

Ⓐ Wave meter

↳ wavelength meter

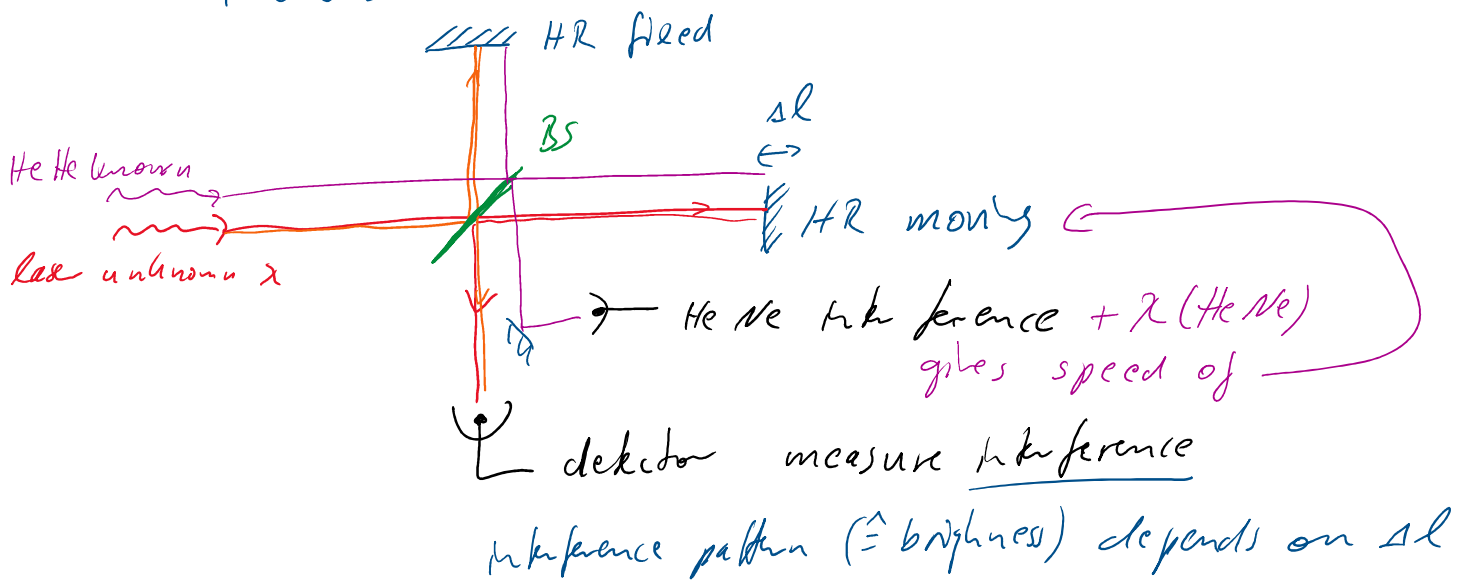
↳ wavelength $\lambda = \frac{\lambda_0}{n}$ is medium-dependent!

