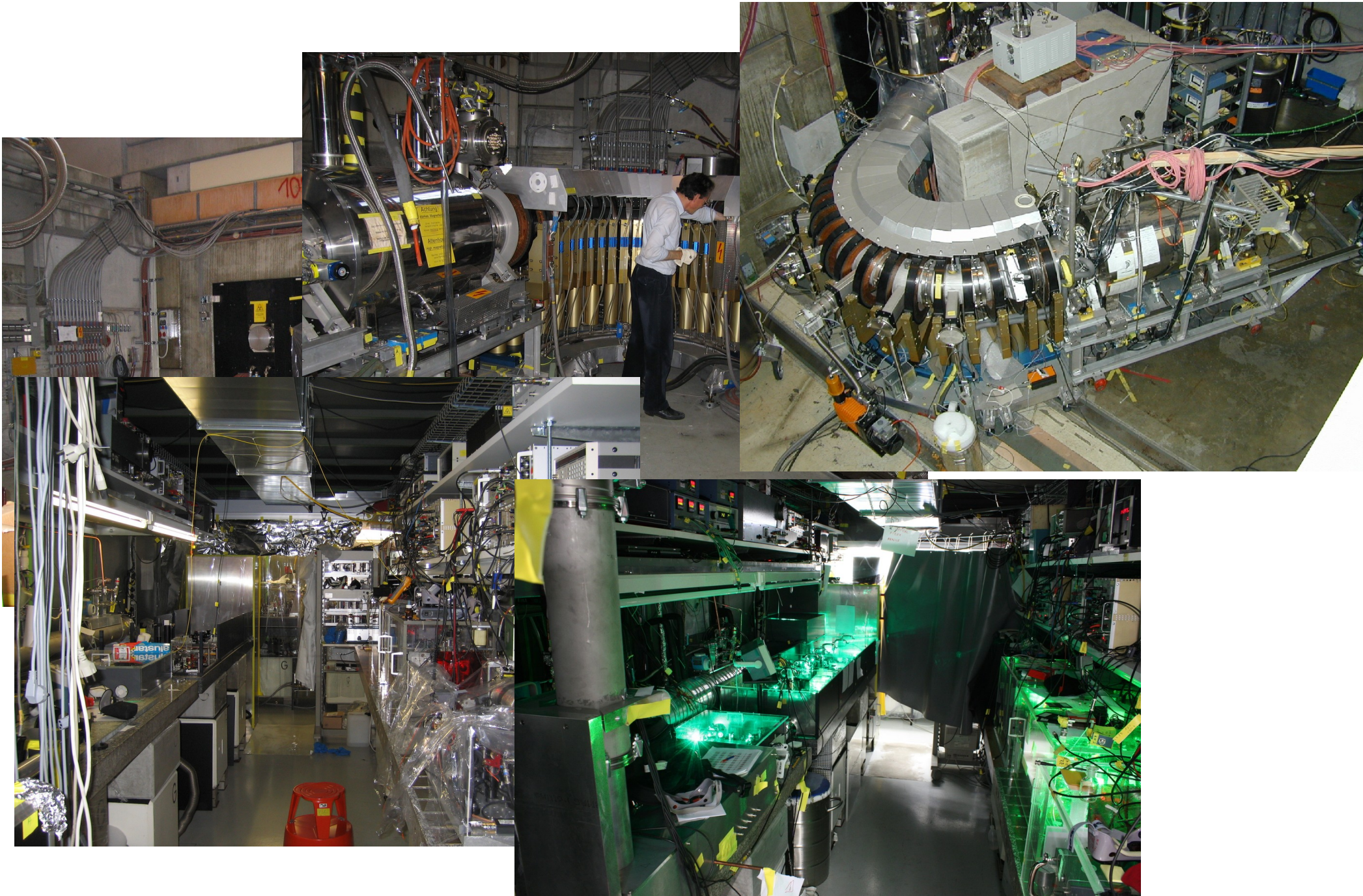
SHRINKING THE PROTON

New value from exotic atom
trims radius by four per cent

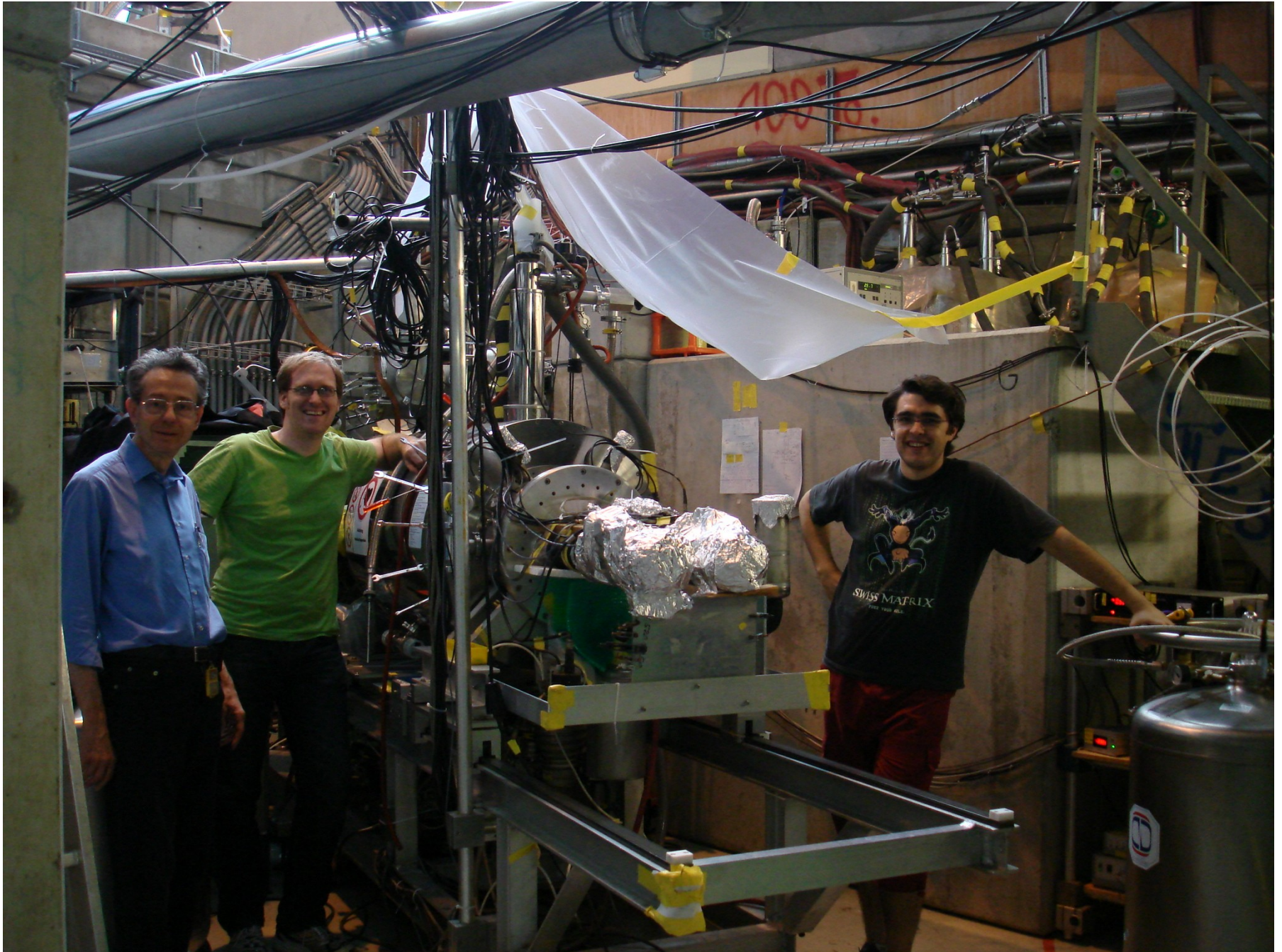
NATURE JOBS
Researchers for hire

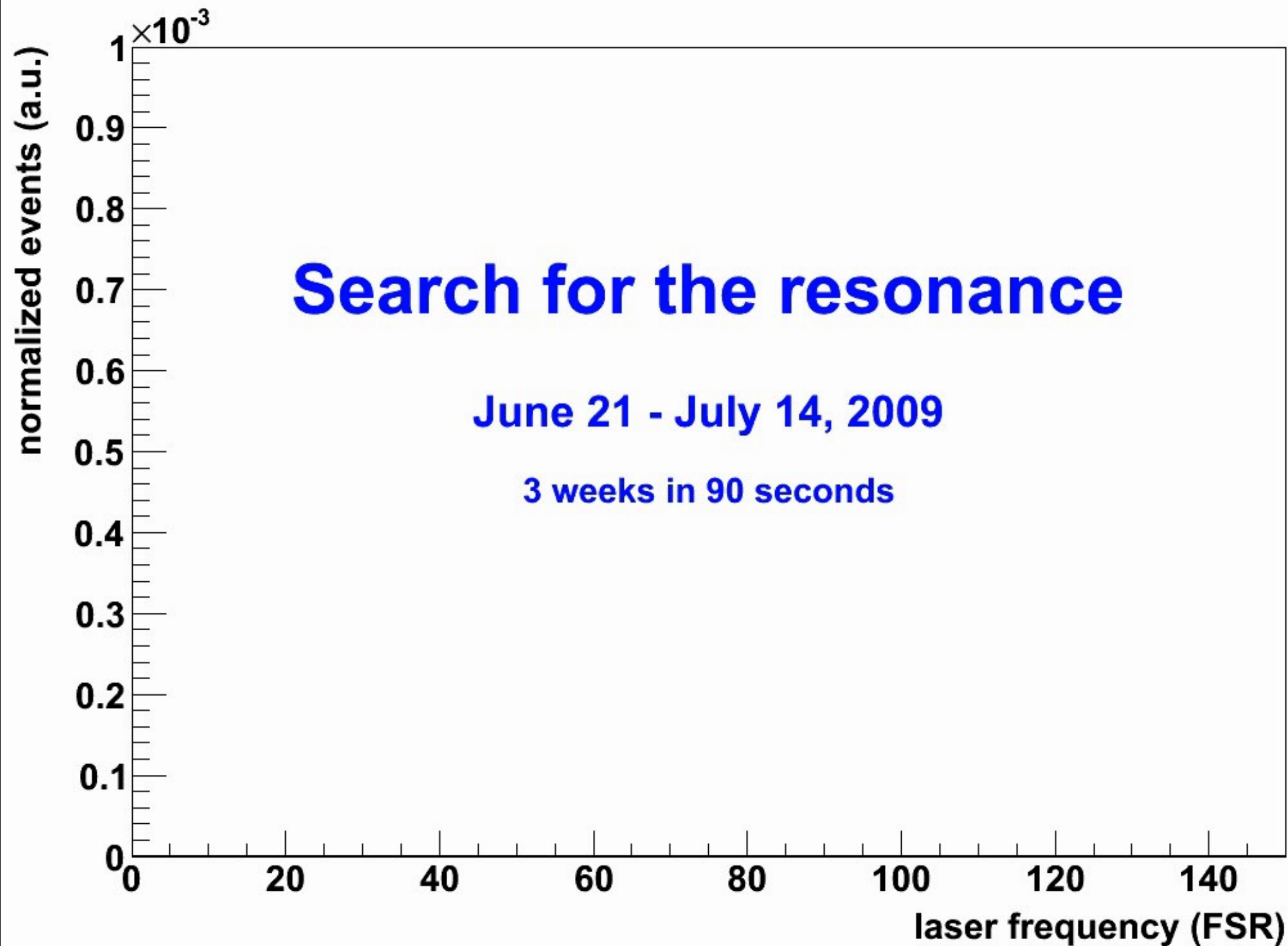


Run 2009

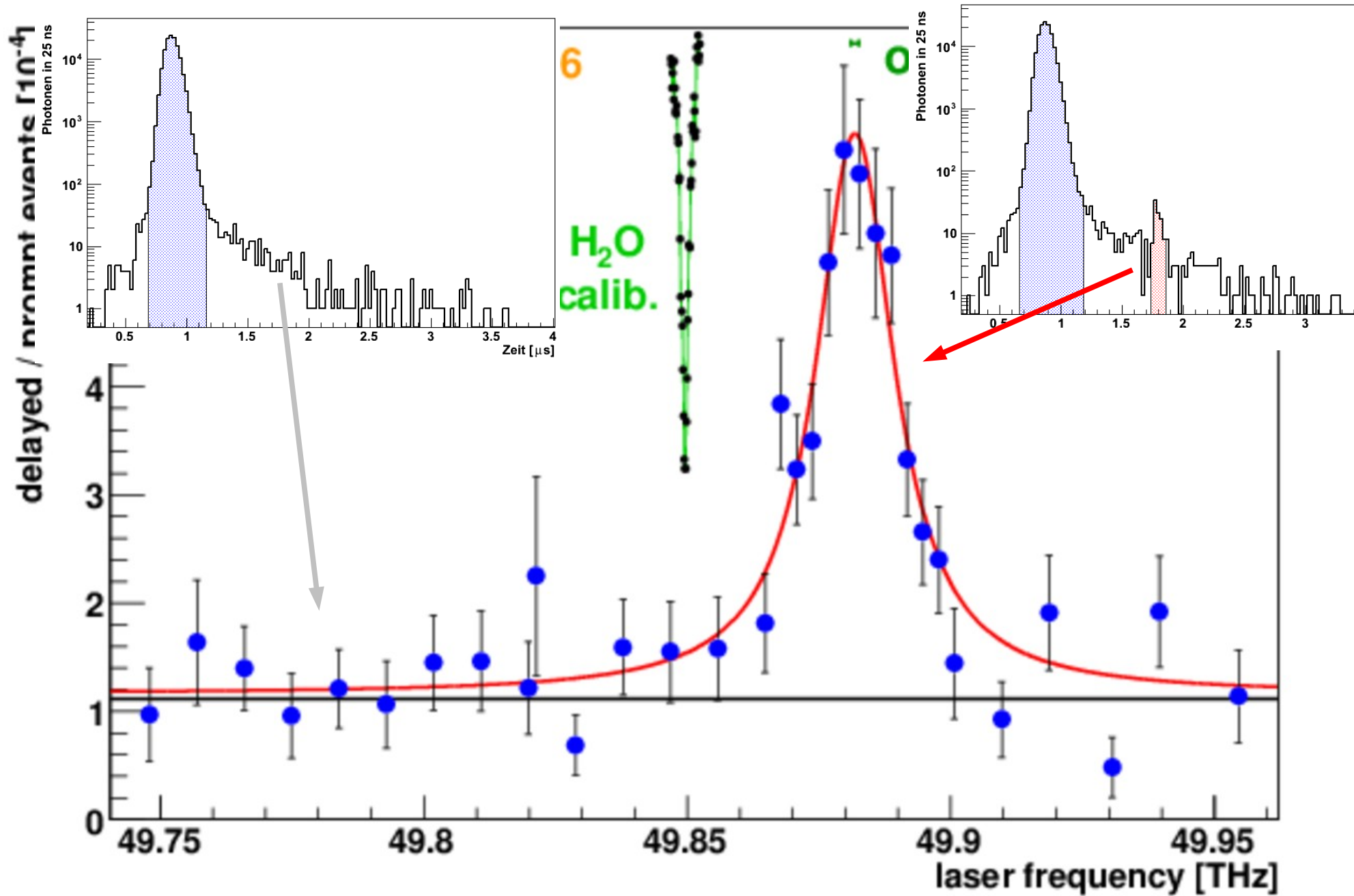


Fertig aufgebaut





Die Resonanzlinie



Yeah!



Auf die Resonanz!



Die Resonanz auf die Linie

8 July 2010 | www.nature.com/nature \$10

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nature

OIL SPILLS

**There's more
to come**

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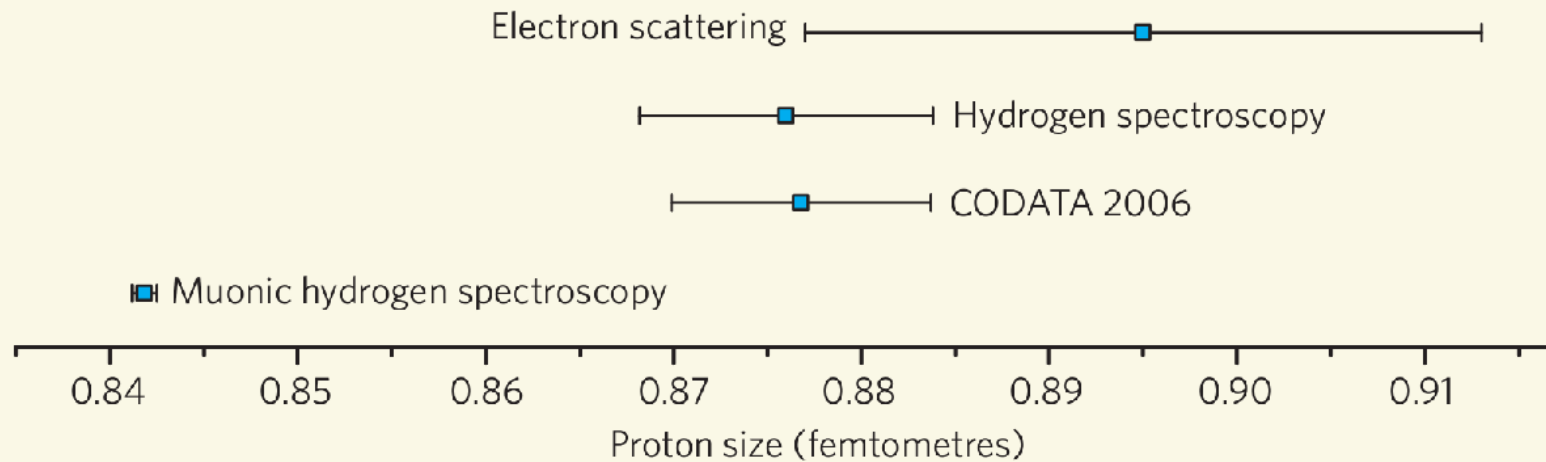
NATURE JOBS
Researchers for hire



Das Proton ist 4% kleiner als gedacht!