① Lambda meter

compare λ_{unknown} with a known λ ,

e.g. HeNe laser at 628nm

Michelson Interferometer



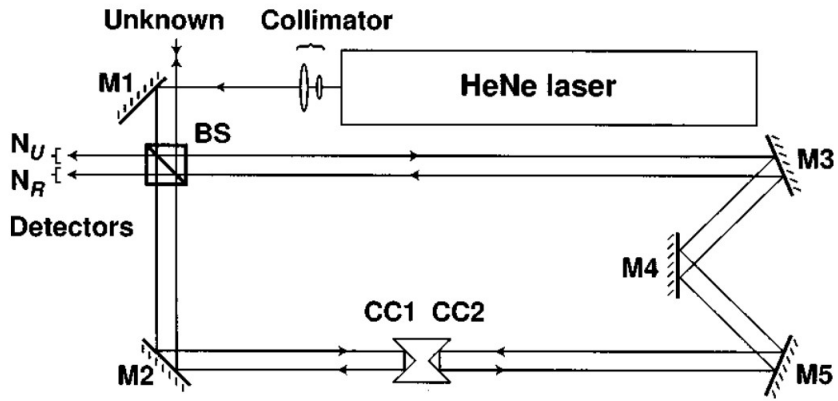
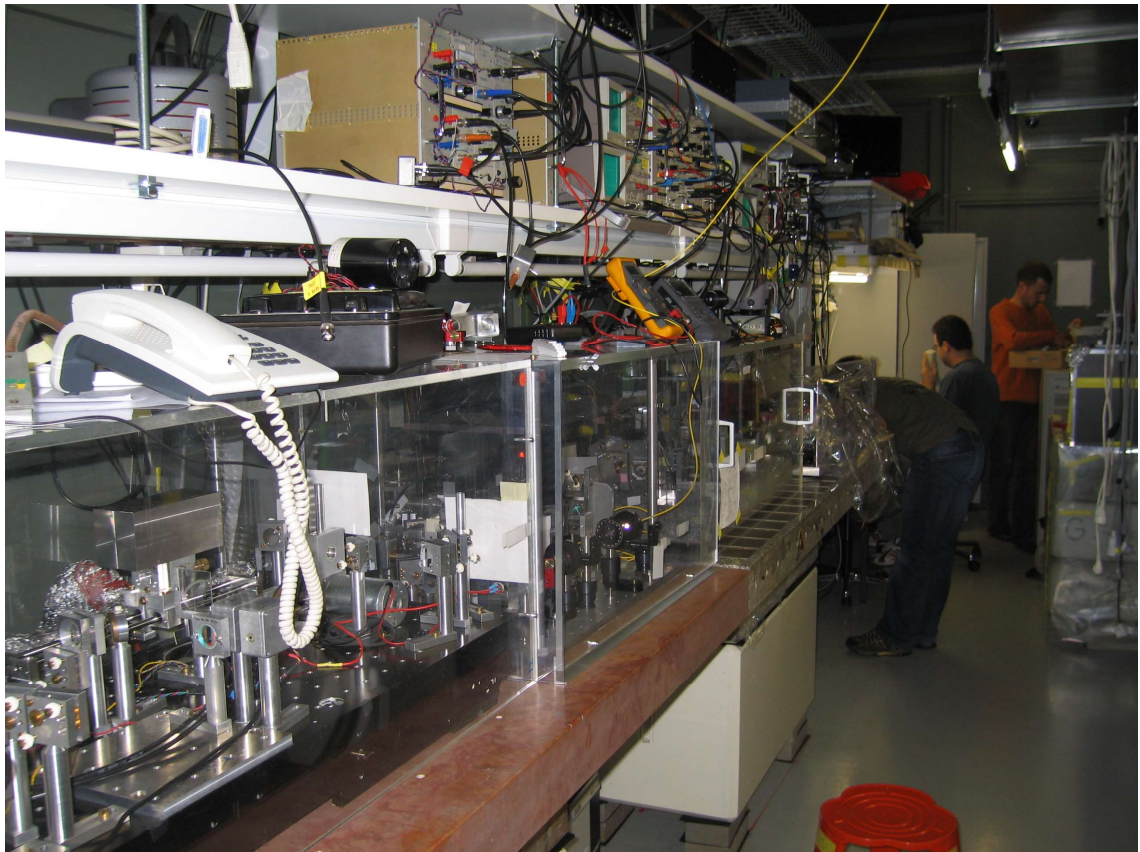
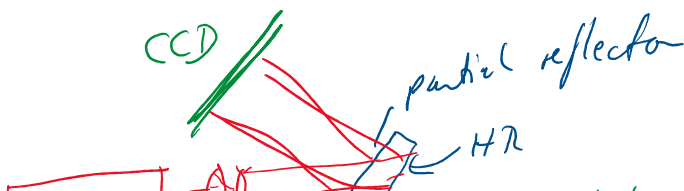


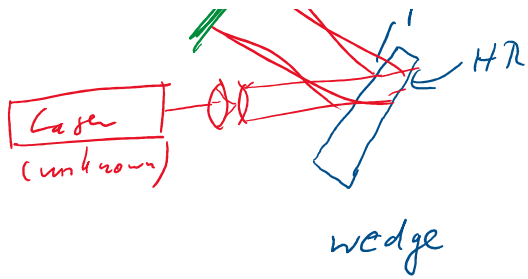
Fig. 2. Wavemeter layout. M1–M5: front-aluminized mirrors, BS: nonpolarizing beamsplitter, plano-convex collimator lenses ($f=4.5, 19$ mm), CC1,2: glass cornercube prisms. The arrows show the beam direction for the reference HeNe laser.

λ -meter



② Fizeau wave meter
 no moving parts!





interference between front & back side

fringes on CCD tell you the wavelength

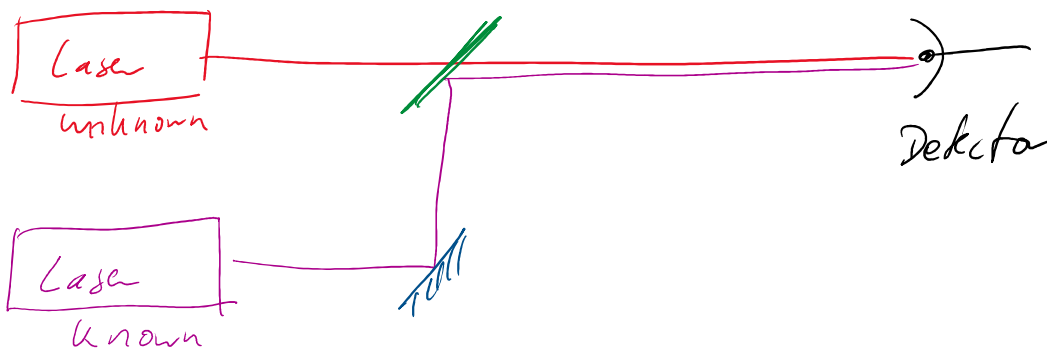
typ. more than one wedge

all these measure wavelength
 \Rightarrow "bad"

③ Art Schawlow: "Never measure anything but frequencies!"

BUT: "counting" frequencies works up to maybe 10 GHz
 certainly not 100s of THz (= optical frequencies)

Easy to measure: beat frequencies, also in the optical



intensity of 2 lasers superimposed on detector.

$$I \propto E_{\text{tot}}^2 \propto \left[E_u \cos(\omega_u t + \varphi) + E_k \cos(\omega_k t) \right]^2 \propto$$

$$\propto \frac{1}{2} E_u^2 + \frac{1}{2} E_k^2 \quad \leftarrow 2 \text{ DC signals}$$

$$+ 2 E_u E_k \cos(\omega_u t + \varphi) \cdot \cos(\omega_k t)$$

$$\cos A \cdot \cos B = \frac{1}{2} [\cos(A+B) + \cos(A-B)]$$

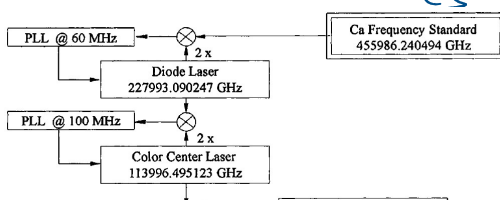
$$\propto \text{const} + E_u E_k \left\{ \cos[(\omega_u + \omega_k)t + \varphi] + \right. \\ \left. \cos[(\omega_u - \omega_k)t + \varphi] \right\}$$