0.84184 ± 0.00067 fm anstatt

0.8768 ± 0.0069 fm



Die Resonanz auf die Linie

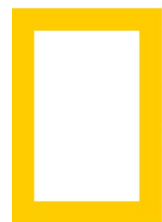


DRS 1

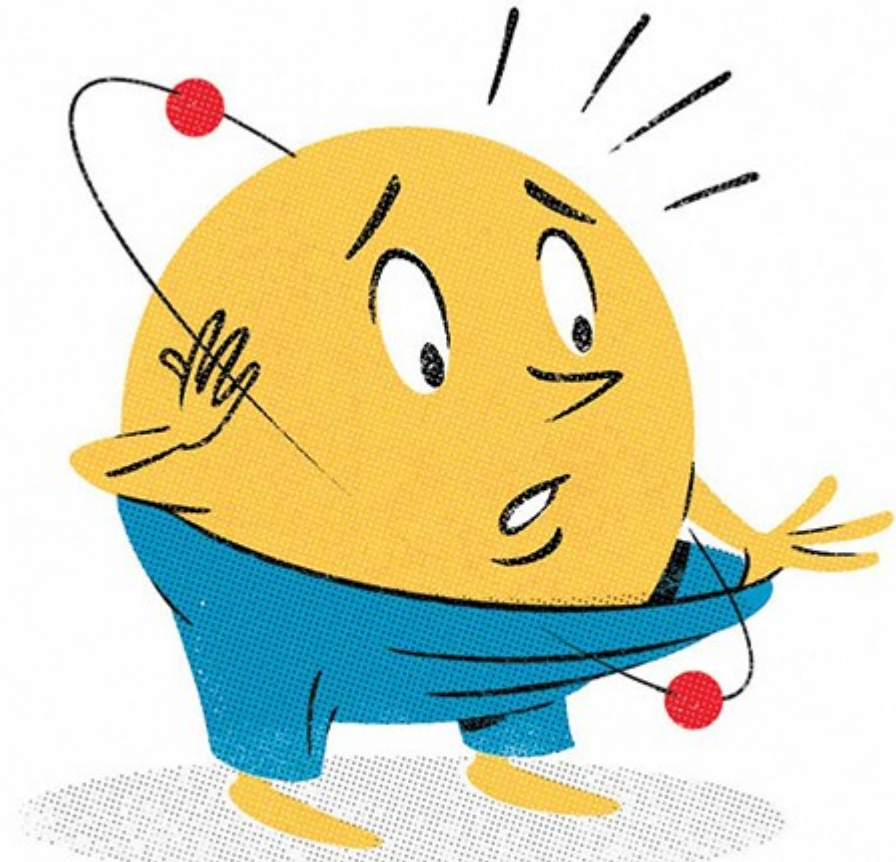
SPIEGEL

DIE 

la Repubblica



**NATIONAL
GEOGRAPHIC**

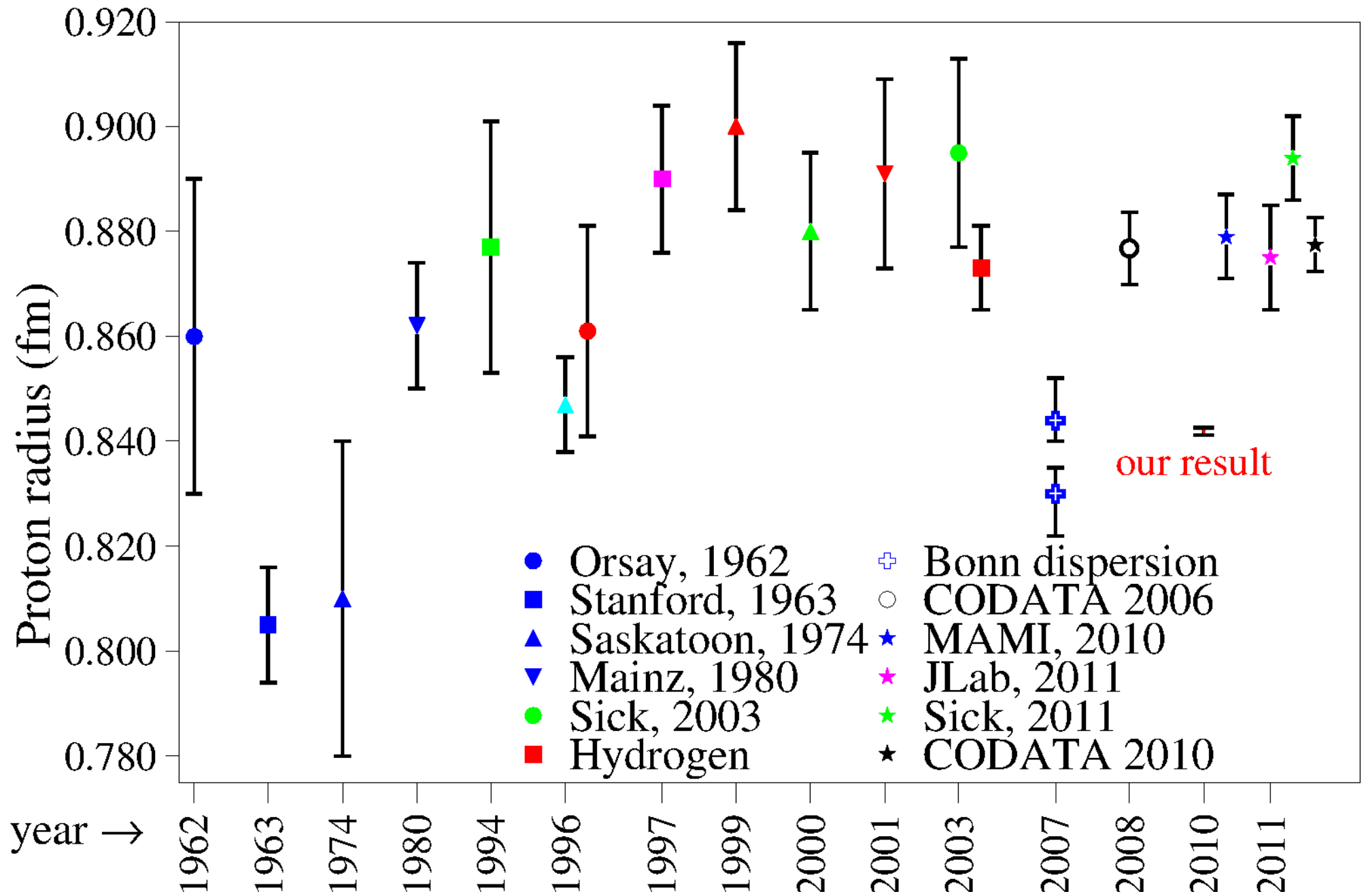


The New York Times

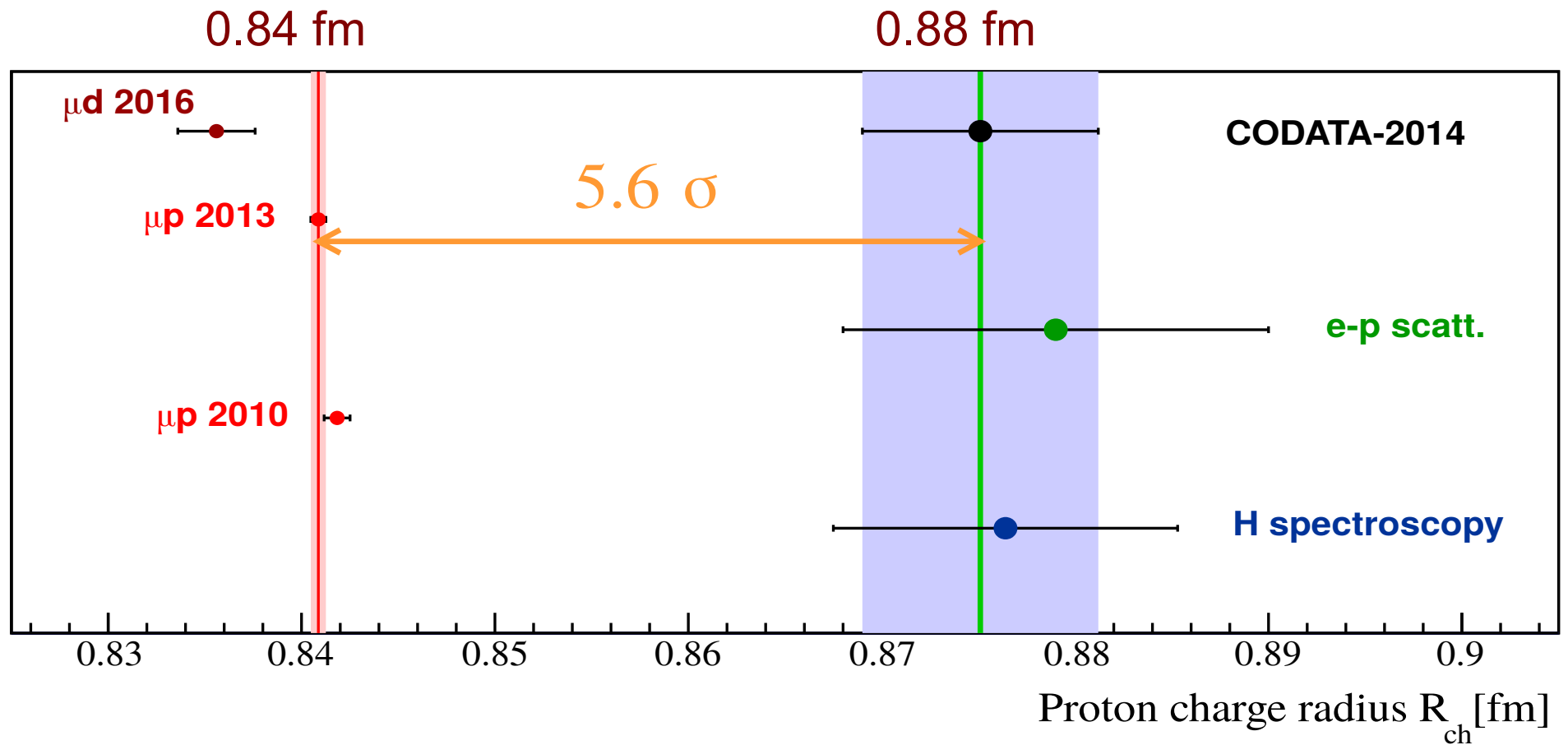
Los Angeles Times

Movie: In the News

Das "Proton Radius Puzzle"



Muonic Hydrogen



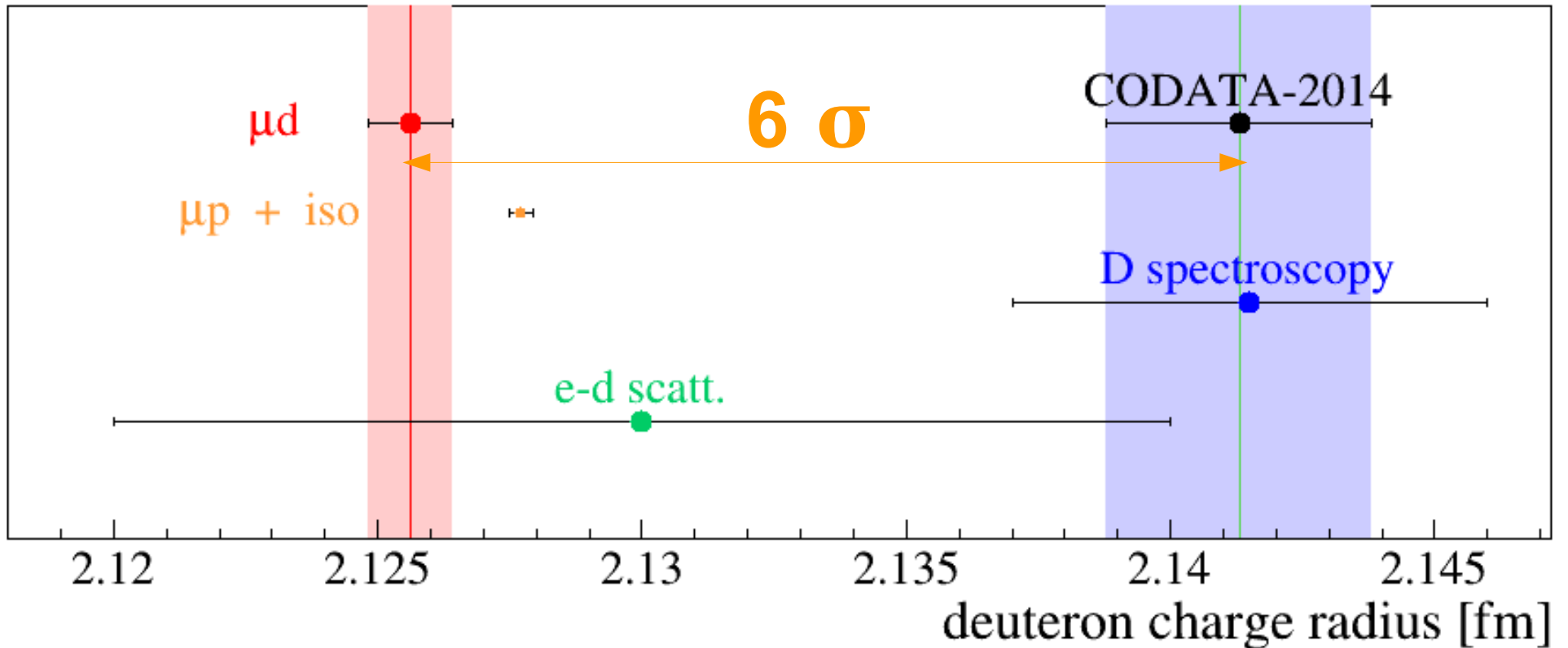
muonic hydrogen: 0.8409 ± 0.0004 fm

electronic hydrogen: 0.876 ± 0.008 fm

electron scattering 0.879 ± 0.011 fm

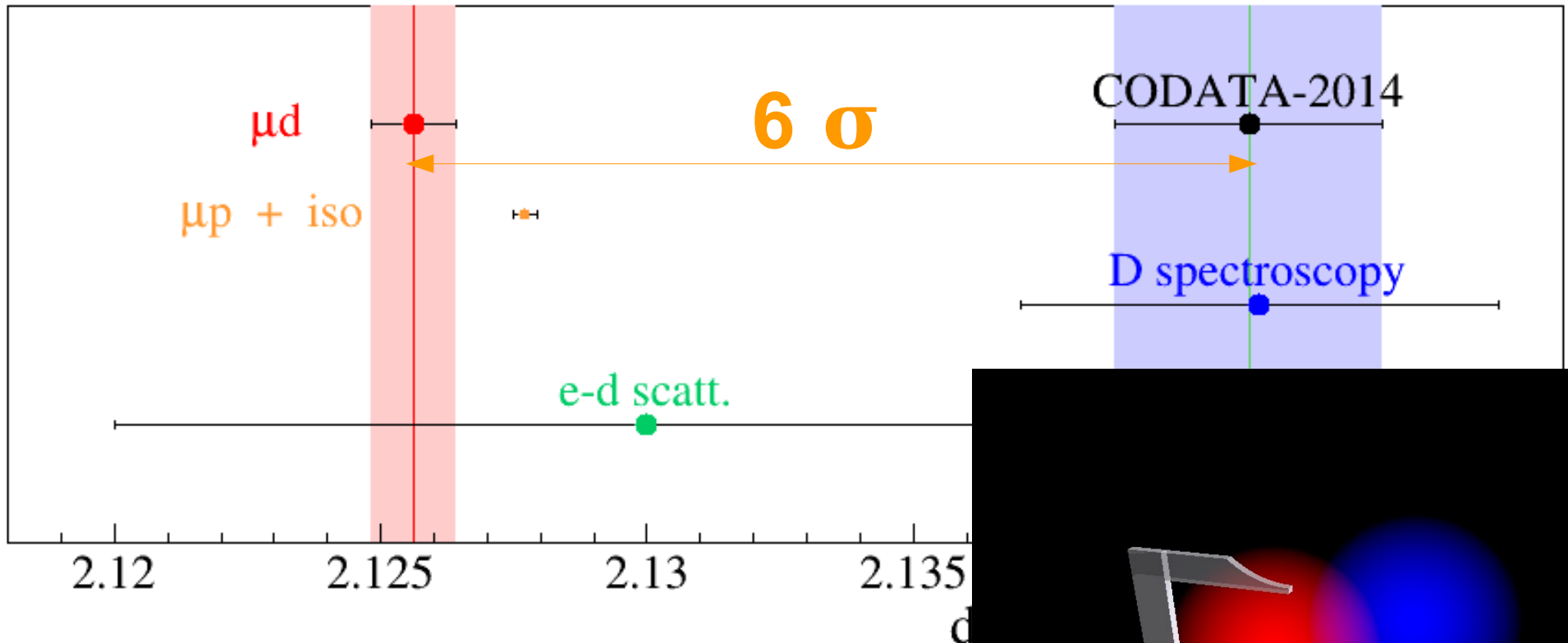
20x more accurate

Muonic Deuterium



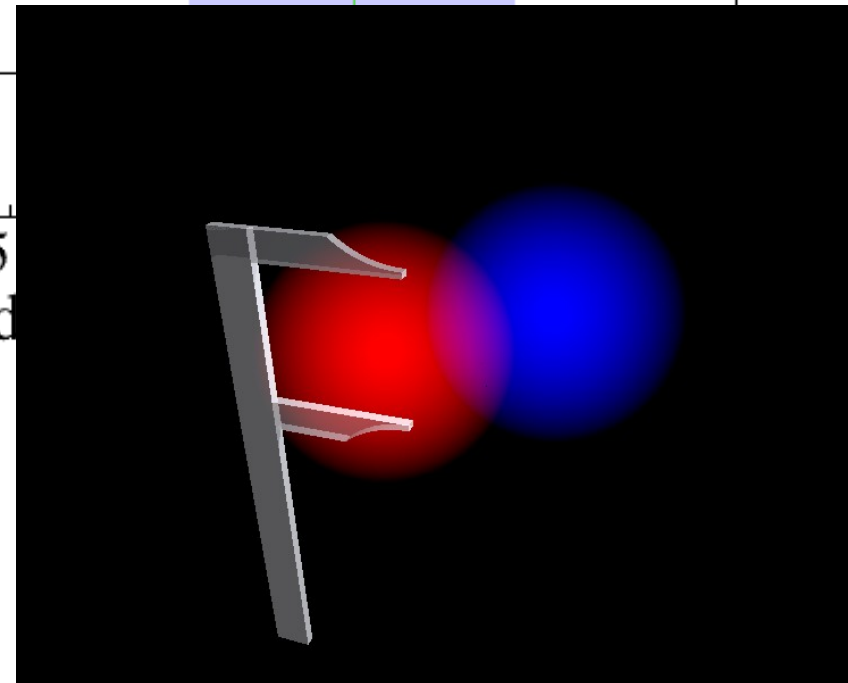
μD : 2.12562 (13)_{exp} (77)_{theo} fm (nucl. polarizability)
 $\mu H + H/D(1S-2S)$: 2.12771 (22) fm
 CODATA-2014: 2.14130 (250) fm

Deuteron radius

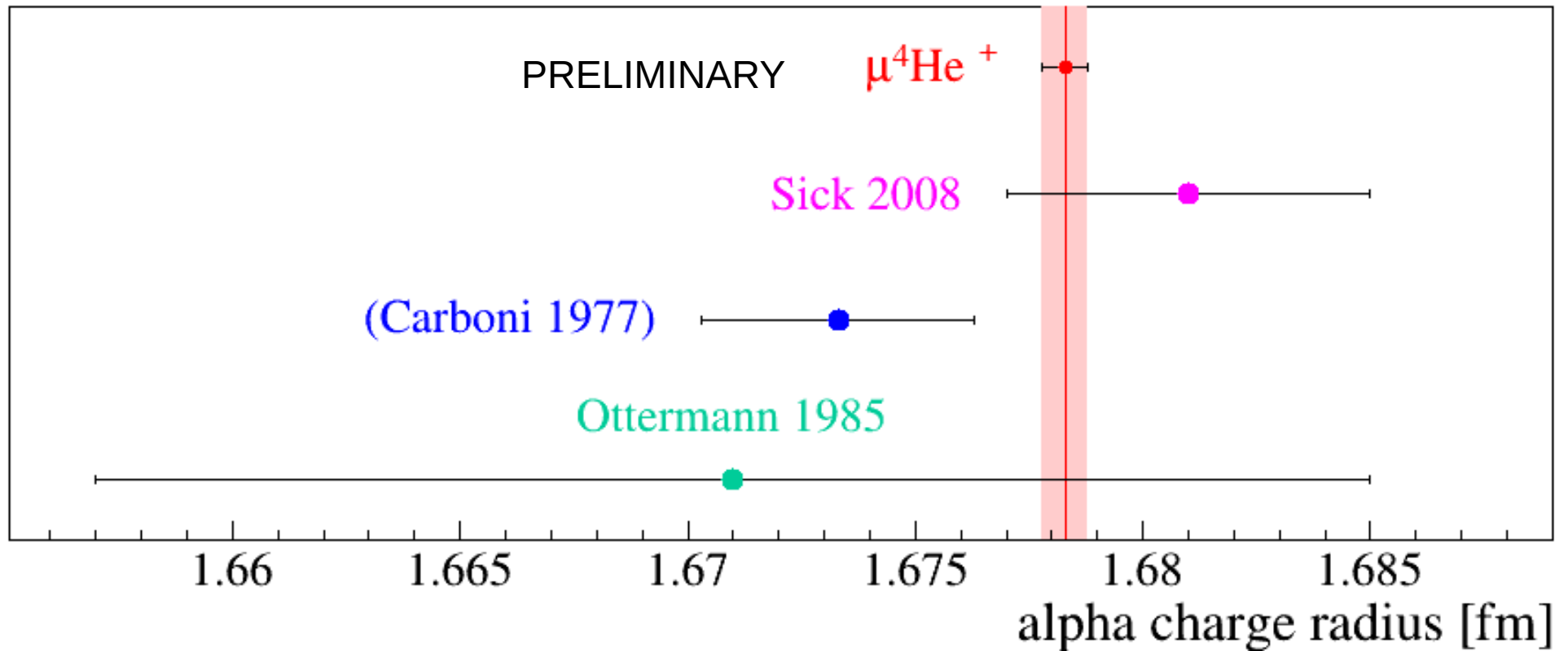


Deuteron is CONSISTENTLY smaller!

$$R_d^2 = R_{struct}^2 + R_p^2 + R_n^2 (+ DF)$$



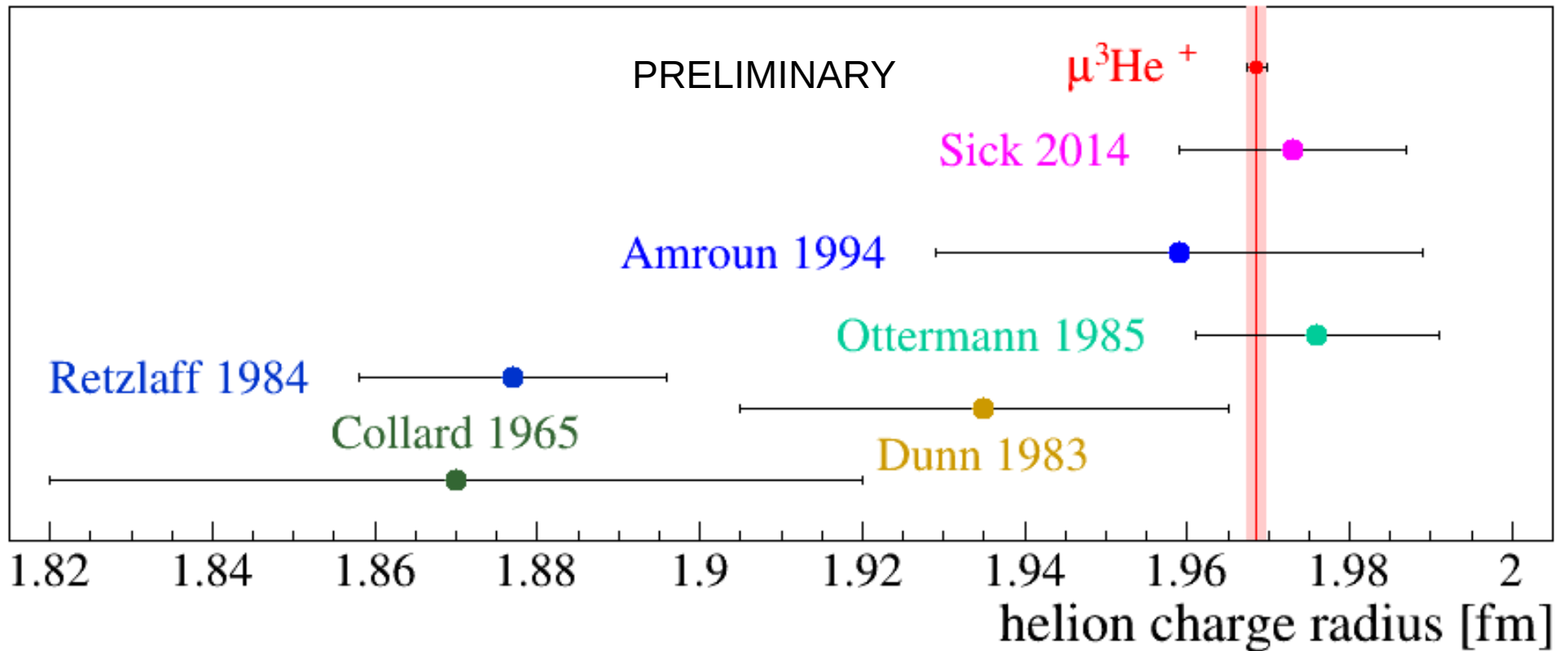
Muonic Helium-4



prel. accuracy: exp ± 0.00019 fm, theo ± 0.00058 fm (nucl. polarizability)

Theory: see Diepold et al. arxiv 1606.05231

Muonic Helium-3



prel. accuracy: exp ± 0.00012 fm, theo ± 0.00128 fm (nucl. polarizability)

Theory: see Franke et al. EPJ D 71, 341 (2017) [1705.00352]

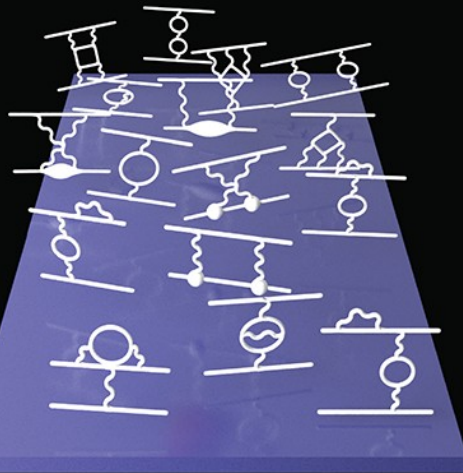
EPJ D

 Recognized by European Physical Society

Atomic, Molecular,
Optical and Plasma
Physics



From:
Theory of the $n = 2$ levels
in muonic helium-3 ions
by B. Franke et al.

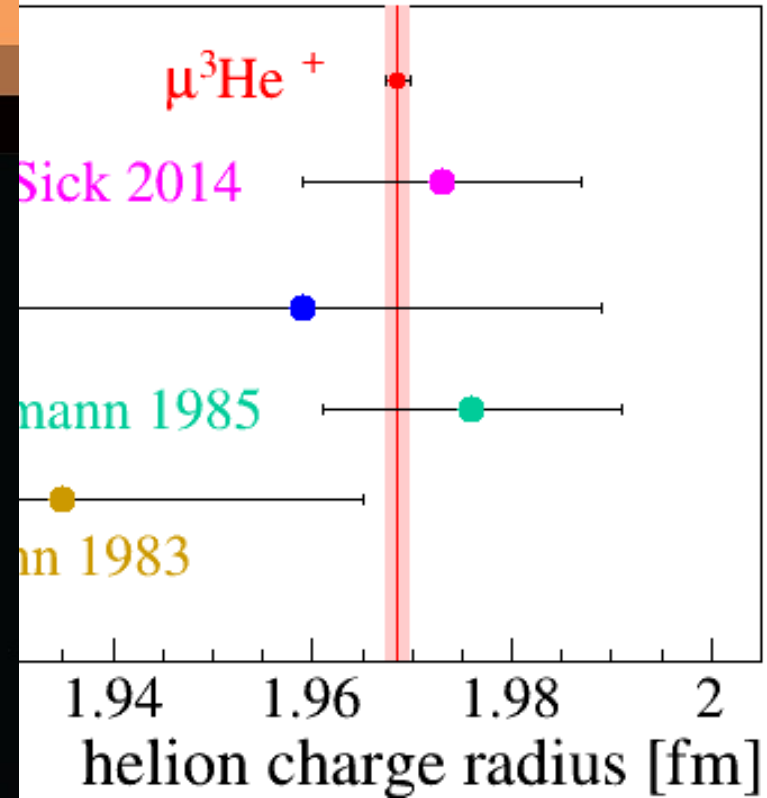





Società Italiana
di Fisica



um-3



0.00128 fm (nucl. polarizability)

prel.

Theory: see Franke et al. EPJ D 71, 341 (2017) [1705.00352]

Muonic conclusions

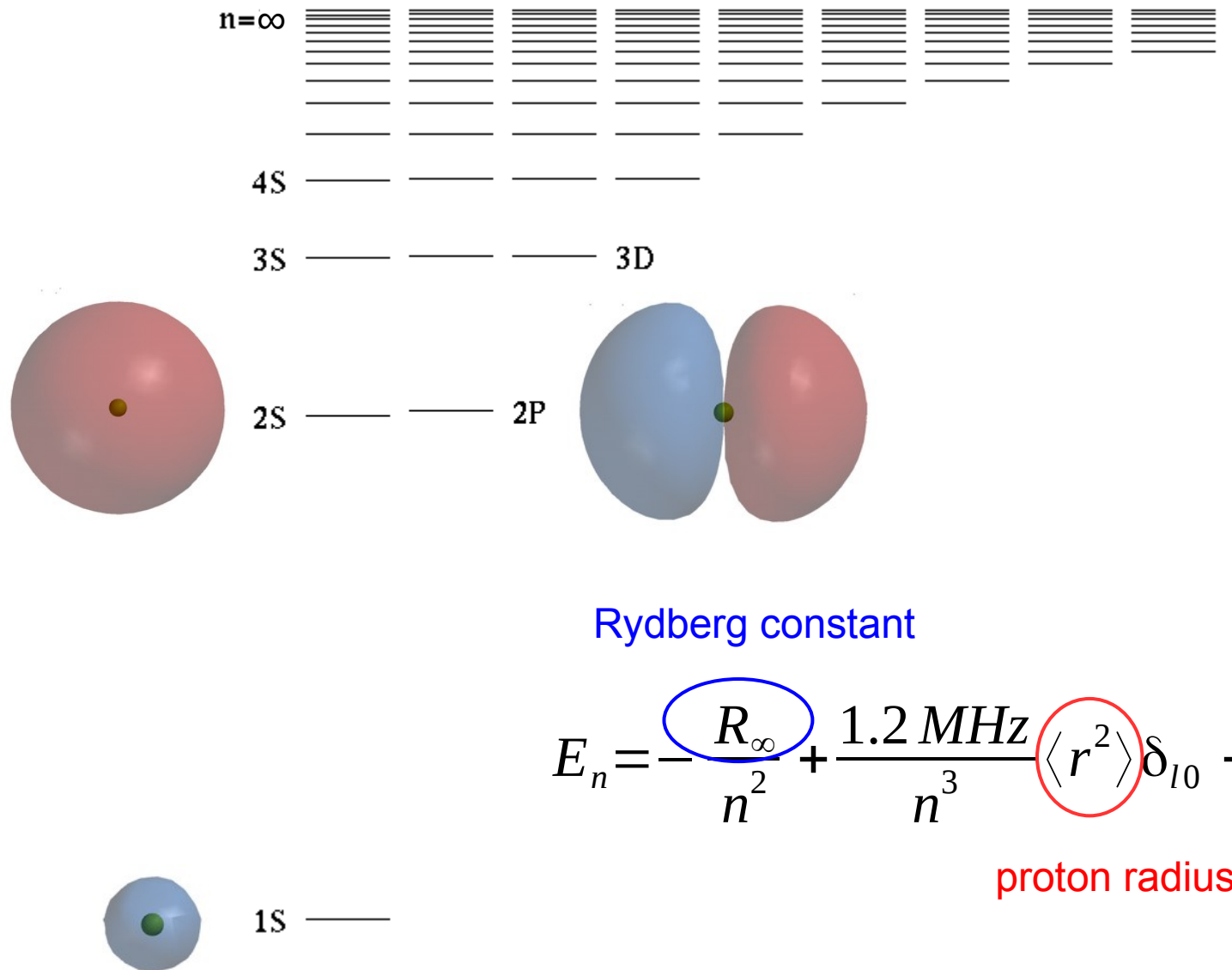
- The **proton** radius is $0.84087 (26)_{\text{exp}} (29)_{\text{theo}}$ fm
- The **deuteron** radius is $2.12771 (22)$ fm
- both are $>5\sigma$ smaller than CODATA values
- No discrepancy for **helion** and **alpha** particle

Part 2: The Rydberg constant

$$R_{\infty} = \frac{\alpha^2 m_e c}{2h}$$

- **most accurately determined** fundamental constant $u_r = 5.9 * 10^{-12}$
- corner stone of the CODATA LSA of fundamental constants
links **fine structure constant α** , **electron mass m_e** , **velocity of light c**
and **Planck's constant h**
- correlation coefficient with **proton radius**: 0.9891
→ The “proton radius puzzle” could be a “Rydberg puzzle”
- R_{∞} is a “unit converter”: atomic units → SI (Hertz)

Energy levels of hydrogen

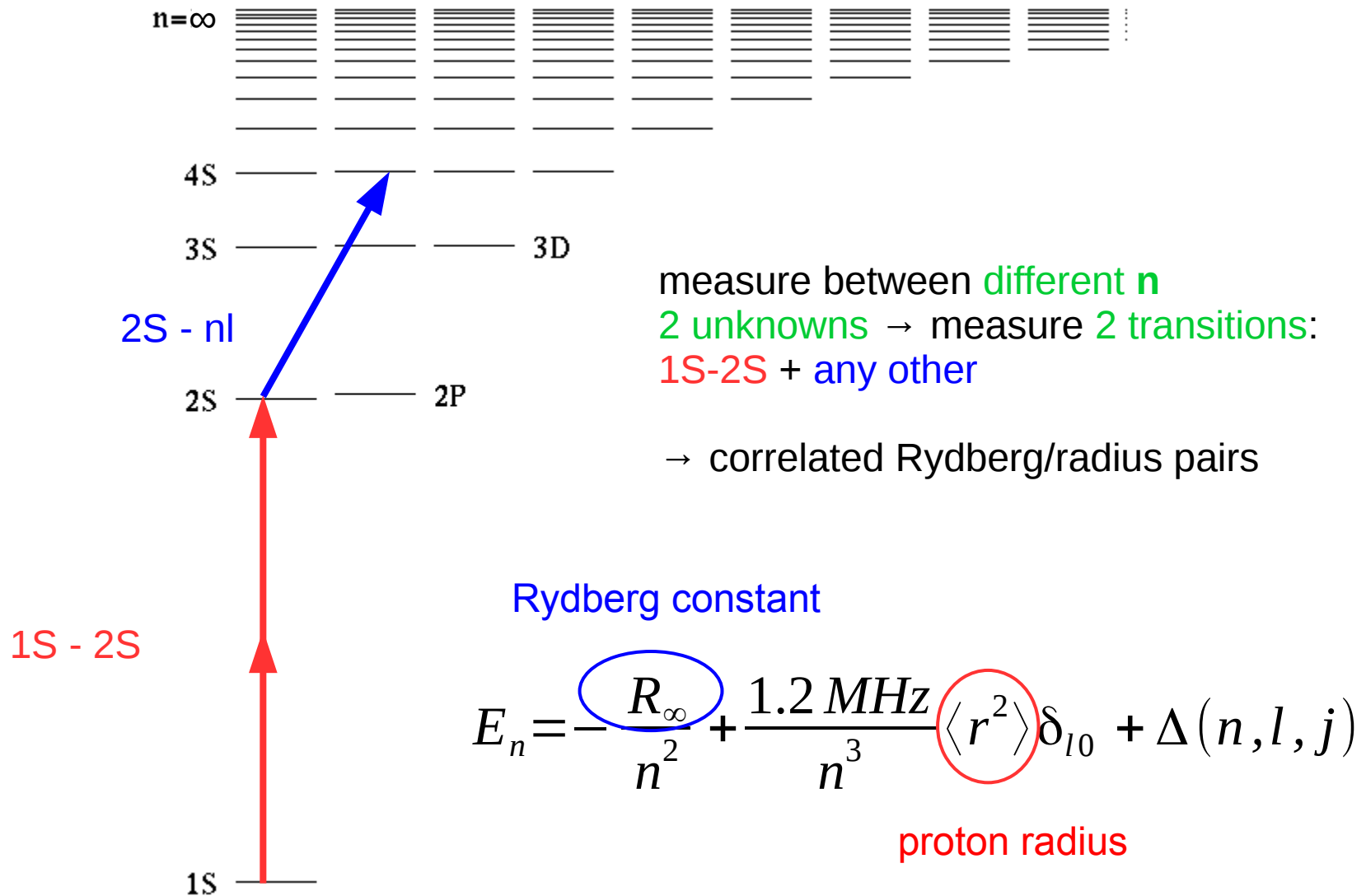


Rydberg constant

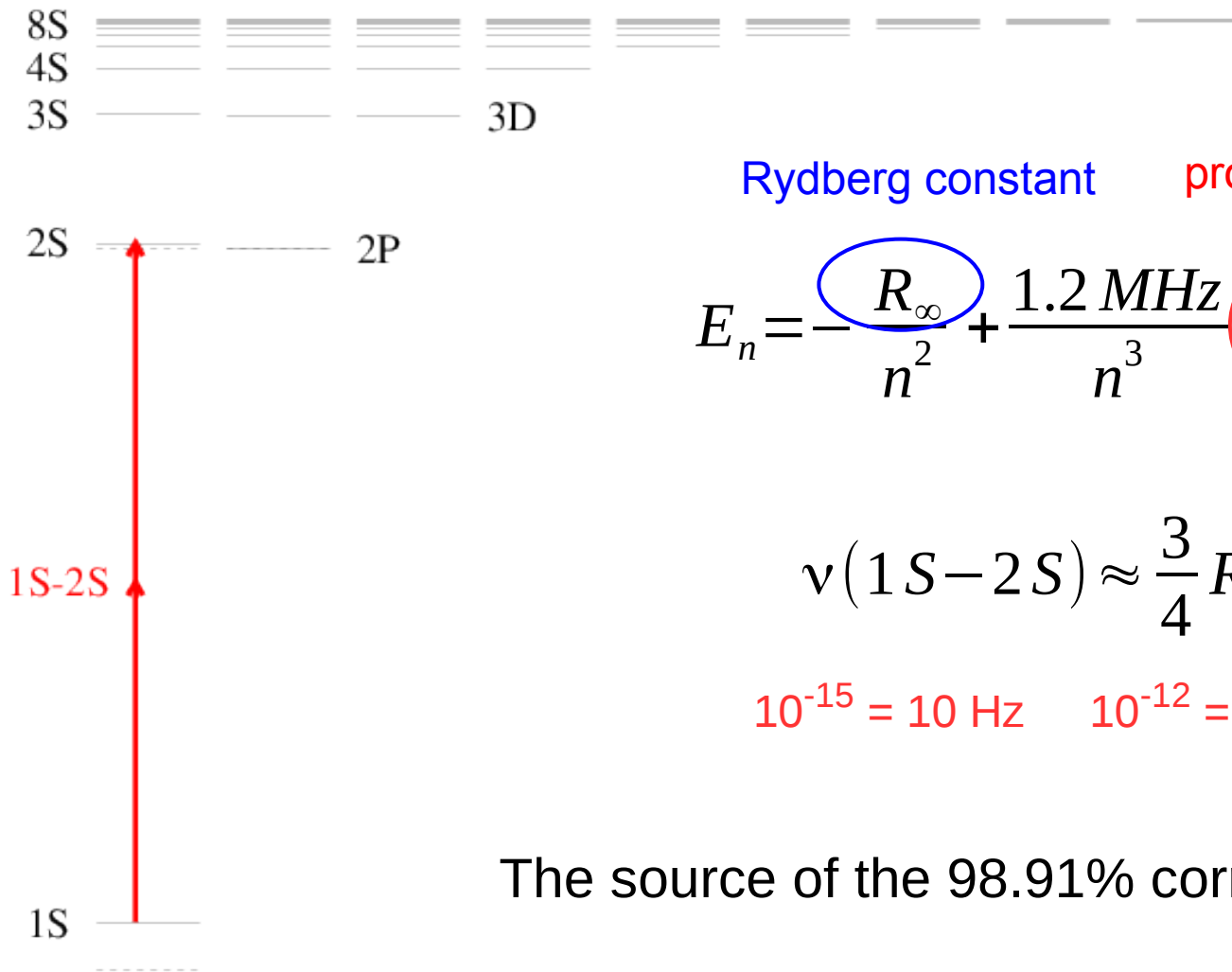
$$E_n = -\frac{R_\infty}{n^2} + \frac{1.2 \text{ MHz}}{n^3} \langle r^2 \rangle \delta_{l0} + \Delta(n, l, j)$$

proton radius

Energy levels of hydrogen



Correlation between R_∞ and R_p / R_d



Rydberg constant proton radius

$$E_n = -\frac{R_\infty}{n^2} + \frac{1.2 \text{ MHz}}{n^3} \langle r^2 \rangle \delta_{l0} + \Delta(n, l, j)$$

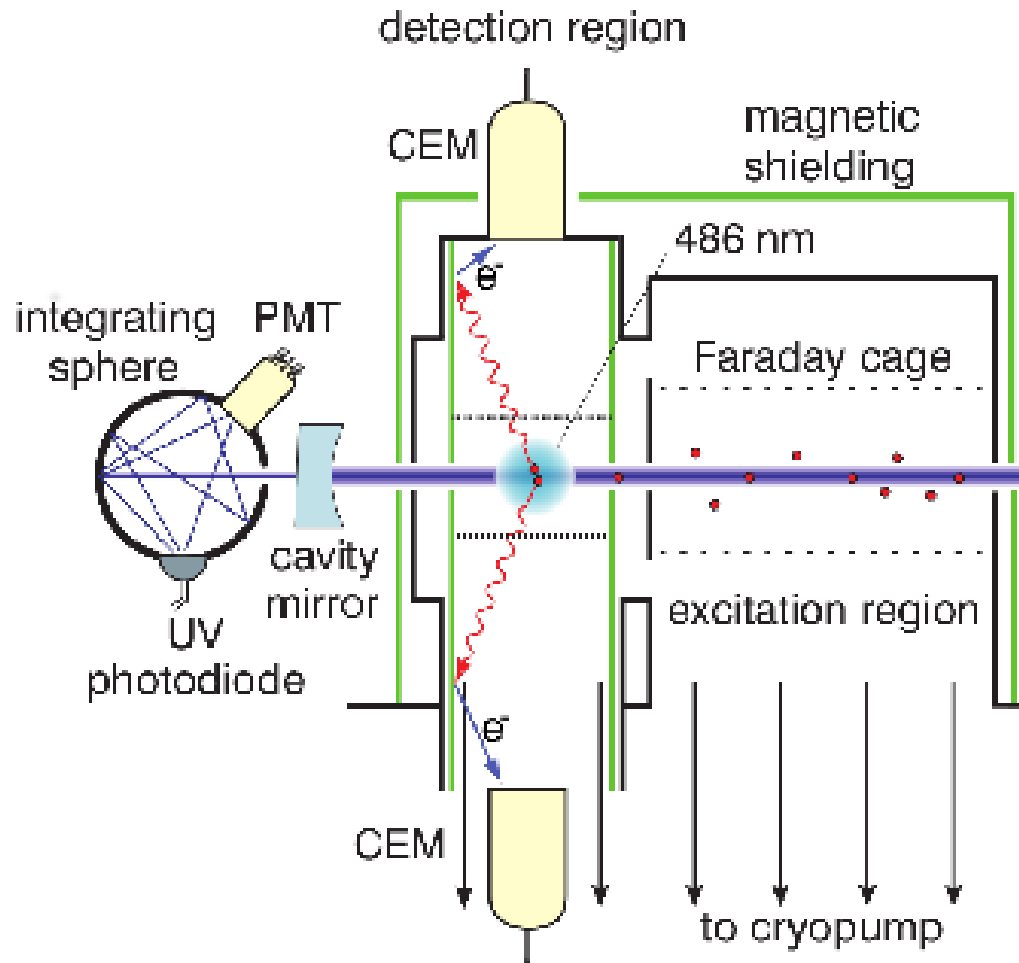
$$\nu(1S-2S) \approx \frac{3}{4} R_\infty - \frac{7}{8} E_{NS}$$

$$10^{-15} = 10 \text{ Hz} \quad 10^{-12} = 20 \text{ kHz}$$

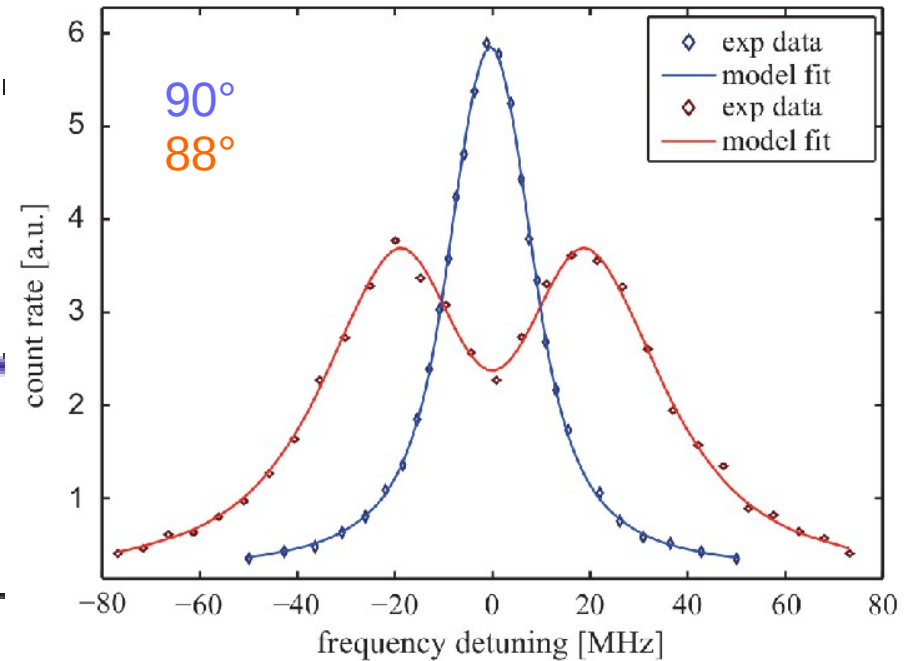
The source of the 98.91% correlation of R_∞ and R_p

1S-2S: Parthey, RP et al., PRL 107, 203001 (2011)

Garching H(2S-4P)