ω_u and ω_k are too fast (100, of THz) to be counted, but

$\omega_u - \omega_k$ may be ≤ 10 GHz \rightarrow countable

"Bad old days": Frequency chain

connect H(1-2S) at 2500 THz to Cs at 9.2 GHz



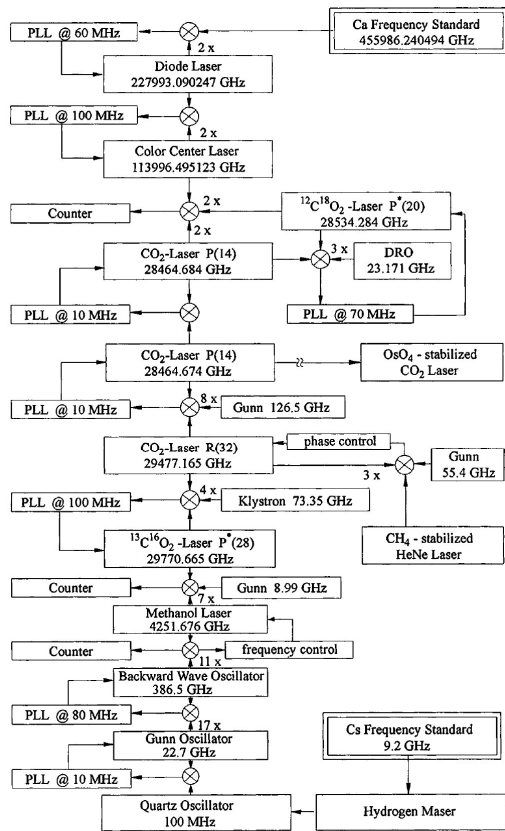
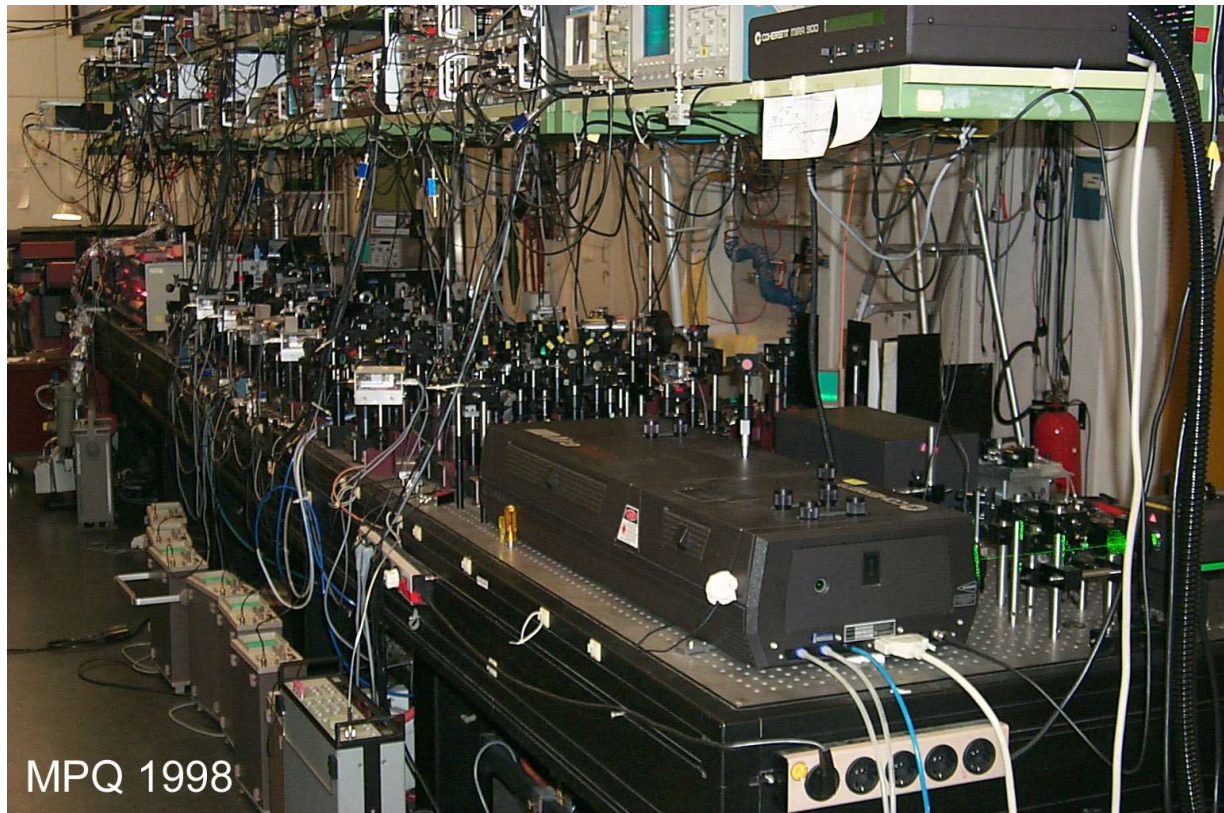
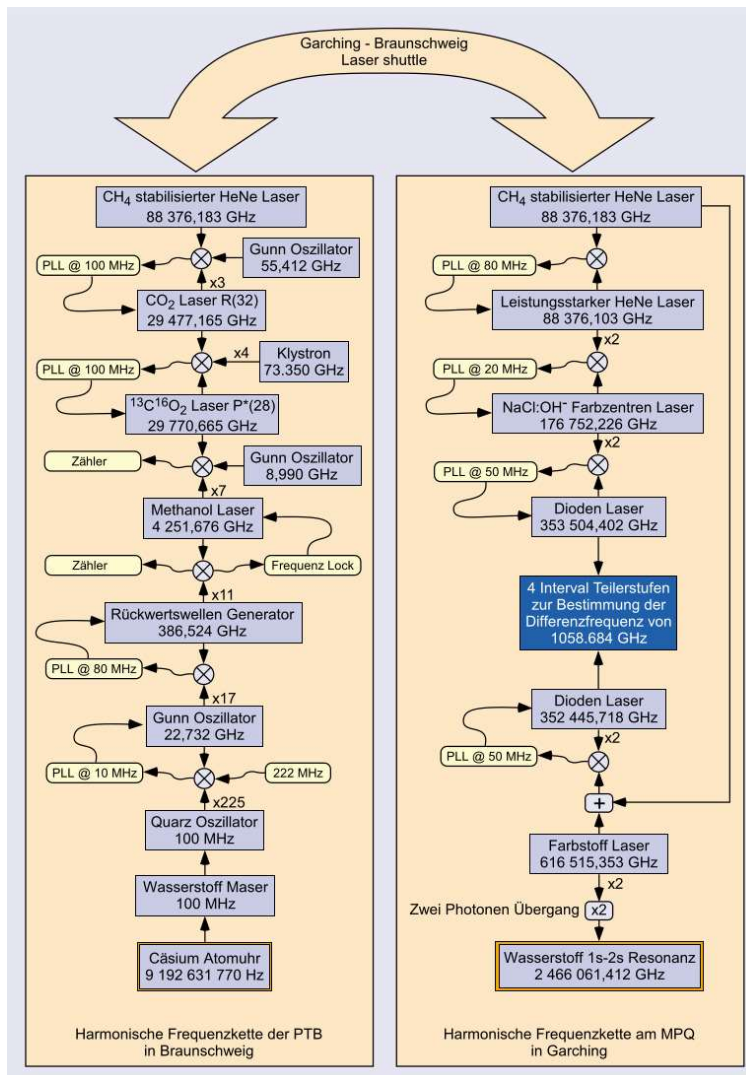