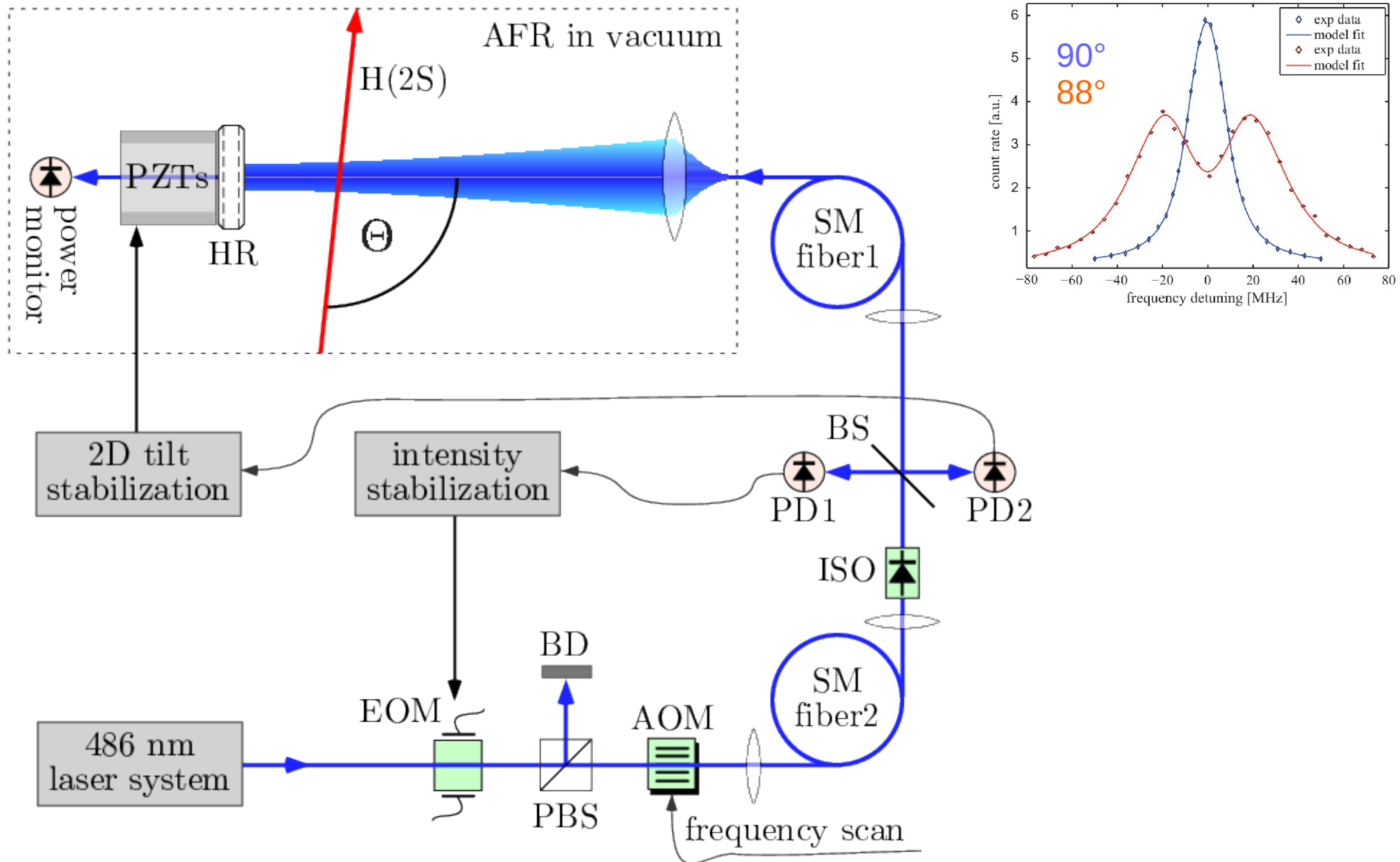


1st order Doppler cancellation



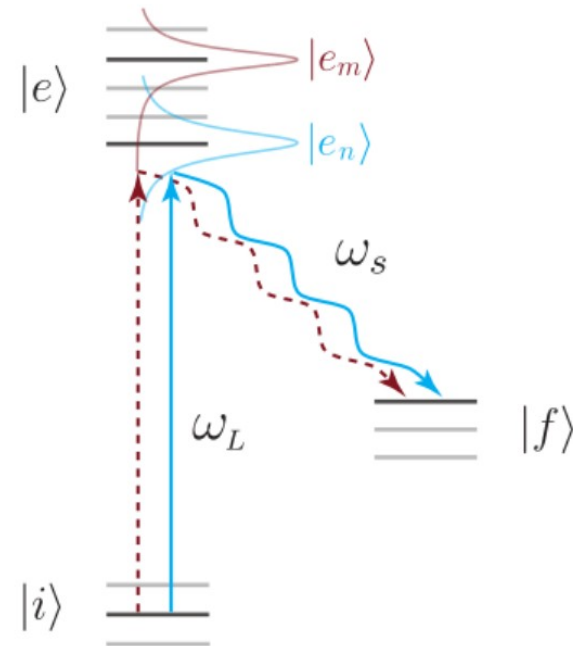
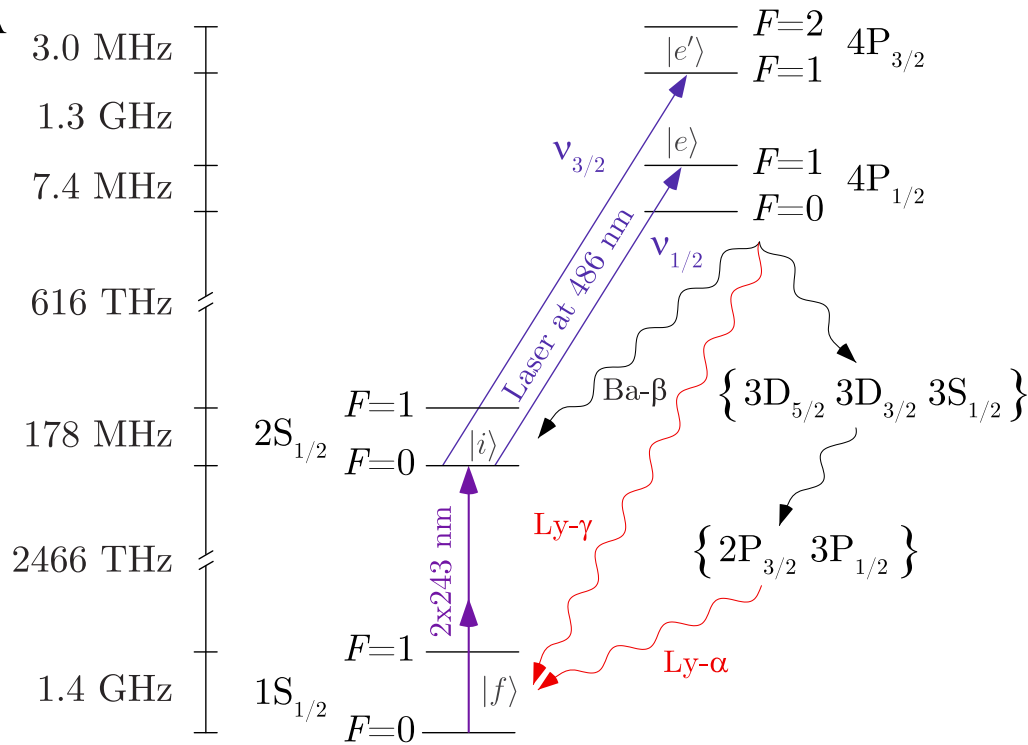
- cryogenic H beam (6 K)
- optical 1S-2S excitation (2S, F=0)
- 2S-4P transition is 1-photon: retroreflector
- split line to 10^{-4} !!!
- 2.3 kHz vs. 9 kHz PRP
- large systematics

1st order Doppler shift

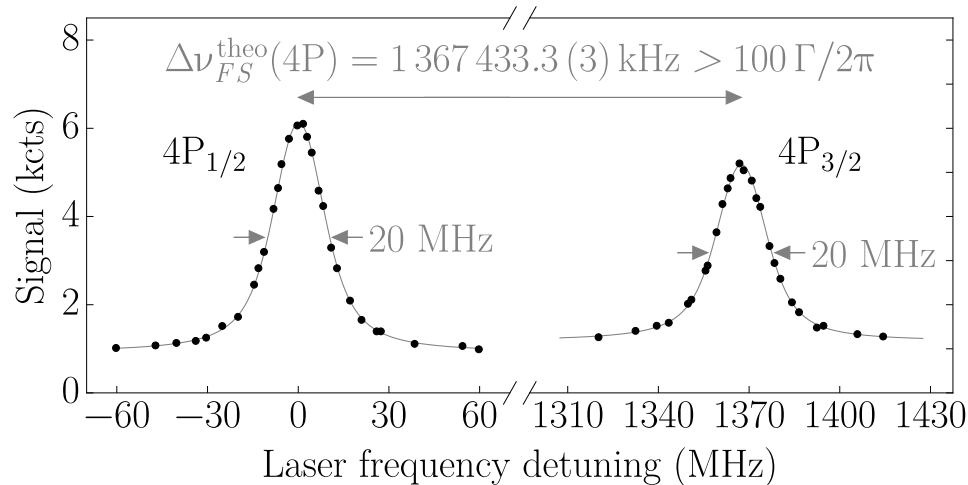


Quantum interference shifts

A



B



$$P(\omega) \propto \left| \frac{(\vec{d}_1 \vec{E}_0) \vec{d}_1}{\omega_1 - \omega_L + i\gamma_1/2} + \frac{(\vec{d}_2 \vec{E}_0) \vec{d}_2 e^{i\Delta\Phi}}{\omega_2 - \omega_L + i\gamma_2/2} \right|^2$$

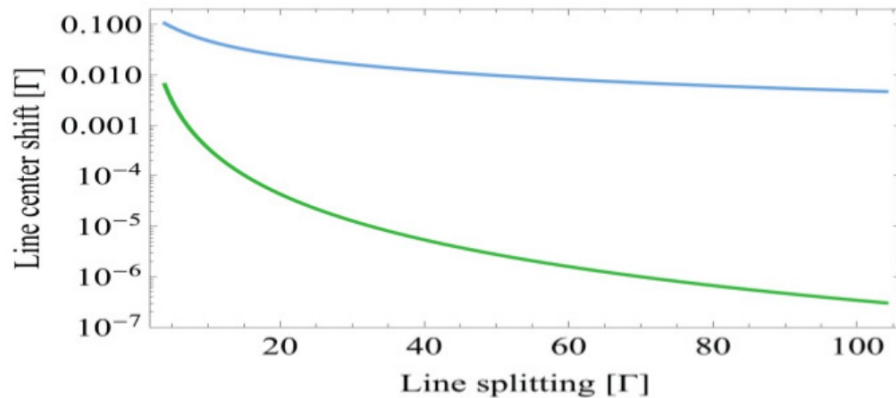
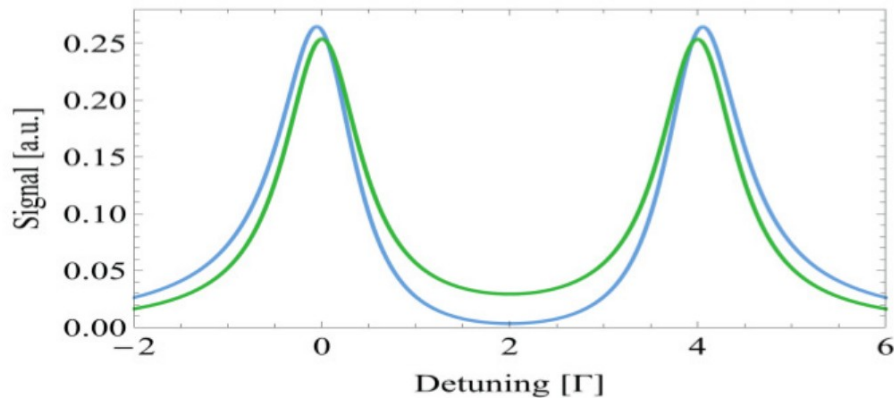
= Lorentzian(1) + Lorentzian(2)

+ cross-term (QI)

see

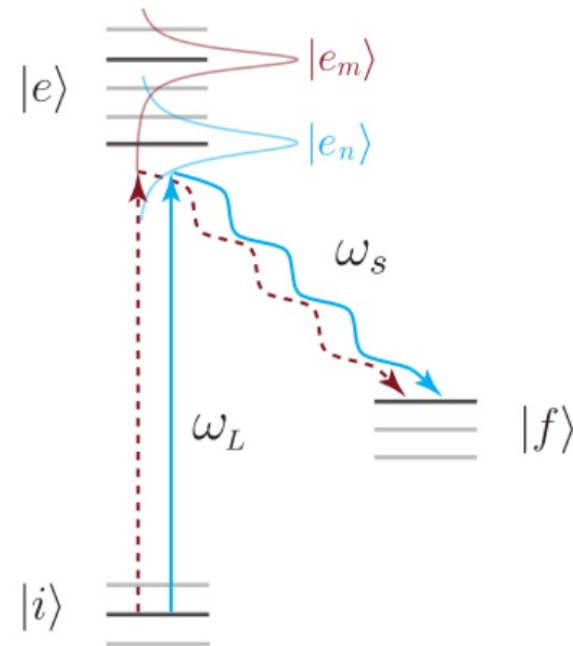
Horbatsch, Hessels, PRA 82, 052519 (2010); PRA 84, 032508 (2011); PRA 86 040501 (2012)
 Sansonetti et al., PRL 107, 021001 (2011)
 Brown et al., PRA 87, 032504 (2013)

Quantum interference shifts



Fitting this with 2 Lorentzians creates

line shifts



$$P(\omega) \propto \left| \frac{(\vec{d}_1 \vec{E}_0) \vec{d}_1}{\omega_1 - \omega_L + i\gamma_1/2} + \frac{(\vec{d}_2 \vec{E}_0) \vec{d}_2 e^{i\Delta\Phi}}{\omega_2 - \omega_L + i\gamma_2/2} \right|^2$$

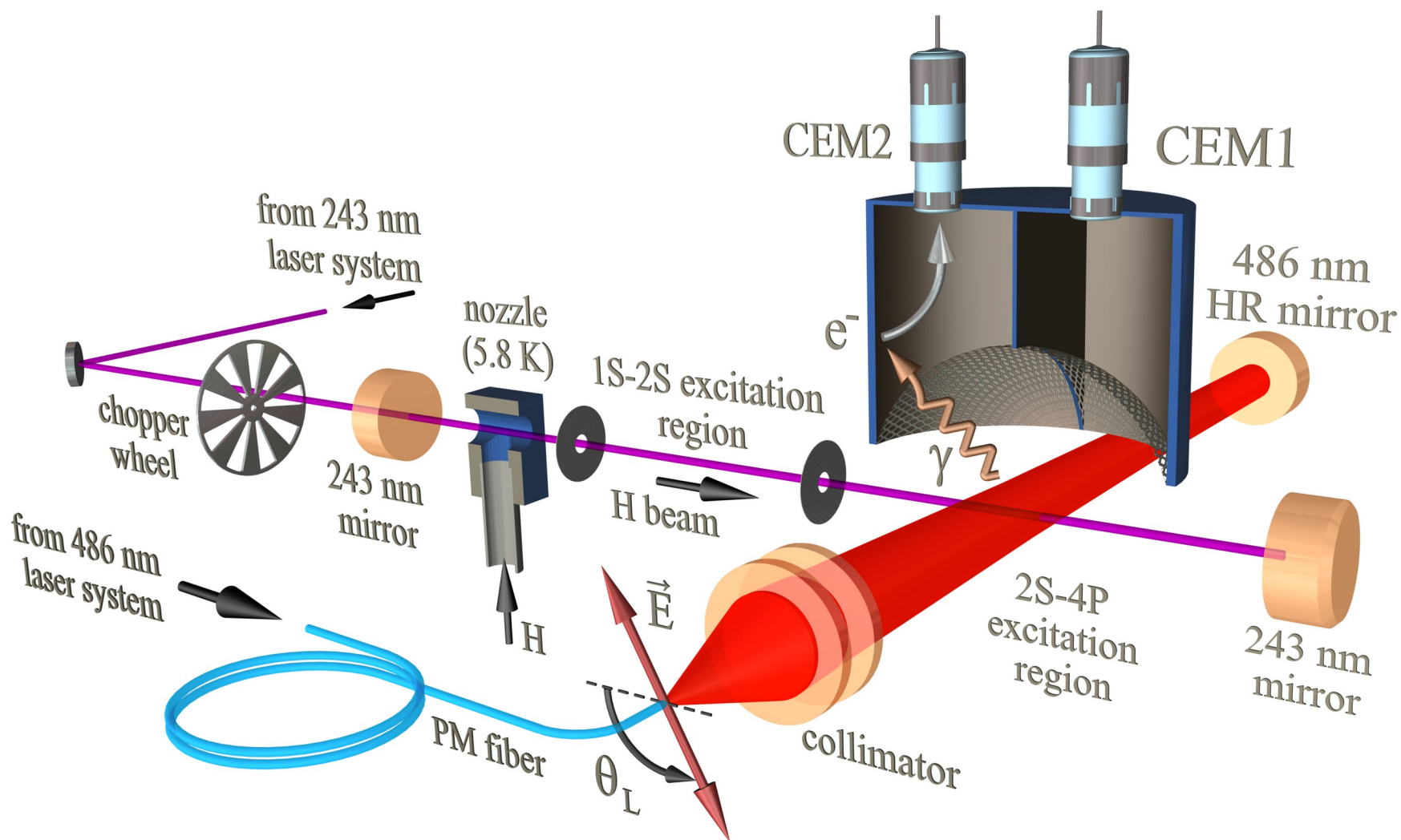
= Lorentzian(1) + Lorentzian(2)

+ cross-term (QI)

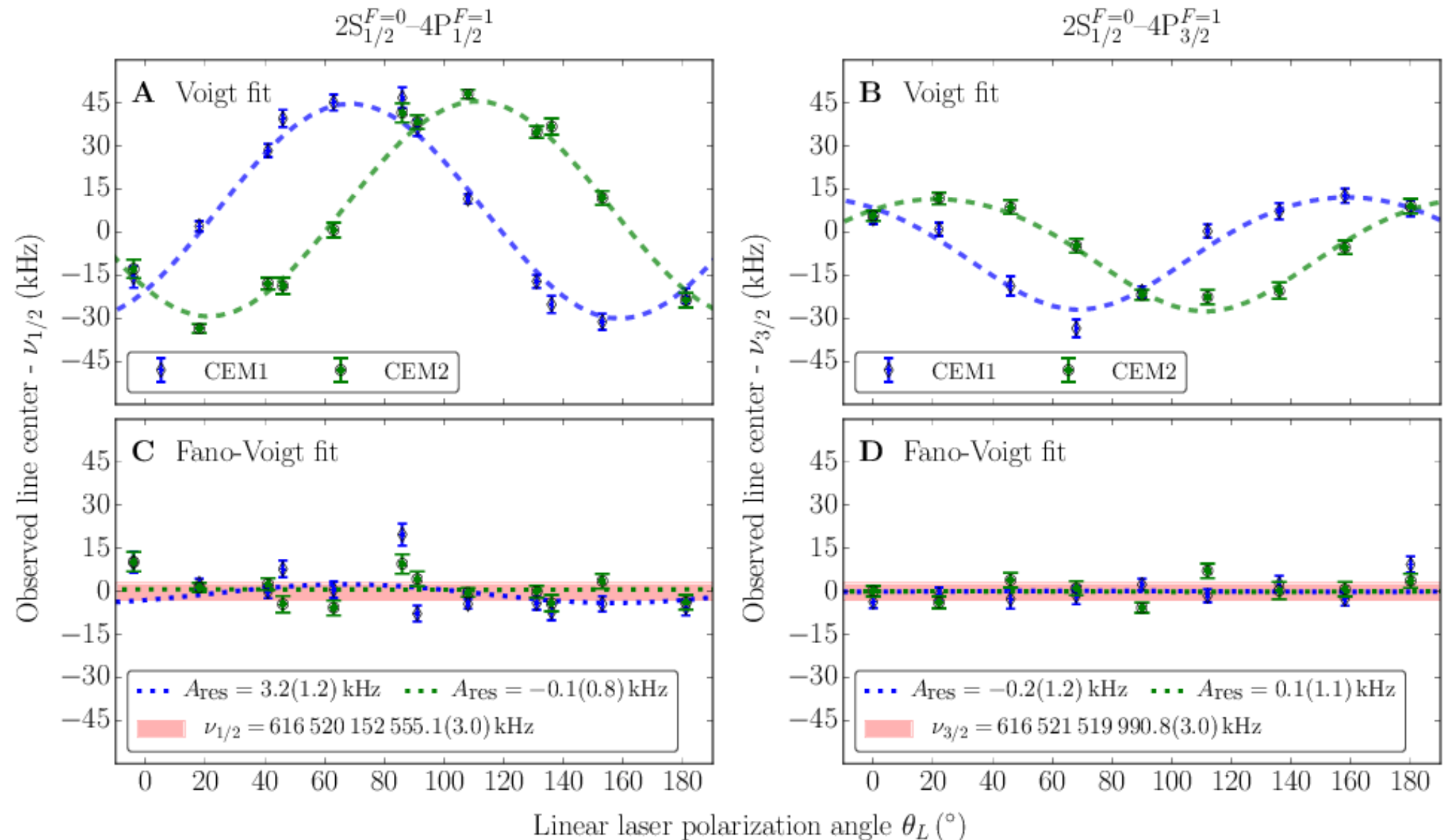
see

Horbatsch, Hessels, PRA 82, 052519 (2010); PRA 84, 032508 (2011); PRA 86 040501 (2012)
 Sansonetti et al., PRL 107, 021001 (2011)
 Brown et al., PRA 87, 032504 (2013)

Studying QI in 2S-4P



QI in hydrogen ($\Delta = 100 \Gamma$)



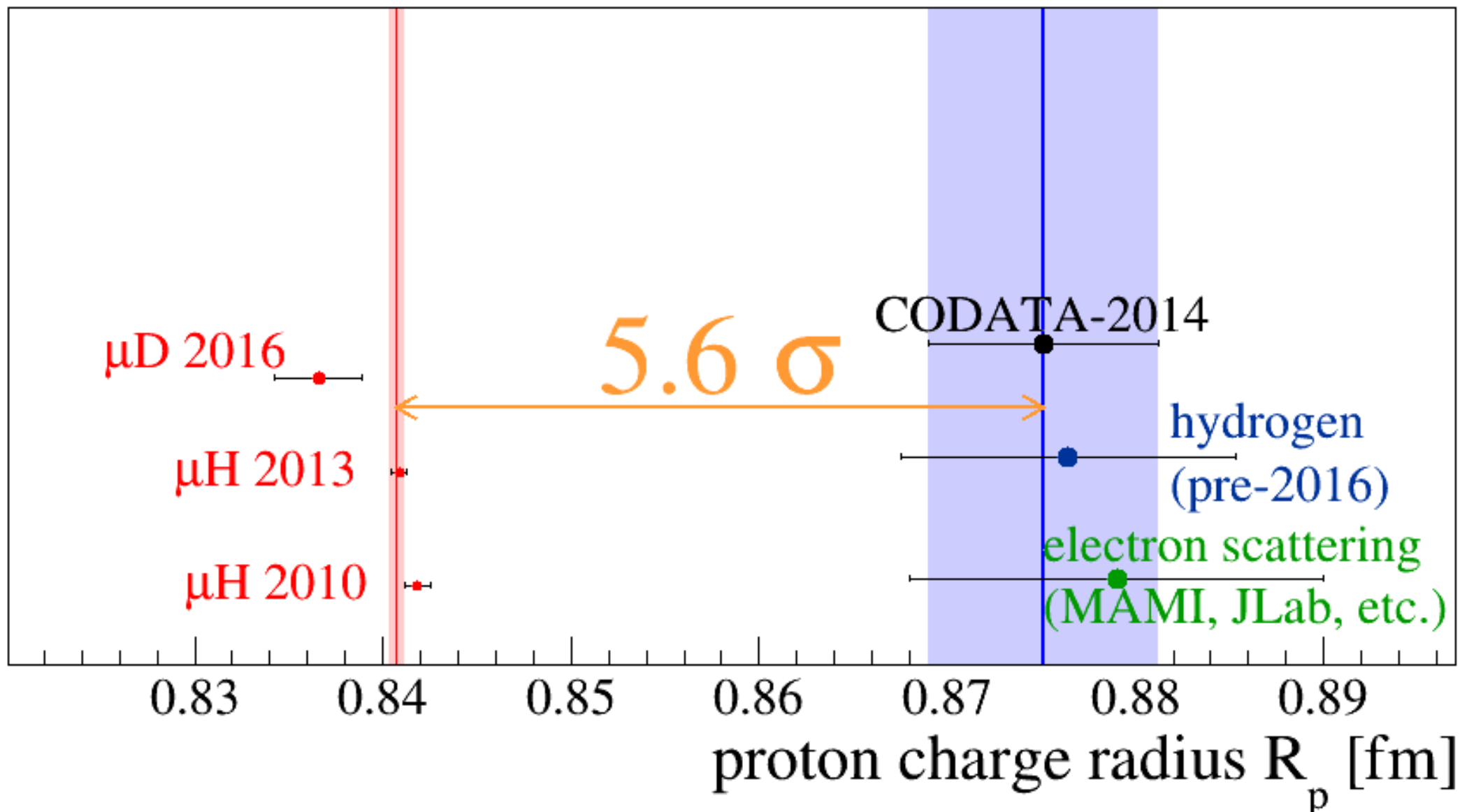
Systematics

Contribution	$\Delta\nu$ (kHz)	σ (kHz)
Statistics	0.00	0.41
First-order Doppler shift	0.00	2.13
Quantum interference shift	0.00	0.21
Light force shift	-0.32	0.30
Model corrections	0.11	0.06
Sampling bias	0.44	0.49
Second-order Doppler shift	0.22	0.05
dc-Stark shift	0.00	0.20
Zeeman shift	0.00	0.22
Pressure shift	0.00	0.02
Laser spectrum	0.00	0.10
Frequency standard (hydrogen maser)	0.00	0.06
Recoil shift	-837.23	0.00
Hyperfine structure corrections	-132,552.092	0.075
Total	-133,388.9	2.3

The “Proton Radius Puzzle”

Muons

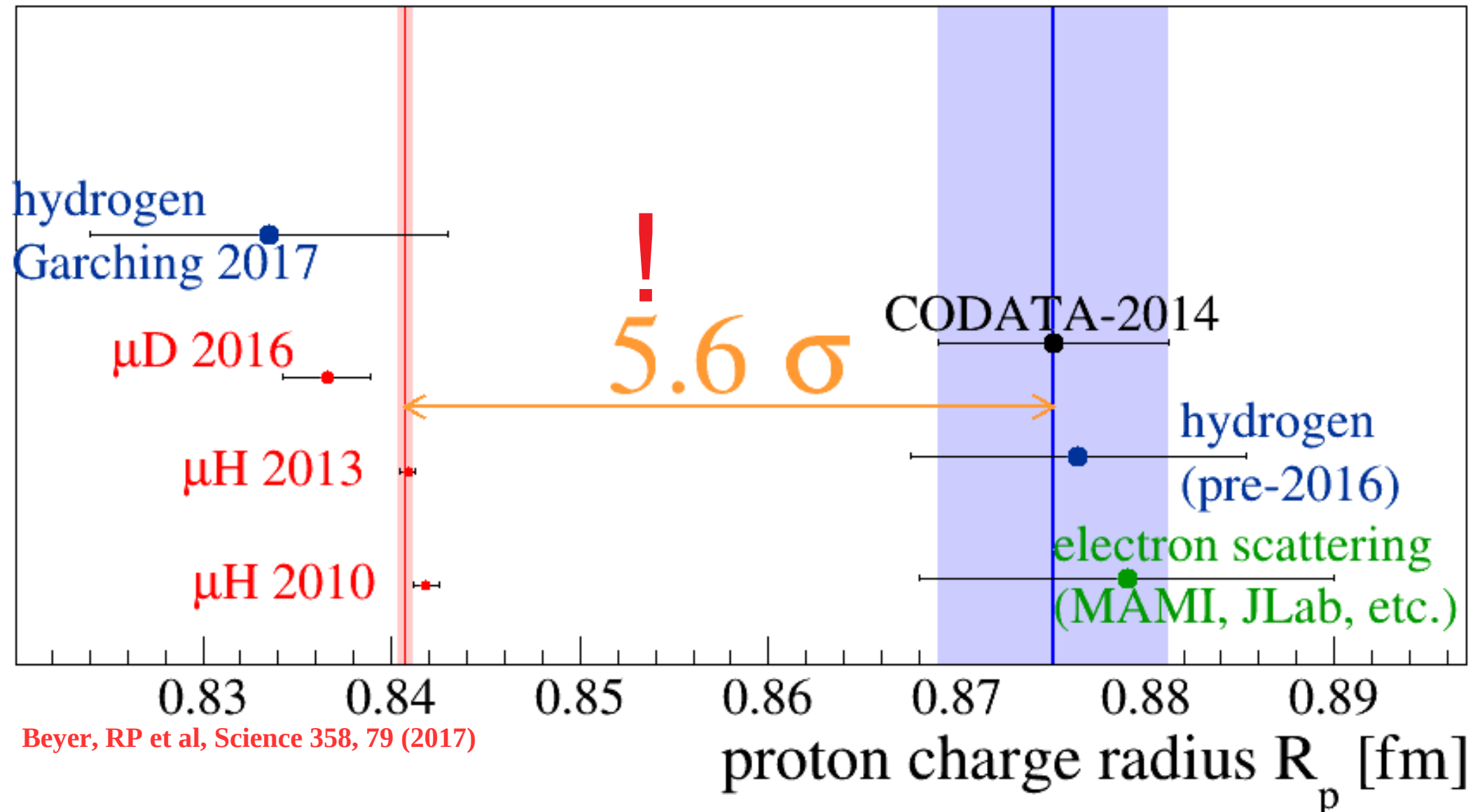
Electrons



New Measurements: Garching 2S-4P

Muons

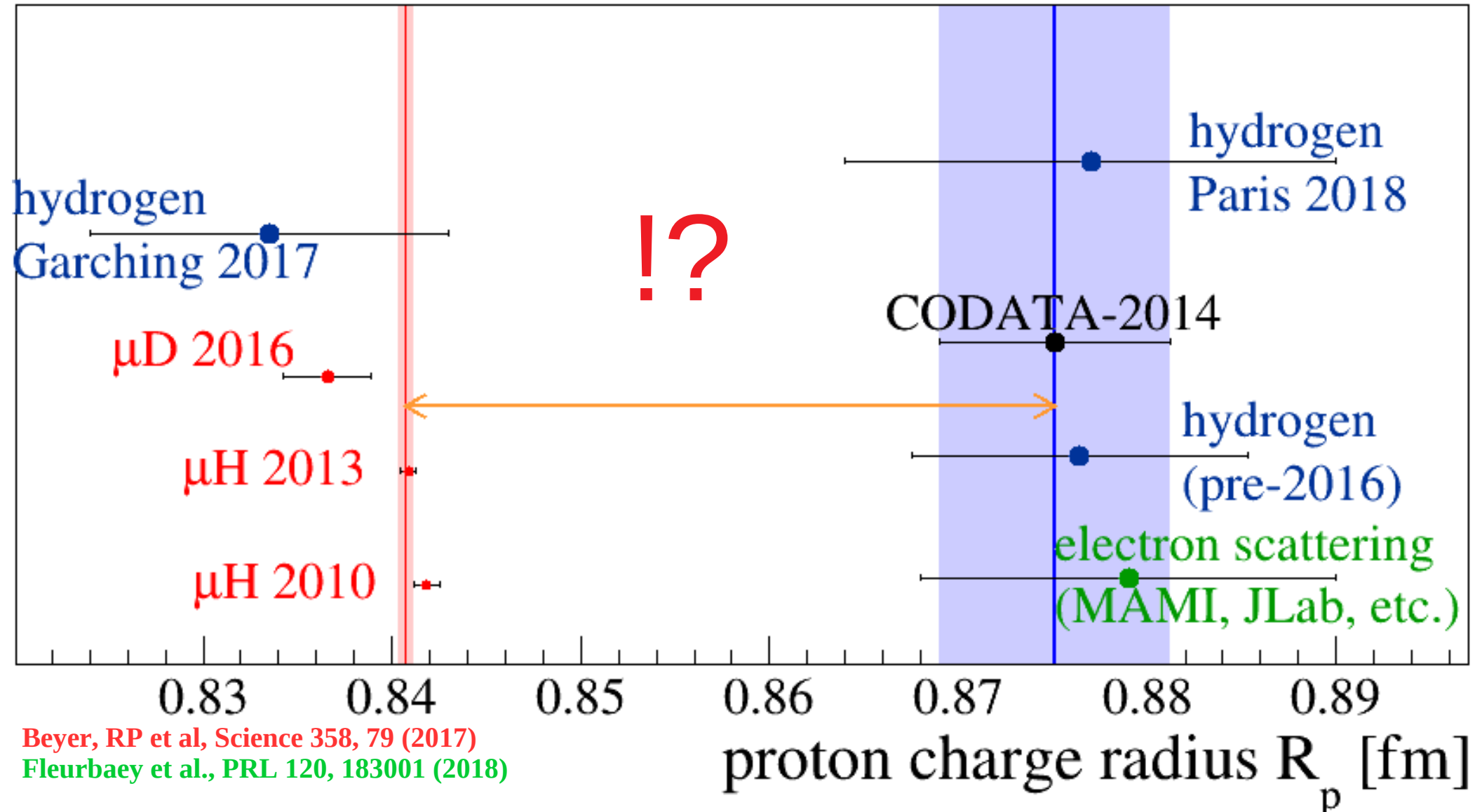
Electrons



New Measurements: Paris 1S-3S

Muons

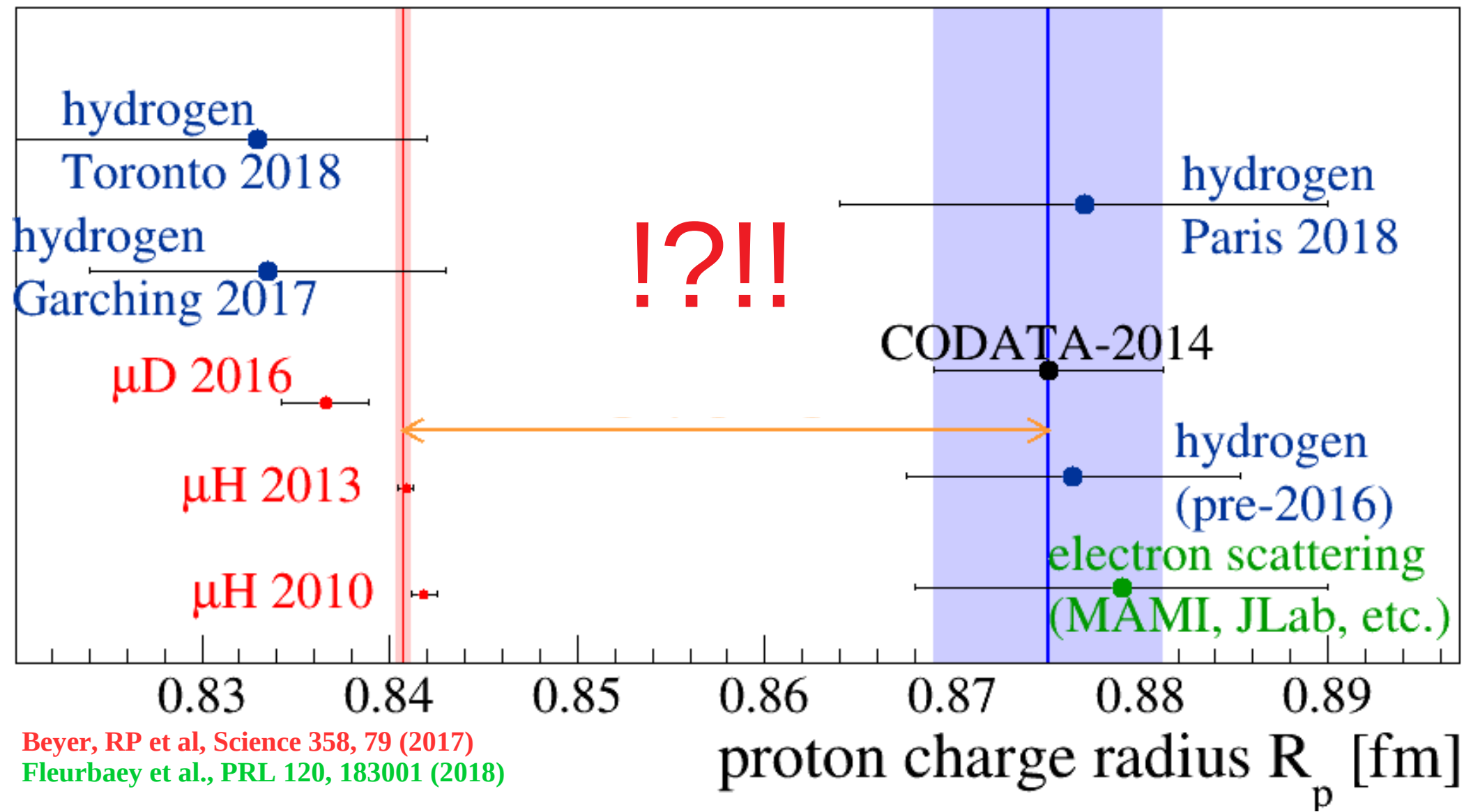
Electrons



New Measurements: Toronto 2S-2P

Muons

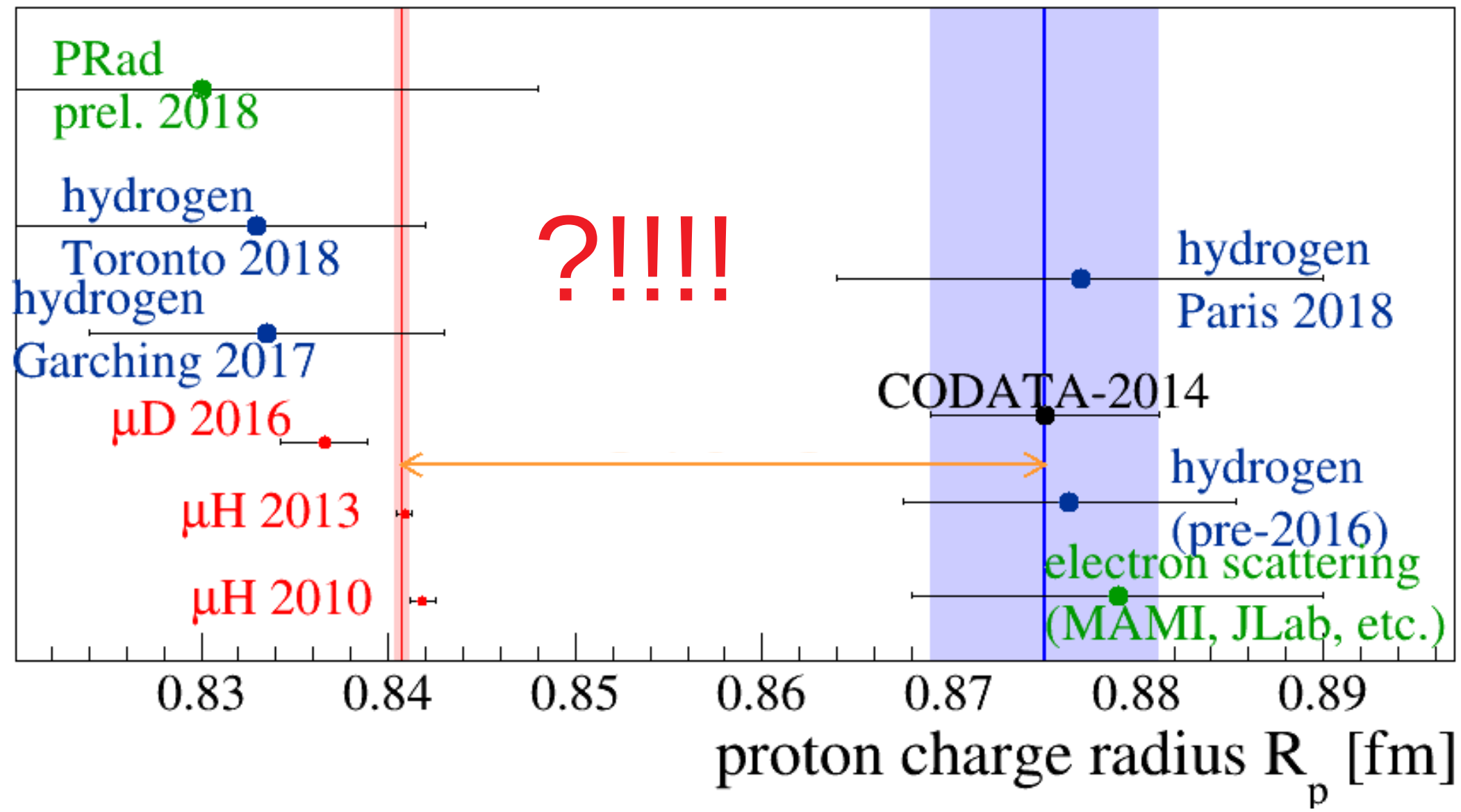
Electrons



New Measurements: PRad

Muons

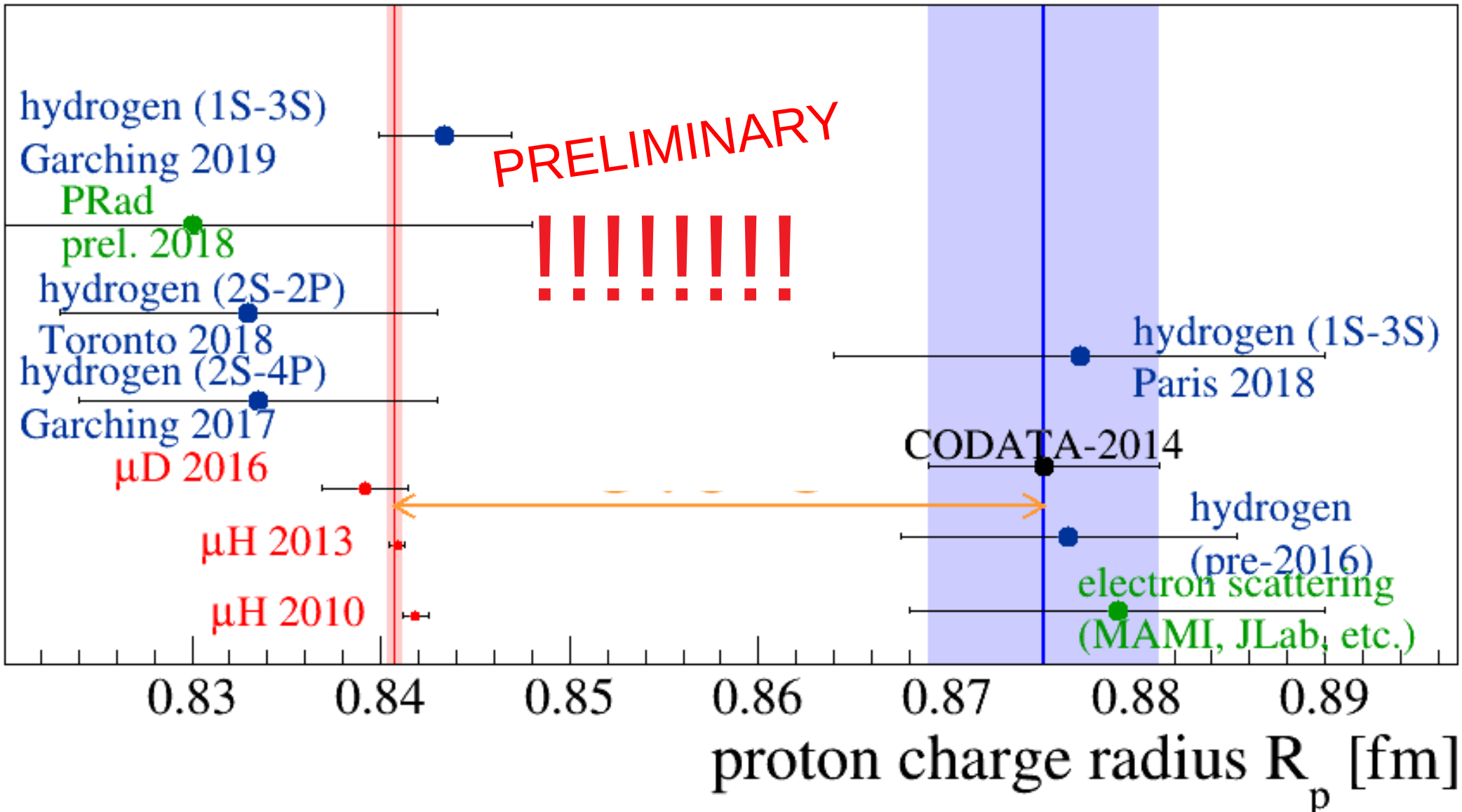
Electrons



New Measurements: Garching 1S-3S

Muons

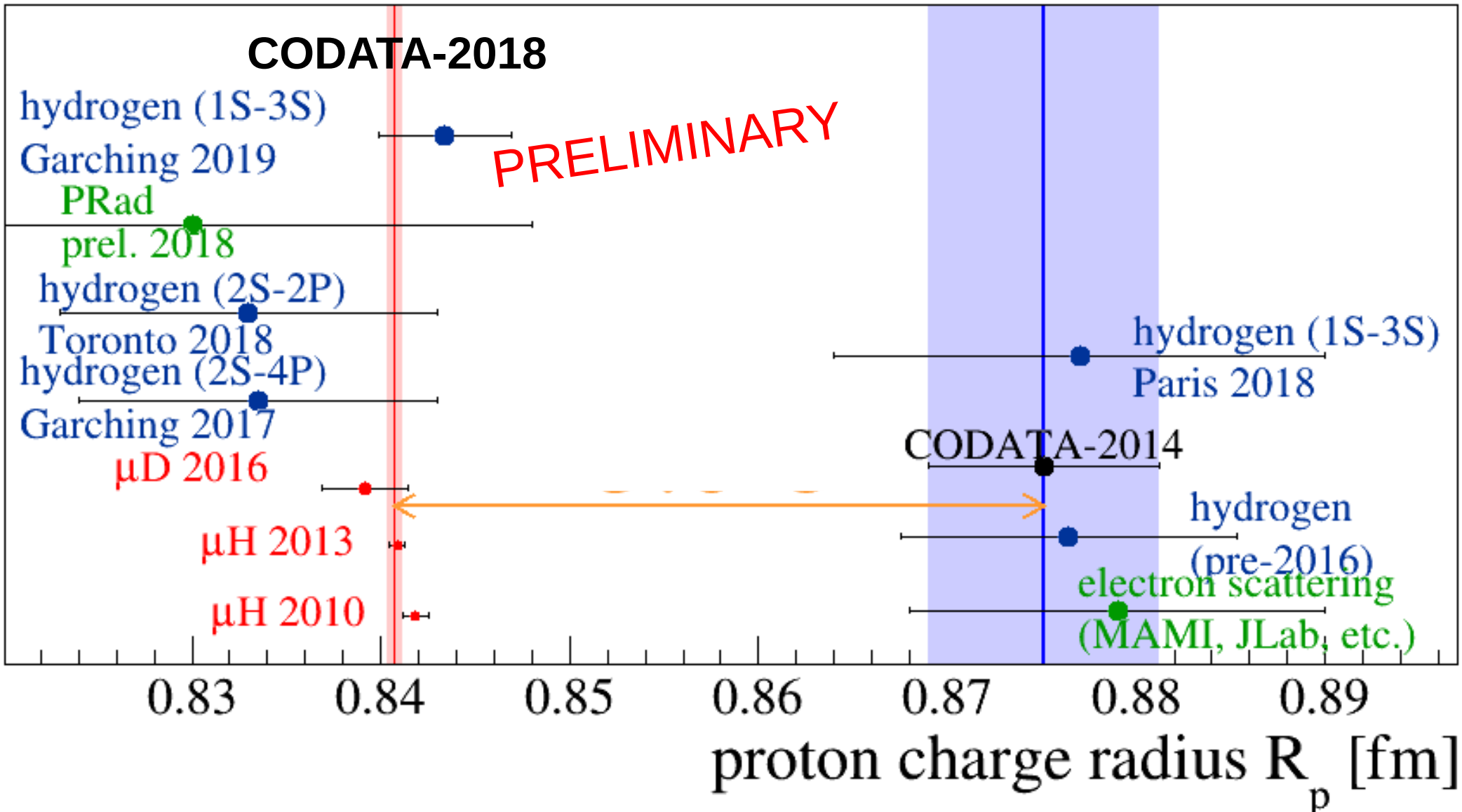
Electrons



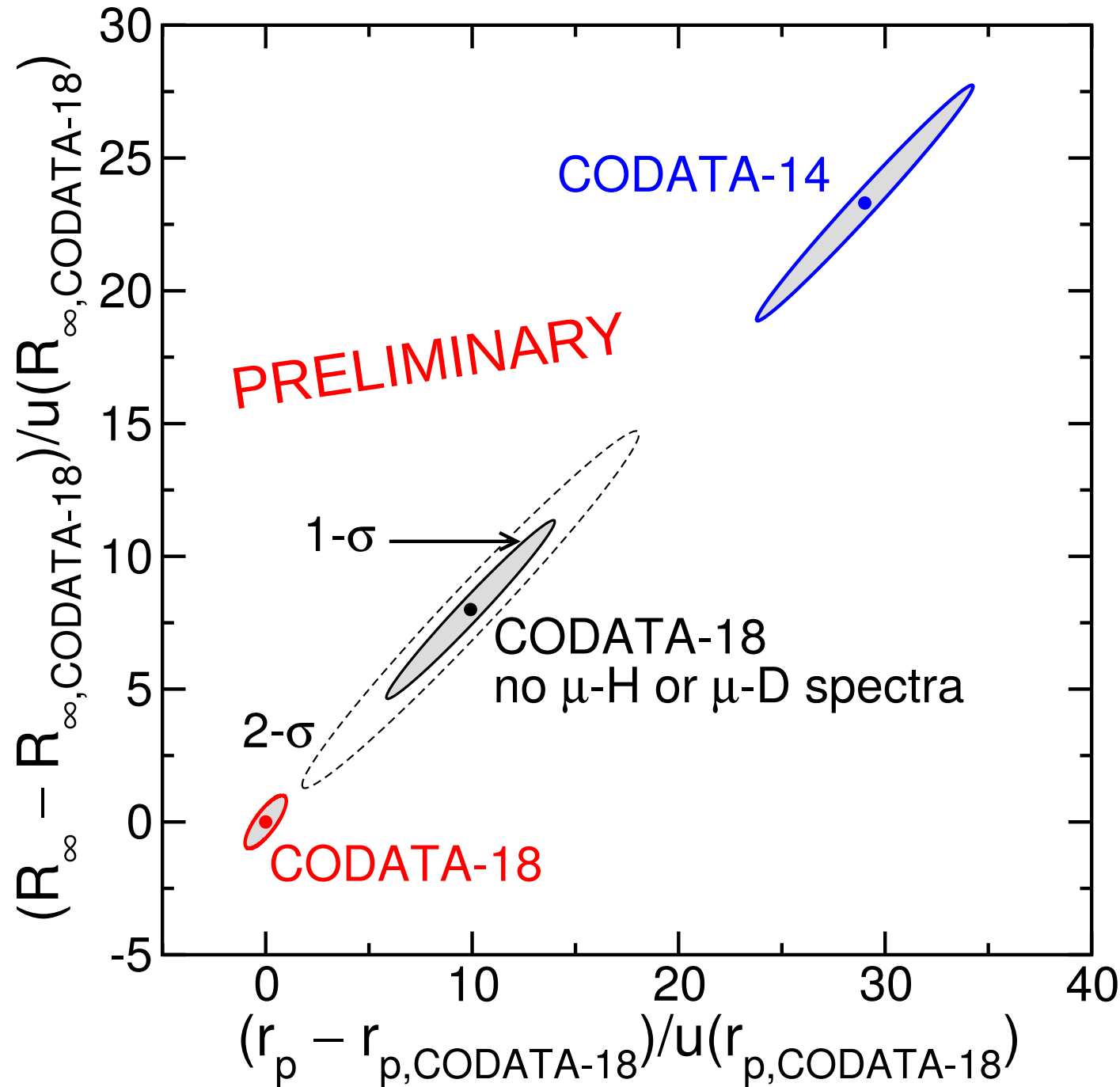
New: CODATA-2018

Muons

Electrons



New: CODATA-2018



Proton radius,
Deuteron radius
and
Rydberg constant
smaller by $>5\sigma$



Conclusions

- smaller radii from **muonic hydrogen** and **deuterium** imply a **smaller Rydberg** constant
- new H(2S-4P) gives **small Rydberg constant** in agreement with muonic values
- new H(2S-4P) gives thus a **smaller proton radius**, too
- new H(1S-3S) however **confirms large proton radius**

More data needed:

- H(2S – 6P, 8P, **9P**, ...) and D(2S-nl) underway in Garching and Colorado
- H(1S – 3S, 4S, ..) underway in Paris and Garching
- H(2S-2P) in Toronto (Hessels)
- Muonium
- Positronium (Cassidy, Crivelli)
- He⁺(1S-2S) underway in Garching (Udem) and Amsterdam (Eikema)
- HD⁺, H₂, etc. in Paris, Amsterdam

- new low-Q² electron scattering at MAMI, JLab, MESA
- muon scattering: MUSE @ PSI, COMPASS @ CERN

Workshop: The “Proton Radius Puzzle”



ECT* Trento, Okt. 2012

47 Teilnehmer

Theorie + Experiment

Atomphysik

Kernphysik

Teilchenphysik

Elektronenstreuung

“Beyond Standard Model”

38 Vorträge

3 “Fighting Sessions”

Am Schluss: Abstimmung

→ Meßfehler

Wir brauchen neue Daten.

Erklärungsversuche

Meßfehler

myonischer Wasserstoff

oder

Wasserstoff UND Elektronenstreuung

Theoriefehler

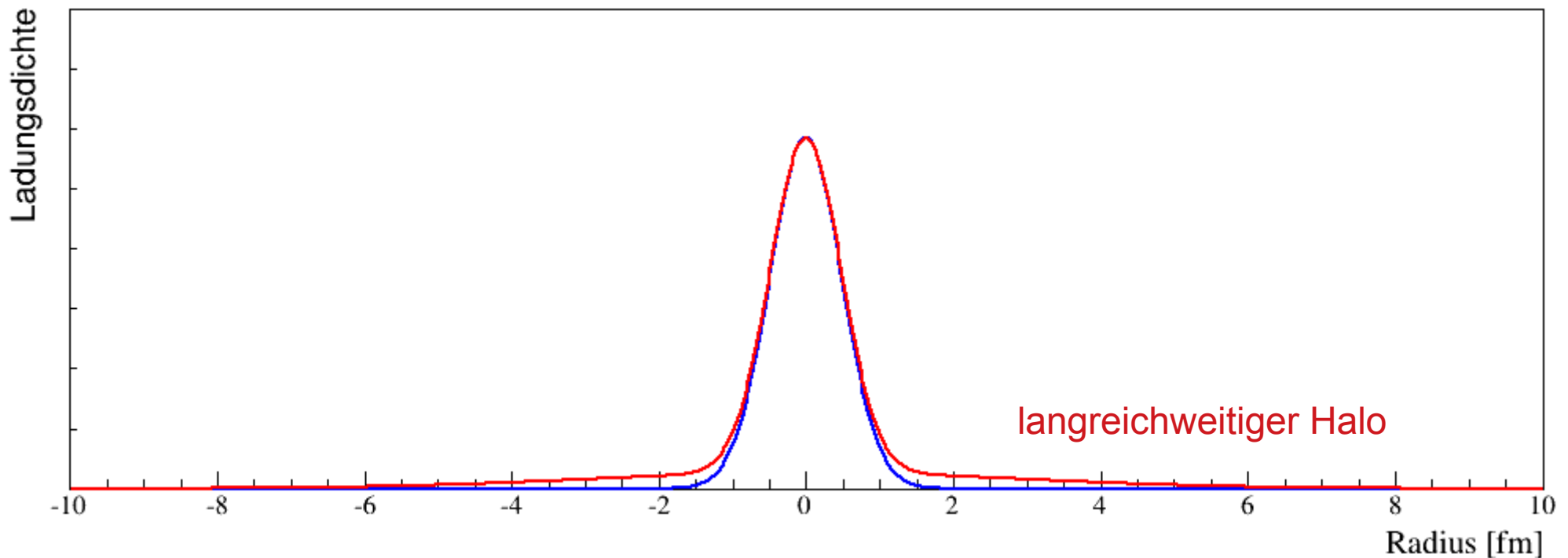
$$\Delta E = 209.998 - 5.226 \mathbf{R}_p^2$$

Fehler im Standard-Modell der Teilchenphysik!

Das Proton schaut anders aus!

Das Proton ist keine feste Kugel.

Die (radiale) Ladungsverteilung schaut anders aus!