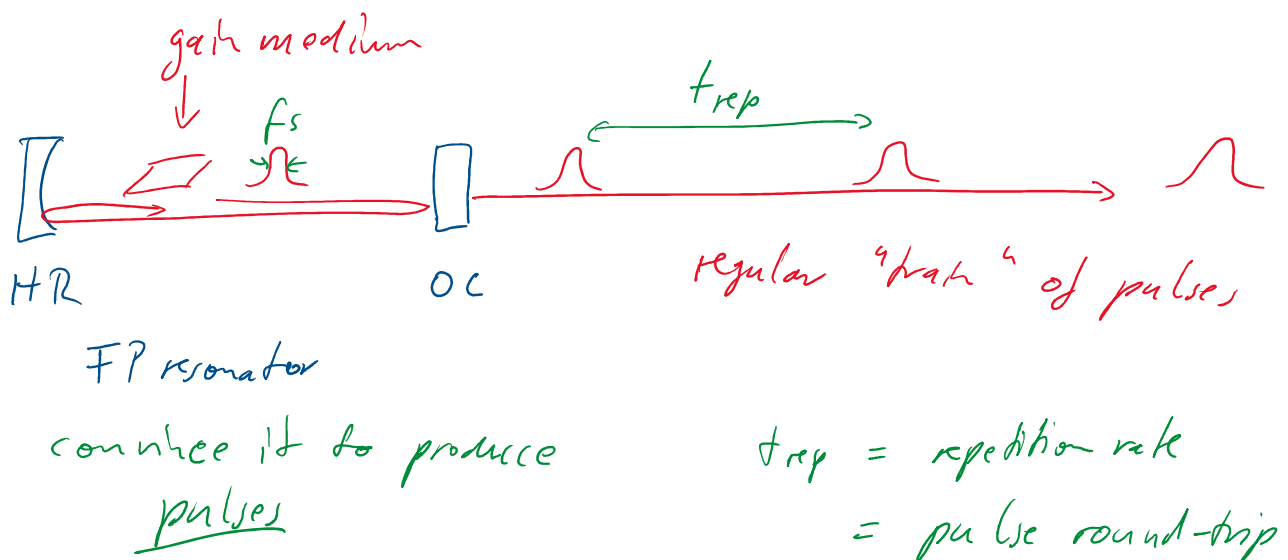
FIG. 1. PTB's frequency chain to the Ca intercombination line (PLL = phase locked loop, details are given in the text).