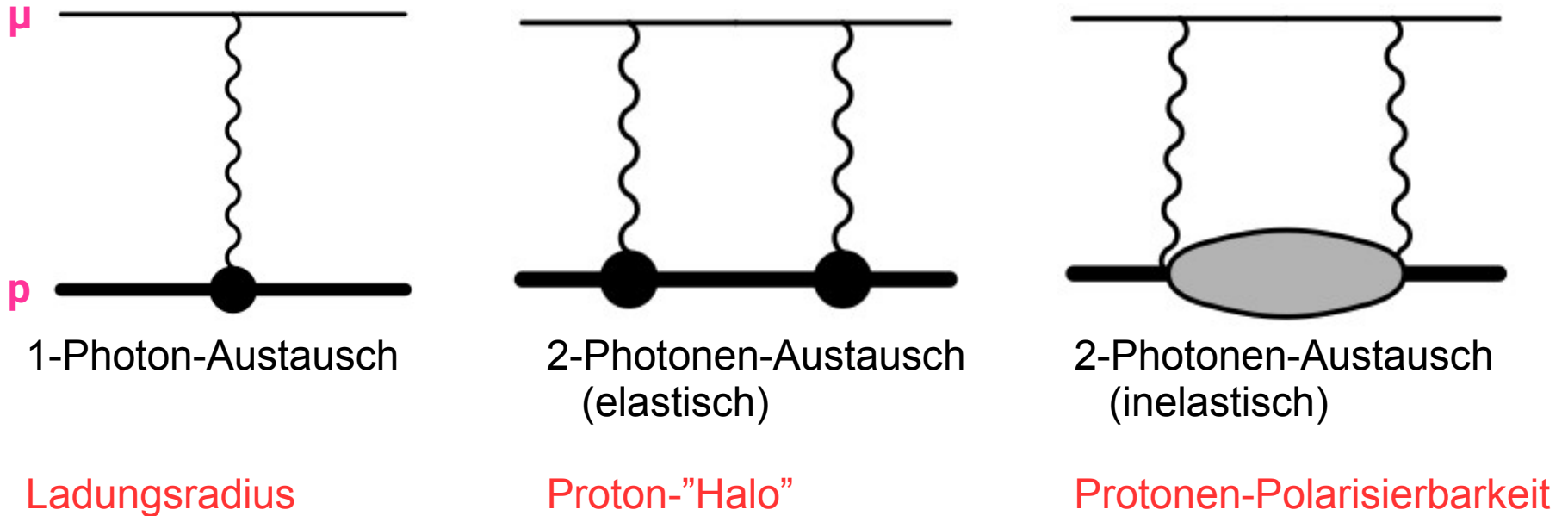


Würde die Diskrepanz erklären!

Ist jedoch im Widerspruch zu Messungen des Halos (e-p Streuung).

3rd Zemach moment: 37 fm^3 vs. $2.7 \pm 0.1 \text{ fm}^3$

Das Myon verändert das Proton



Ja! Die sog. "Polarisierbarkeit des Protons"

Aber der Effekt ist schon berücksichtigt und viel zu klein!

Diskrepanz: 0.31 meV
Polarisierbarkeit: 0.0127 ± 0.0005 meV

Ein neues Teilchen!

mass →	$\approx 2.3 \text{ MeV}/c^2$	$\approx 1.275 \text{ GeV}/c^2$	$\approx 173.07 \text{ GeV}/c^2$	0	$\approx 126 \text{ GeV}/c^2$
charge →	$2/3$	$2/3$	$2/3$	0	0
spin →	$1/2$	$1/2$	$1/2$	1	0
	u up	c charm	t top	g gluon	H Higgs boson
QUARKS	$\approx 4.8 \text{ MeV}/c^2$	$\approx 95 \text{ MeV}/c^2$	$\approx 4.18 \text{ GeV}/c^2$	0	
	$-1/3$	$-1/3$	$-1/3$	0	
	$1/2$	$1/2$	$1/2$	1	
	d down	s strange	b bottom	γ photon	
	$0.511 \text{ MeV}/c^2$	$105.7 \text{ MeV}/c^2$	$1.777 \text{ GeV}/c^2$	$91.2 \text{ GeV}/c^2$	
	-1	-1	-1	0	
	$1/2$	$1/2$	$1/2$	1	
	e electron	μ muon	τ tau	Z Z boson	
LEPTONS	$< 2.2 \text{ eV}/c^2$	$< 0.17 \text{ MeV}/c^2$	$< 15.5 \text{ MeV}/c^2$	$80.4 \text{ GeV}/c^2$	
	0	0	0	± 1	
	$1/2$	$1/2$	$1/2$	1	
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	
				GAUGE BOSONS	

Gravitation!

Dunkle Materie?

Dunkle Energie?

Baryonen-Asymmetrie!

Starkes CP-Problem!

...

Ein neues Teilchen!

Physik jenseits des Standardmodells

könnte im Prinzip für die Diskrepanz verantwortlich sein!

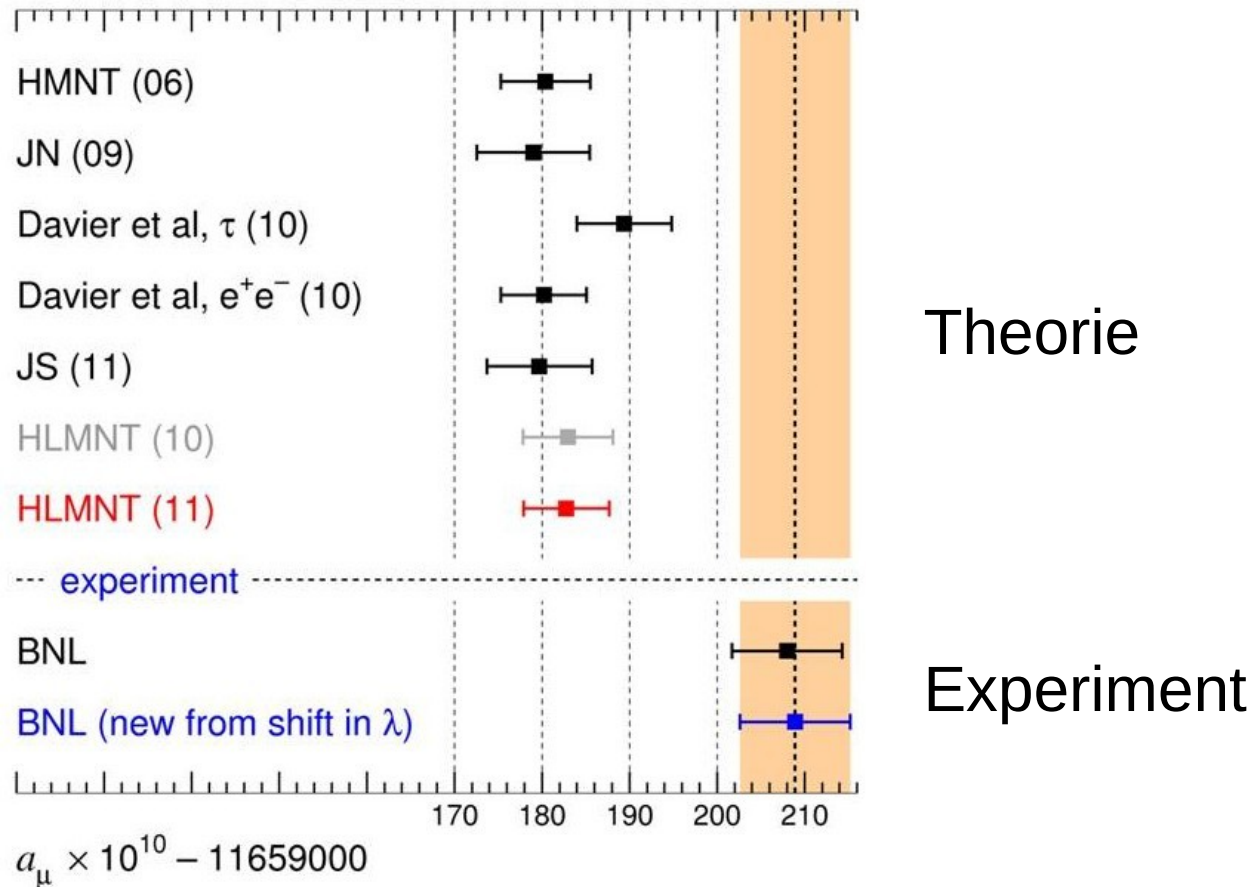
Das wäre ein **neues Teilchen**, das eine **neue Kraft** überträgt!

Diese Teilchen muß aber in das Korsett bestehender
Messungen passen!

Schwierig.....

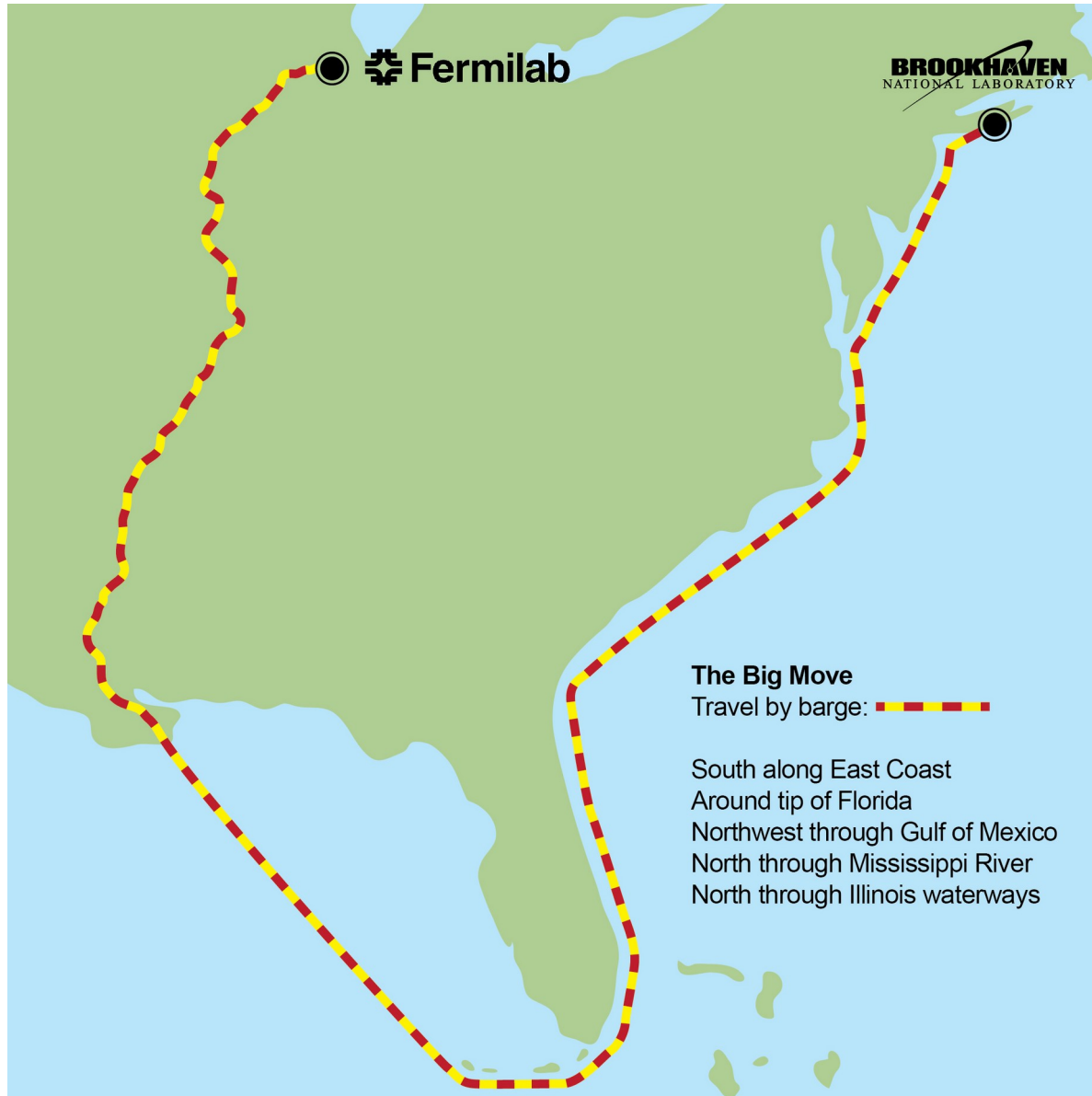
Das Myon macht uns **zwei** Probleme!

Anomales magnetisches Moment des Myons ($g-2$)



Seit 10 Jahren existiert eine ca. 3.6σ Diskrepanz zum Standardmodell

Das neue Myon g-2 Experiment



Umzug: Sommer 2013
Messung: 2017/18

Zusammenfassung

Das Rätsel um das geschrumpfte Proton ist ungelöst.

Vielleicht will uns das Myon etwas sagen?

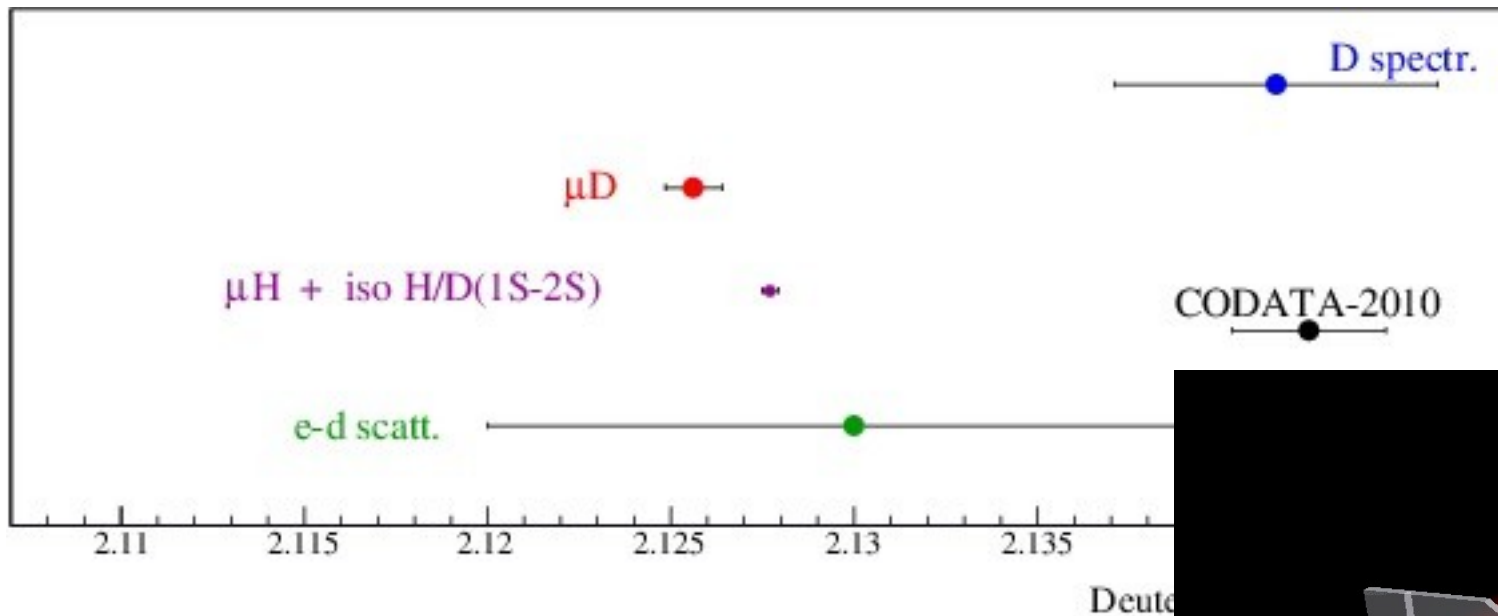
Oder ein **Meßfehler**?

Eine Menge neuer Experimente sind auf dem Weg.

Zum Beispiel: **Myonisches Deuterium**

Radius des Deuterons

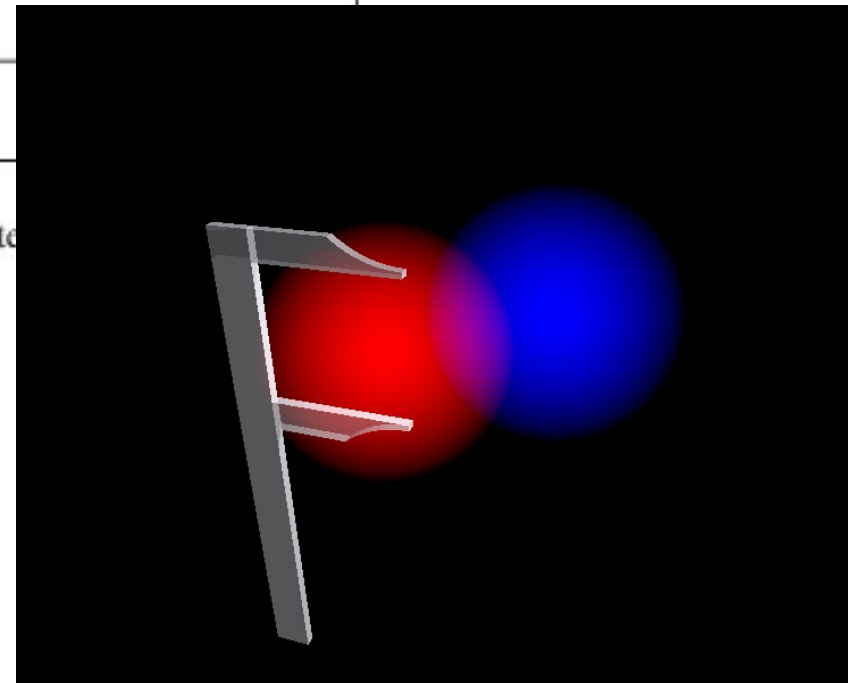
Lamb-Verschiebung in myonischem Deuterium



Deuteron is KONSISTENT zu klein!

$$R_d^2 = R_{\text{struct}}^2 + R_p^2 + R_n^2 (+ DF)$$

Pohl et al. (CREMA), Science 353, 669 (2016)
RP, Physik in unserer Zeit 47, 266 (2016)



Zusammenfassung

Das Rätsel um das geschrumpfte Proton ist ungelöst.

Vielleicht will uns das Myon etwas sagen?

Oder ein Meßfehler?

Eine Menge neuer Experimente sind
auf dem Weg.

Es bleibt spannend.....

Jan Bernauer & RP,
April 2014





Proton Size Investigators thank you for your attention



Up next: Hyperfine structure in μp

The **21 cm line** in hydrogen (1S hyperfine splitting) has been **measured** to **12 digits** (1 mHz) in **1971**:

$$\nu_{\text{exp}} = 1\,420\,405.751\,766\,7 \pm 0.000\,001 \text{ kHz}$$

Essen et al., Nature 229, 110 (1971)

QED test is limited to **6 digits** (800 Hz) because of **proton structure** effects:

$$\nu_{\text{theo}} = 1\,420\,403.1 \pm 0.6_{\text{proton size}} \pm 0.4_{\text{polarizability}} \text{ kHz}$$

Eides et al., Springer Tracts 222, 217 (2007)

Proton Zemach radius

HFS depends on “Zemach” radius:

$$\Delta E = -2(Z\alpha)m\langle r \rangle_{(2)} E_F$$

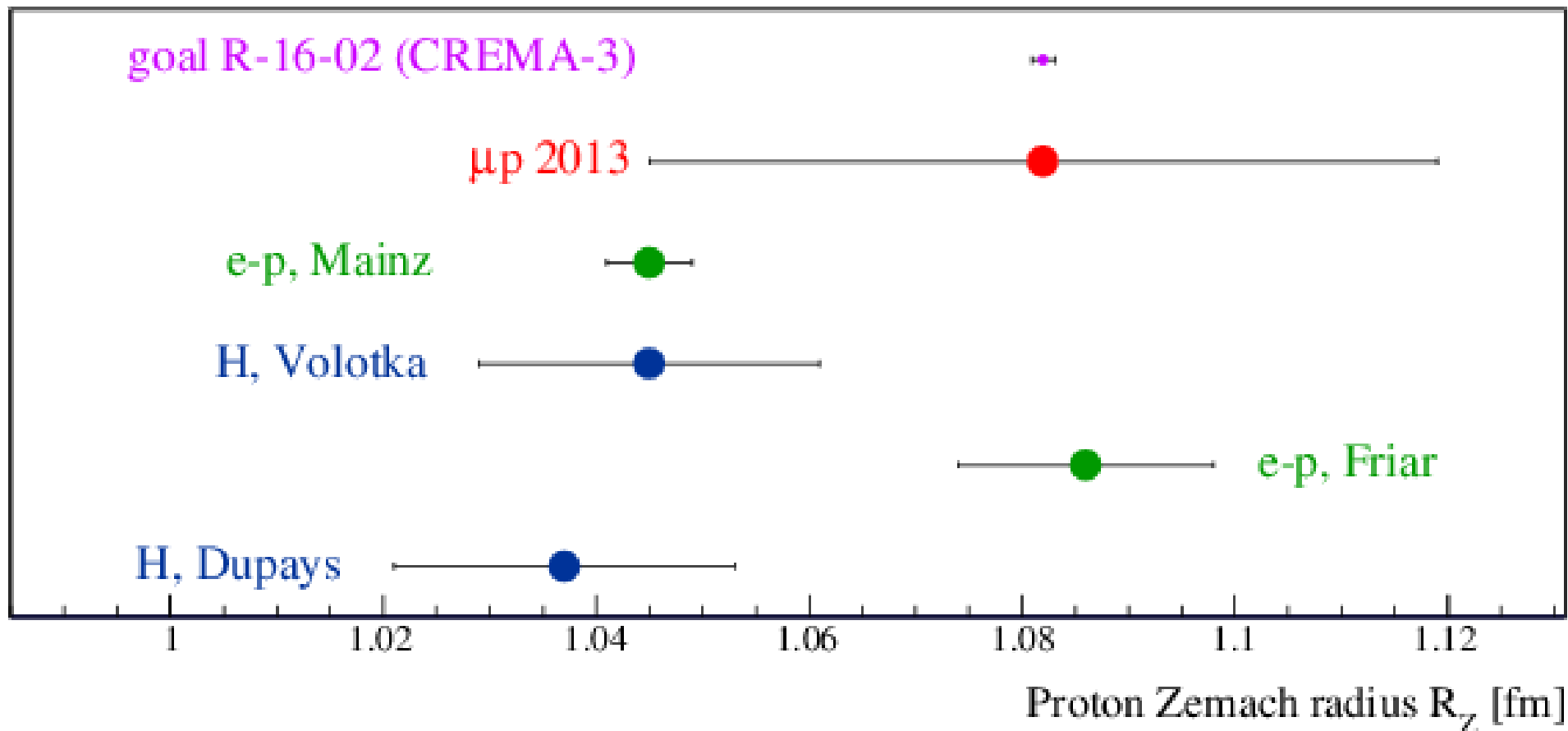
$$\langle r \rangle_{(2)} = \int d^3r d^3r' \rho_E(r) \rho_M(r') |r - r'|$$

Zemach, Phys. Rev. 104, 1771 (1956)

Form factors and momentum space

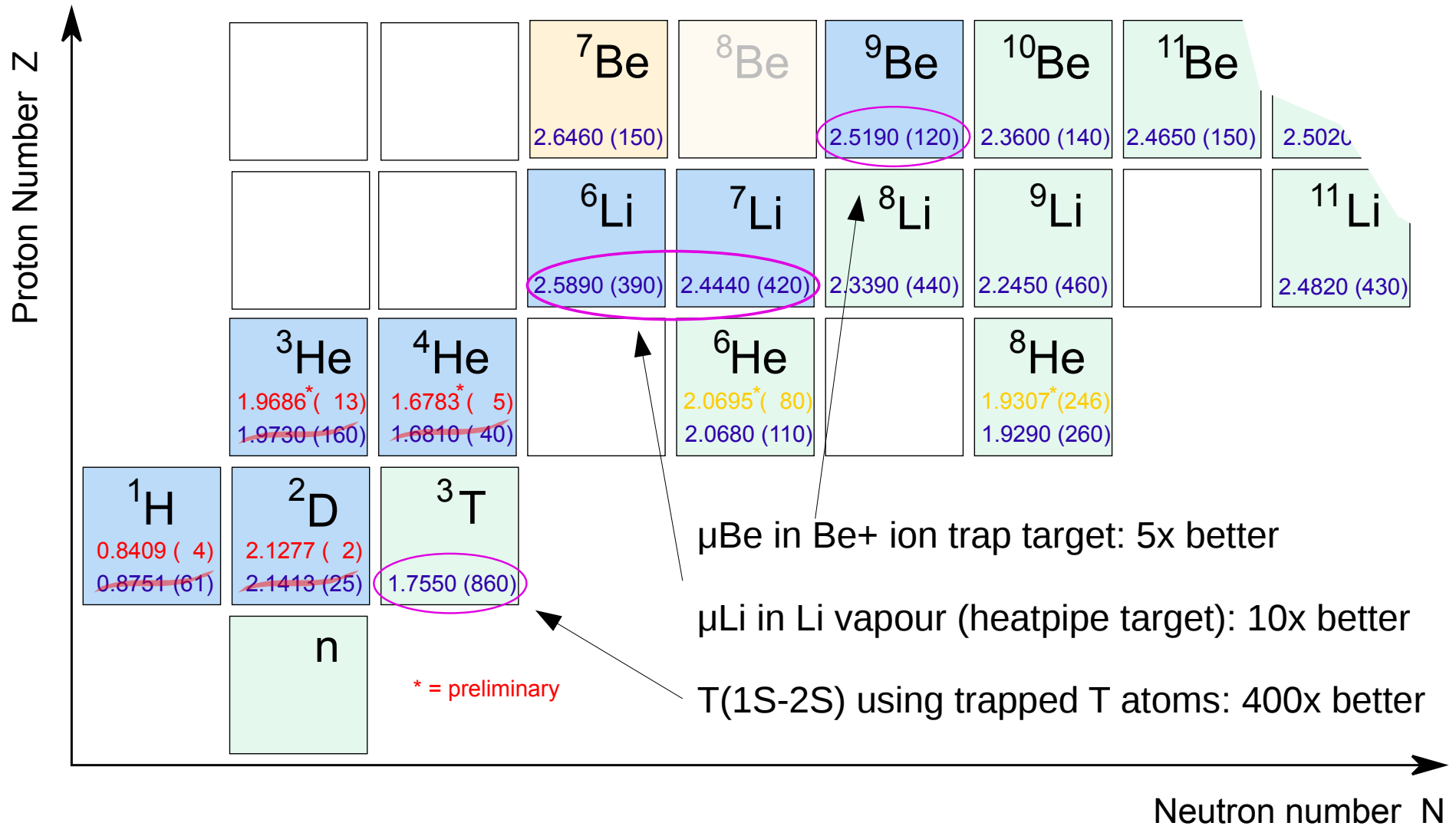
$$\Delta E = \frac{8(Z\alpha)m}{\pi n^3} E_F \int_0^\infty \frac{dk}{k^2} \left[\frac{G_E(-k^2) G_M(-k^2)}{1+\kappa} \right]$$

Proton Zemach radius from μp



PSI Exp. R-16-02: Antognini, RP et al. (CREMA-3 / HyperMu)

Charge radii: The future



Thanks a lot for your attention

The Garching Hydrogen Team:

Axel Beyer, Lothar Maisenbacher, Arthur Matveev, RP,
Ksenia Khabarova, Alexey Grinin, Tobias Lamour, Dylan C. Yost,
Theodor W. Hänsch, Nikolai Kolachevsky, Thomas Udem

The CREMA Collaboration:

Aldo Antognini, Fernando D. Amaro, François Biraben, João M. R. Cardoso,
Daniel S. Covita, Andreas Dax, Satish Dhawan, Marc Diepold, Luis M. P.
Fernandes, Adolf Giesen, Andrea L. Gouvea, Thomas Graf, Theodor W.
Hänsch, Paul Indelicato, Lucile Julien, Paul Knowles, Franz Kottmann, Eric-
Olivier Le Bigot, Yi-Wei Liu, José A. M. Lopes, Livia Ludhova, Cristina M. B.
Monteiro, Françoise Mulhauser, Tobias Nebel, François Nez, Paul
Rabinowitz, Joaquim M. F. dos Santos, Lukas A. Schaller, Karsten
Schuhmann, Catherine Schwob, David Taqqu, João F. C. A. Veloso, RP

Thanks a lot for your attention

My new Mainz group:

Jan Haack, Rishi Horn, Ahmed Ouf, Stefan Schmidt, Lukas Schumacher, Gregor Schwendler, Andreas Wieltsch, Marcel Willig

The Garching Hydrogen Team:

Axel Beyer, Lothar Maisenbacher, Arthur Matveev, RP, Ksenia Khabarova, Alexey Grinin, Tobias Lamour, Dylan C. Yost, Theodor W. Hänsch, Nikolai Kolachevsky, Thomas Udem

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Thanks a lot for your attention

My new Mainz group:

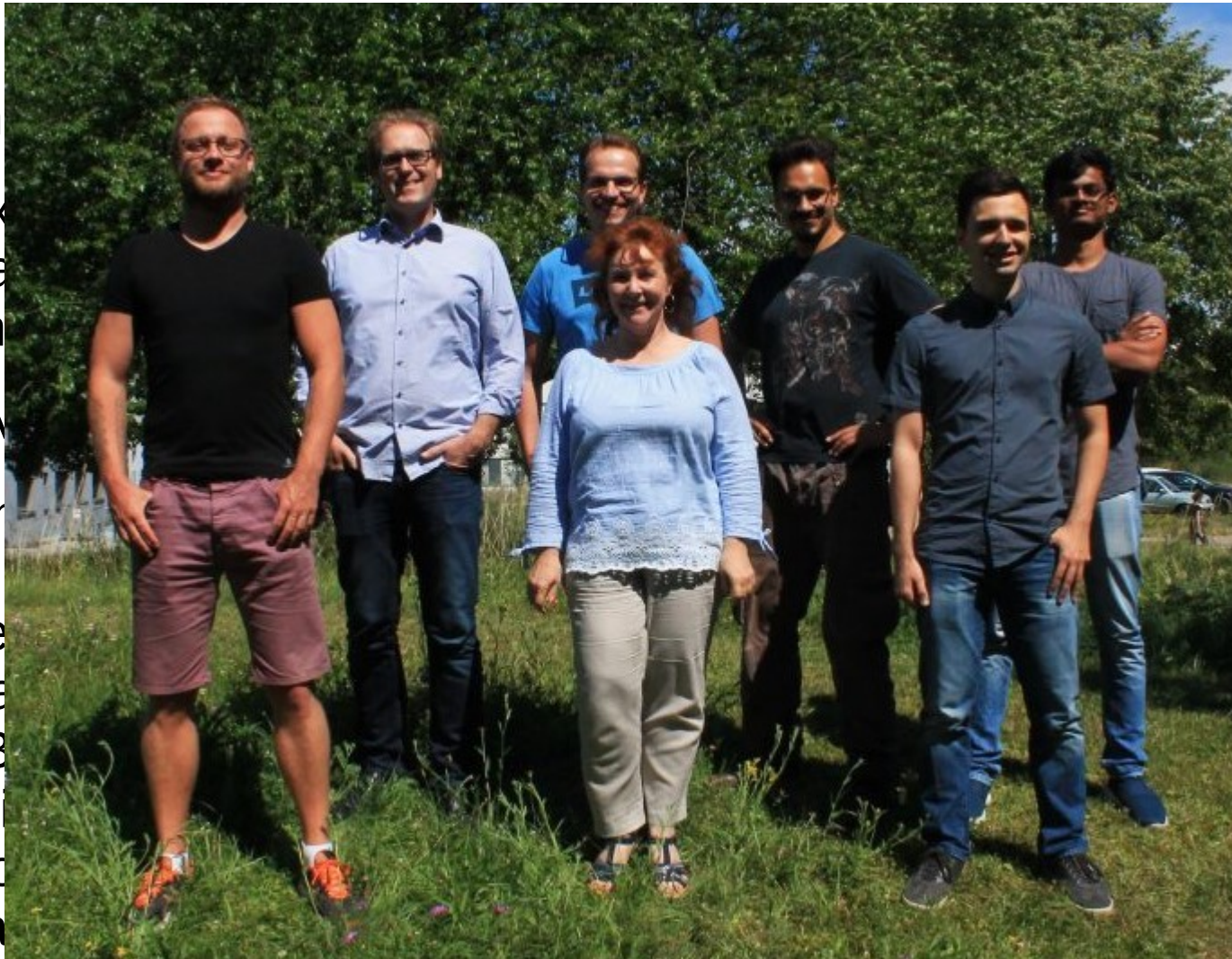
Jan Haack, Rishi Horn, Ahmed Ouf, Stefan Schmidt, Lukas Schumacher, Gregor Schwendler, Andreas Wieltsch, Marcel Willig

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eodor W.
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eloso, RP

■ ■ ■

CODATA “sub-adjustments”

Adj. 3: “The Adjustment” (all data) $R_p = 0.8775(51)$ fm, $R_d = 2.1424(21)$ fm
 Adj. 8: H spectroscopy only $R_p = 0.8764(89)$ fm
 Adj. 10: D spectroscopy only $R_d = 2.1210(250)$ fm

TABLE XXXVIII. Summary of the results of some of the least-squares adjustments used to analyze the input data related to R_∞ . The values of R_∞ , r_p , and r_d are those obtained in the indicated adjustment, N is the number of input data, M is the number of adjusted constants, $\nu = N - M$ is the degrees of freedom, and $R_B = \sqrt{\chi^2/\nu}$ is the Birge ratio. See the text for an explanation and discussion of each adjustment. In brief, adjustment 6 is 3 but the scattering data for the nuclear radii are omitted; 7 is 3, but with only the hydrogen data included (no isotope shift); 8 is 7 with the r_p data deleted; 9 and 10 are similar to 7 and 8, but for the deuterium data; 11 is 3 with the muonic Lamb-shift value of r_p included; and 12 is 11, but without the scattering values of r_p and r_d .

Adj.	N	M	ν	χ^2	R_B	R_∞ (m ⁻¹)	$u_r(R_\infty)$	r_p (fm)	r_d (fm)
3	149	82	67	58.1	0.93	10 973 731.568 539(55)	5.0×10^{-12}	<u>0.8775(51)</u>	<u>2.1424(21)</u>
6	146	82	64	55.5	0.93	10 973 731.568 521(82)	7.4×10^{-12}	0.8758(77)	2.1417(31)
7	131	72	59	53.4	0.95	10 973 731.568 561(60)	5.5×10^{-12}	0.8796(56)	
8	129	72	57	52.5	0.96	10 973 731.568 528(94)	8.6×10^{-12}	<u>0.8764(89)</u>	
9	114	65	49	46.9	0.98	10 973 731.568 37(13)	1.1×10^{-11}		2.1288(93)
10	113	65	48	46.8	0.99	10 973 731.568 28(30)	2.7×10^{-11}		<u>2.121(25)</u>
11	150	82	68	104.9	1.24	10 973 731.568 175(12)	1.1×10^{-12}	0.842 25(65)	2.128 24(28)
12	147	82	65	74.3	1.07	10 973 731.568 171(12)	1.1×10^{-12}	0.841 93(66)	2.128 11(28)

Spectroscopy data in CODATA

TABLE XI. Summary of measured transition frequencies ν considered in the present work for the determination of the Rydberg constant R_∞ (H is hydrogen and D is deuterium).

Authors	Laboratory ^a	Frequency interval(s)	Reported value ν (kHz)	Rel. stand. uncert. u_r	
(Fischer <i>et al.</i> , 2004)	MPQ	$\nu_H(1S_{1/2} - 2S_{1/2})$	<u>2 466 061 413 187.080(34)</u>	1.4×10^{-14}	H(1S-2S)
(Weitz <i>et al.</i> , 1995)	MPQ	$\nu_H(2S_{1/2} - 4S_{1/2}) - \frac{1}{4}\nu_H(1S_{1/2} - 2S_{1/2})$	4 797 338(10)	2.1×10^{-6}	
		$\nu_H(2S_{1/2} - 4D_{5/2}) - \frac{1}{4}\nu_H(1S_{1/2} - 2S_{1/2})$	6 490 144(24)	3.7×10^{-6}	
		$\nu_D(2S_{1/2} - 4S_{1/2}) - \frac{1}{4}\nu_D(1S_{1/2} - 2S_{1/2})$	4 801 693(20)	4.2×10^{-6}	
		$\nu_D(2S_{1/2} - 4D_{5/2}) - \frac{1}{4}\nu_D(1S_{1/2} - 2S_{1/2})$	6 494 841(41)	6.3×10^{-6}	
(Parthey <i>et al.</i> , 2010)	MPQ	$\nu_D(1S_{1/2} - 2S_{1/2}) - \nu_H(1S_{1/2} - 2S_{1/2})$	<u>670 994 334.606(15)</u>	2.2×10^{-11}	D(1S-2S) –
(de Beauvoir <i>et al.</i> , 1997)	LKB/SYRTE	$\nu_H(2S_{1/2} - 8S_{1/2})$	770 649 350 012.0(8.6)	1.1×10^{-11}	H(1S-2S)
		$\nu_H(2S_{1/2} - 8D_{3/2})$	770 649 504 450.0(8.3)	1.1×10^{-11}	
		$\nu_H(2S_{1/2} - 8D_{5/2})$	770 649 561 584.2(6.4)	8.3×10^{-12}	
		$\nu_D(2S_{1/2} - 8S_{1/2})$	770 859 041 245.7(6.9)	8.9×10^{-12}	(iso shift)
		$\nu_D(2S_{1/2} - 8D_{3/2})$	770 859 195 701.8(6.3)	8.2×10^{-12}	
		$\nu_D(2S_{1/2} - 8D_{5/2})$	770 859 252 849.5(5.9)	7.7×10^{-12}	
(Schwob <i>et al.</i> , 1999)	LKB/SYRTE	$\nu_H(2S_{1/2} - 12D_{3/2})$	799 191 710 472.7(9.4)	1.2×10^{-11}	
		$\nu_H(2S_{1/2} - 12D_{5/2})$	799 191 727 403.7(7.0)	8.7×10^{-12}	
		$\nu_D(2S_{1/2} - 12D_{3/2})$	799 409 168 038.0(8.6)	1.1×10^{-11}	
		$\nu_D(2S_{1/2} - 12D_{5/2})$	799 409 184 966.8(6.8)	8.5×10^{-12}	
(Arnoult <i>et al.</i> , 2010)	LKB	$\nu_H(1S_{1/2} - 3S_{1/2})$	2 922 743 278 678(13)	4.4×10^{-12}	
(Bourzeix <i>et al.</i> , 1996)	LKB	$\nu_H(2S_{1/2} - 6S_{1/2}) - \frac{1}{4}\nu_H(1S_{1/2} - 3S_{1/2})$	4 197 604(21)	4.9×10^{-6}	
		$\nu_H(2S_{1/2} - 6D_{5/2}) - \frac{1}{4}\nu_H(1S_{1/2} - 3S_{1/2})$	4 699 099(10)	2.2×10^{-6}	
(Berkeland, Hinds, and Boshier, 1995)	Yale	$\nu_H(2S_{1/2} - 4P_{1/2}) - \frac{1}{4}\nu_H(1S_{1/2} - 2S_{1/2})$	4 664 269(15)	3.2×10^{-6}	
		$\nu_H(2S_{1/2} - 4P_{3/2}) - \frac{1}{4}\nu_H(1S_{1/2} - 2S_{1/2})$	6 035 373(10)	1.7×10^{-6}	
(Hagley and Pipkin, 1994)	Harvard	$\nu_H(2S_{1/2} - 2P_{3/2})$	9 911 200(12)	1.2×10^{-6}	
(Lundeen and Pipkin, 1986)	Harvard	$\nu_H(2P_{1/2} - 2S_{1/2})$	1 057 845.0(9.0)	8.5×10^{-6}	
(Newton, Andrews, and Unsworth, 1979)	U. Sussex	$\nu_H(2P_{1/2} - 2S_{1/2})$	1 057 862(20)	1.9×10^{-5}	

^aMPQ: Max-Planck-Institut für Quantenoptik, Garching. LKB: Laboratoire Kastler-Brossel, Paris. SYRTE: Systèmes de référence Temps Espace, Paris, formerly Laboratoire Primaire du Temps et des Fréquences (LPTF).

Spectroscopy data: H

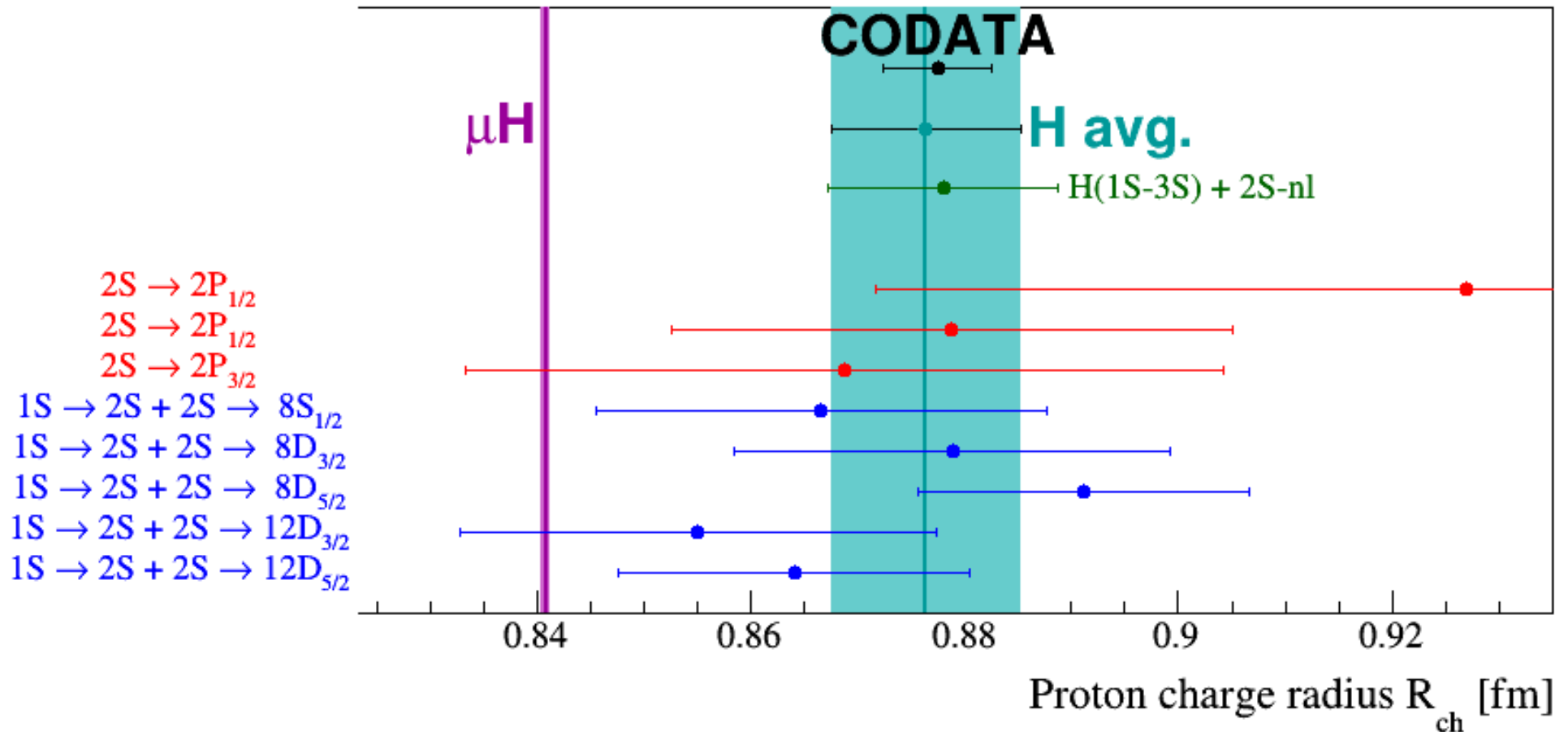
TABLE III: Some recent measurements in atomic hydrogen. An asterisk following the reference denotes items considered in the most recent CODATA-2010 report. Following our nomenclature, the $2S \rightarrow 2P_{1/2}$ transition must be assigned a negative frequency, because the final state $(n', \ell', j') = 2P_{1/2}$ is *lower* than the initial $(n, \ell, j) = 2S_{1/2}$ state.

#	$(n, \ell, j) - (n', \ell', j')$	ν_{meas} (kHz)	rel. unc.	Source	Ref.
H1	$2S_{1/2} \rightarrow 2P_{1/2}$	-1 057 862(20)	1.9×10^{-5}	Sussex 1979	[25] *
H2		-1 057 845.0(9.0)	8.5×10^{-6}	Harvard 1986	[26] *
H3	$2S_{1/2} \rightarrow 2P_{3/2}$	9 911 200(12)	1.2×10^{-6}	Harvard 1994	[27] *
H4	$2S_{1/2} \rightarrow 8S_{1/2}$	770 649 350 012.0(8.6)	1.1×10^{-11}	LKB 1997	[28] *
H5	$2S_{1/2} \rightarrow 8D_{3/2}$	770 649 504 450.0(8.3)	1.1×10^{-11}	LKB 1997	[28] *
H6	$2S_{1/2} \rightarrow 8D_{5/2}$	770 649 561 584.2(6.4)	8.3×10^{-12}	LKB 1997	[28] *
H7	$2S_{1/2} \rightarrow 12D_{3/2}$	799 191 710 472.7(9.4)	1.1×10^{-11}	LKB 1999	[29] *
H8	$2S_{1/2} \rightarrow 12D_{5/2}$	799 191 727 403.7(7.0)	8.7×10^{-12}	LKB 1999	[29] *
H9	$1S_{1/2} \rightarrow 2S_{1/2}$	2 466 061 413 187.103(46)	1.9×10^{-14}	MPQ 2000	[30]
H10		2 466 061 413 187.080(34)	1.4×10^{-14}	MPQ 2004	[31] *
H11		2 466 061 413 187.035(10)	4.2×10^{-15}	MPQ 2011	[32]
H12		2 466 061 413 187.018(11)	4.5×10^{-15}	MPQ 2013	[33]
H13	$1S_{1/2} \rightarrow 3S_{1/2}$	2 922 743 278 678(13)	4.4×10^{-12}	LKB 2010	[34] *
H14		2 922 743 278 659(17)	5.8×10^{-12}	MPQ 2016	[35]

Rp from H spectroscopy

#	Transition	r_p [fm]
H1	$2S \rightarrow 2P_{1/2}$	0.9270 ± 0.0553
H2	$2S \rightarrow 2P_{1/2}$	0.8788 ± 0.0262
H3	$2S \rightarrow 2P_{3/2}$	0.8688 ± 0.0354
H10 + H4	$1S \rightarrow 2S + 2S \rightarrow 8S_{1/2}$	0.8666 ± 0.0211
H10 + H5	$1S \rightarrow 2S + 2S \rightarrow 8D_{3/2}$	0.8789 ± 0.0204
H10 + H6	$1S \rightarrow 2S + 2S \rightarrow 8D_{5/2}$	0.8911 ± 0.0155
H10 + H7	$1S \rightarrow 2S + 2S \rightarrow 12D_{3/2}$	0.8551 ± 0.0222
H10 + H8	$1S \rightarrow 2S + 2S \rightarrow 12D_{5/2}$	0.8641 ± 0.0164
$1S \rightarrow 2S$ (H10) + all H($2S \rightarrow n\ell$)		0.8747 ± 0.0091 avg.
$1S \rightarrow 3S$ (H13+H14) + all H($2S \rightarrow n\ell$)		0.8780 ± 0.0108
CODATA Adj. 8		0.8764 ± 0.0089 Eq. (18)

Rp from H spectroscopy



Spectroscopy data: D

TABLE V: Some recent measurements of the H-D isotope shift. An asterisk following the reference denotes items considered in the most recent CODATA-2010 report.

#	Transition	Frequency (kHz)	rel. unc.	Source	Ref.
I1	$1S_{1/2} \rightarrow 2S_{1/2}$	670 994 334.64(15)	2.2×10^{-10}	MPQ 1998 [7]	
I2		670 994 334.606(15)	2.2×10^{-11}	MPQ 2010 [8] *	

TABLE VI: Some recent measurements in atomic deuterium. An asterisk following the reference denotes items considered in the most recent CODATA-2010 report. Items D9 and D10 are direct measurements, while D11 and D12 have been constructed as justified in the text.

#	$(n, \ell, j) - (n', \ell', j')$	ν_{meas} (kHz)	rel. unc.	Source	Ref.
D4	$2S_{1/2} \rightarrow 8S_{1/2}$	770 859 041 245.7(6.9)	8.9×10^{-12}	LKB 1997	[28] *
D5	$2S_{1/2} \rightarrow 8D_{3/2}$	770 859 195 701.8(6.3)	8.2×10^{-12}	LKB 1997	[28] *
D6	$2S_{1/2} \rightarrow 8D_{5/2}$	770 859 252 849.5(5.9)	7.7×10^{-12}	LKB 1997	[28] *
D7	$2S_{1/2} \rightarrow 12D_{3/2}$	799 409 168 038.0(8.6)	1.1×10^{-11}	LKB 1999	[29] *
D8	$2S_{1/2} \rightarrow 12D_{5/2}$	799 409 184 966.8(6.8)	8.5×10^{-12}	LKB 1999	[29] *
D9	$1S_{1/2} \rightarrow 2S_{1/2}$	2 466 732 407 521.8(1.5)	6.1×10^{-13}	MPQ 1997	[36]
D10		2 466 732 407 522.88(91)	3.7×10^{-13}	MPQ 1997	[36]
D11		2 466 732 407 521.74(20)	7.9×10^{-14}	MPQ 1998/2000	H9 +I1
D12		2 466 732 407 521.641(25)	1.0×10^{-14}	MPQ 2010/2011	H11+I2

D only



H + iso

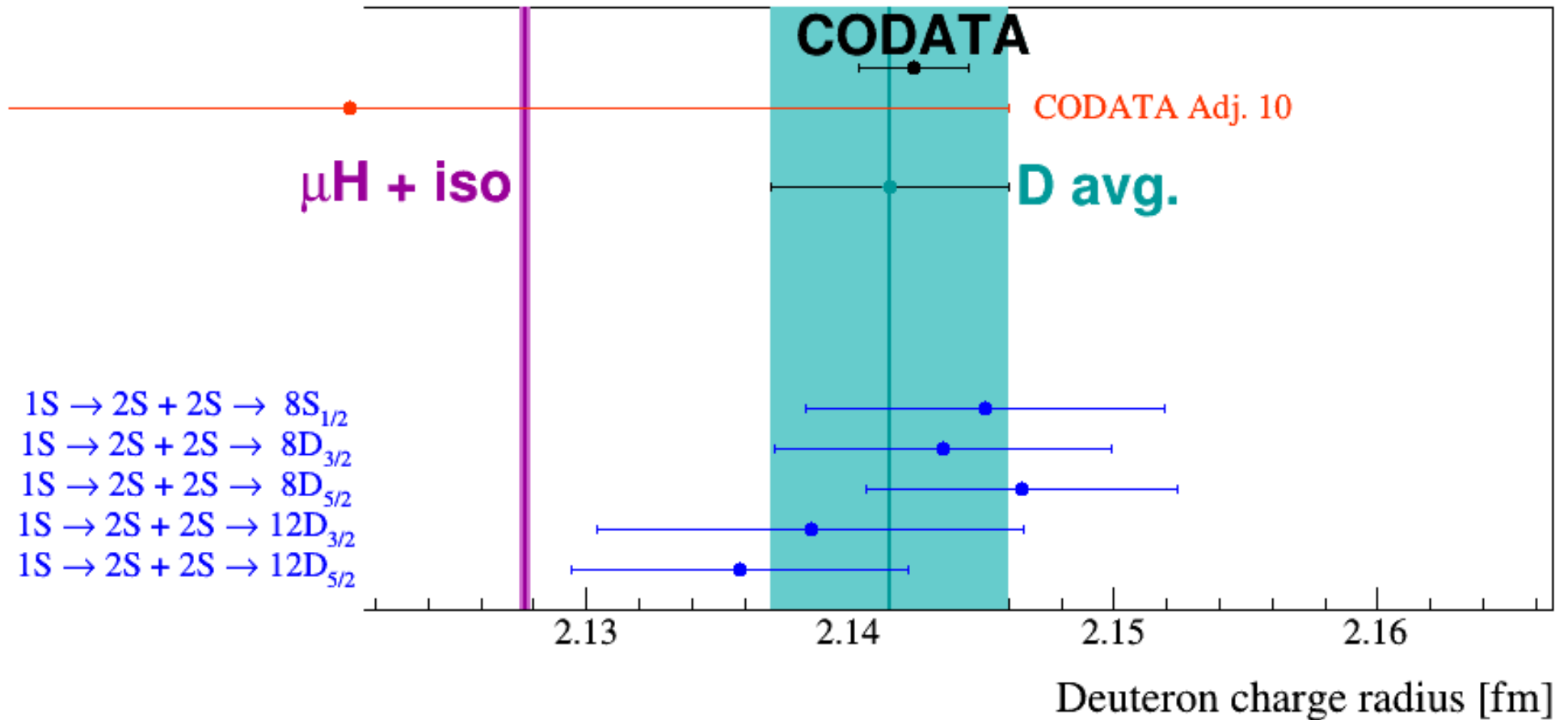


Rd from D spectroscopy

TABLE VII: Deuteron charge radii from deuterium. The value labelled “Eq. (19)” is our result. It is the average of the individual values above it, taking into account the known correlations between the $2S \rightarrow n\ell$ measurements. The next 2 values use items D9 and D10, which have not been measured using atomic hydrogen as a transfer oscillator (see text).

#	Transition	r_d [fm]	
D12 + D4	$1S \rightarrow 2S + 2S \rightarrow 8S_{1/2}$	2.1451 ± 0.0068	
D12 + D5	$1S \rightarrow 2S + 2S \rightarrow 8D_{3/2}$	2.1435 ± 0.0064	
D12 + D6	$1S \rightarrow 2S + 2S \rightarrow 8D_{5/2}$	2.1465 ± 0.0059	
D12 + D7	$1S \rightarrow 2S + 2S \rightarrow 12D_{3/2}$	2.1385 ± 0.0081	
D12 + D8	$1S \rightarrow 2S + 2S \rightarrow 12D_{5/2}$	2.1358 ± 0.0064	
D12 + all D($2S \rightarrow n\ell$)		2.1415 ± 0.0045	← Eq. (19)
D9 + all D($2S \rightarrow n\ell$)		2.1414 ± 0.0045	5.6 times more accurate!
D10 + all D($2S \rightarrow n\ell$)		2.1411 ± 0.0045	
CODATA Adj. 10:		2.1214 ± 0.0253	

Rd from D spectroscopy



Rd from D spectroscopy

WHICH 1S-2S we choose is IRRELEVANT!

#	Transition	r_d [fm]
D12 + D4	$1S \rightarrow 2S + 2S \rightarrow 8S_{1/2}$	2.1451 ± 0.0068
D12 + D5	$1S \rightarrow 2S + 2S \rightarrow 8D_{3/2}$	2.1435 ± 0.0064
D12 + D6	$1S \rightarrow 2S + 2S \rightarrow 8D_{5/2}$	2.1465 ± 0.0059
D12 + D7	$1S \rightarrow 2S + 2S \rightarrow 12D_{3/2}$	2.1385 ± 0.0081
D12 + D8	$1S \rightarrow 2S + 2S \rightarrow 12D_{5/2}$	2.1358 ± 0.0064
D12 + all D($2S \rightarrow n\ell$)		2.1415 ± 0.0045 Eq. (19)
D9 + all D($2S \rightarrow n\ell$)		2.1414 ± 0.0045
D10 + all D($2S \rightarrow n\ell$)		2.1411 ± 0.0045
CODATA Adj. 10:		2.1214 ± 0.0253

Deuteron charge radius from spectroscopy data in atomic deuterium

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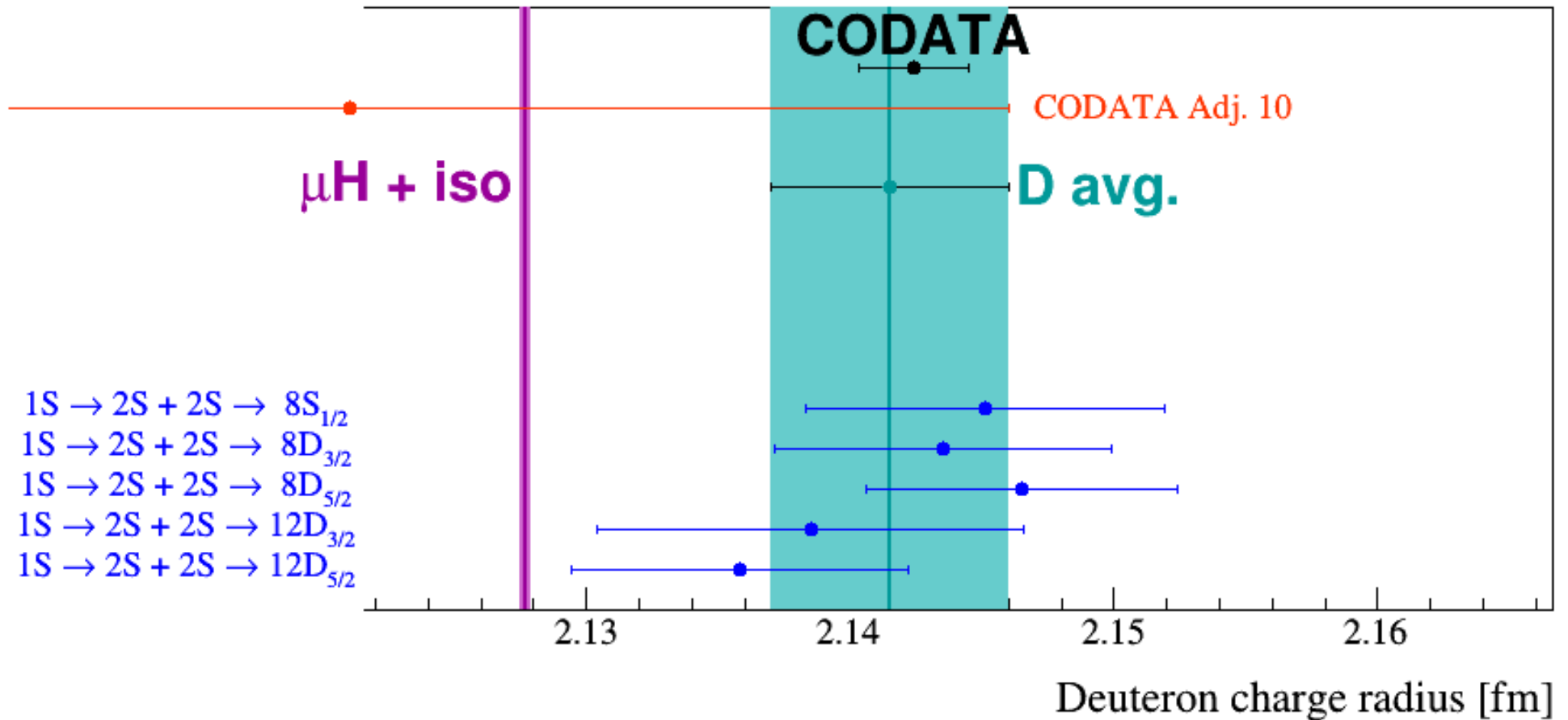
We give a pedagogical description of the method to extract the charge radii and Rydberg constant from laser spectroscopy in regular hydrogen (H) and deuterium (D) atoms, that is part of the CODATA least-squares adjustment (LSA) of the fundamental physical constants. We give a deuteron charge radius r_d from D spectroscopy alone of 2.1415(45) fm. This value is independent of the proton charge radius, and five times more accurate than the value found in the CODATA Adjustment 10.

arXiv 1607.03165

Related work:

* Horbatsch, Hessels, “Tabulation of bound-state energies of atomic hydrogen”, PRA 93, 022513 (2016) [1601.01057] (see Talk Wed.)

Rd from D spectroscopy



Summary

- $R_p = 0.8775(51)$ fm CODATA-2010
 - $0.8747(91)$ fm H(1S-2S) + 2S-nl (*) uncorrel.
 - $0.8780(108)$ fm H(1S-3S) + 2S-nl
 - $0.8764(89)$ fm CODATA Adj. 8
 - $0.8409(4)$ fm μ H 4.0 sigma
- $R_d = 2.1424(21)$ fm CODATA-2010
 - $2.1415(45)$ fm Deuterium only (*) uncorrel.
 - $2.1XXX(8)$ fm μ D → next talk