can only measure 1 frequency
different technology for each step

Solution: Frequency comb Hänsch 1999



pulses
fs-laser

= pulse round-trip
time

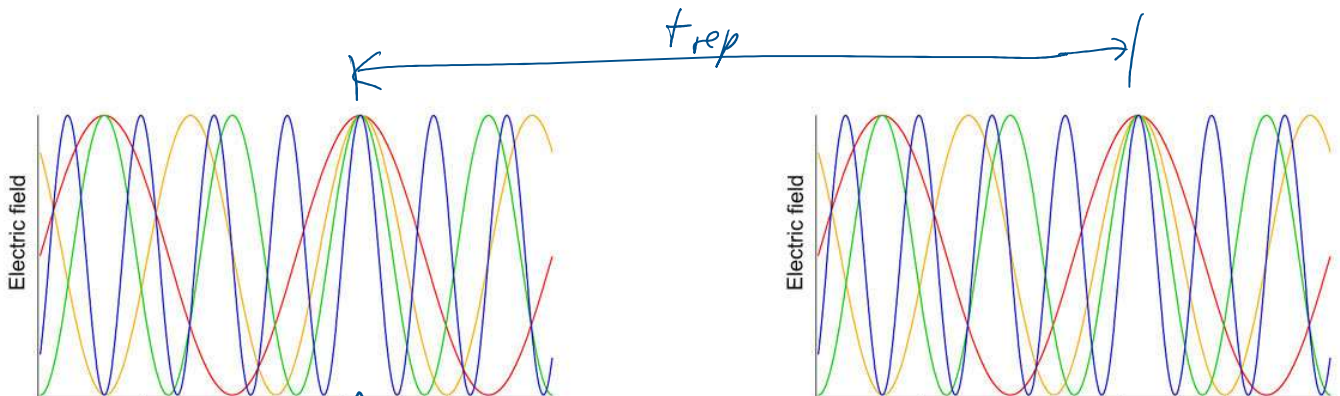
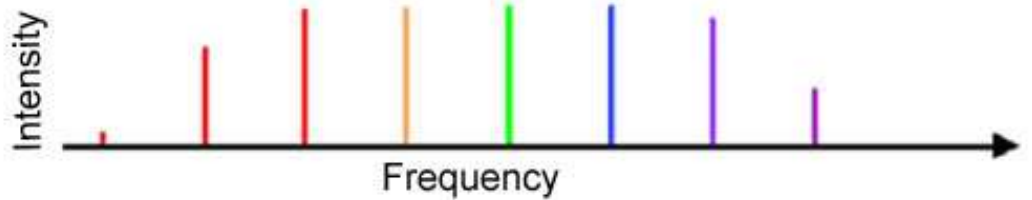
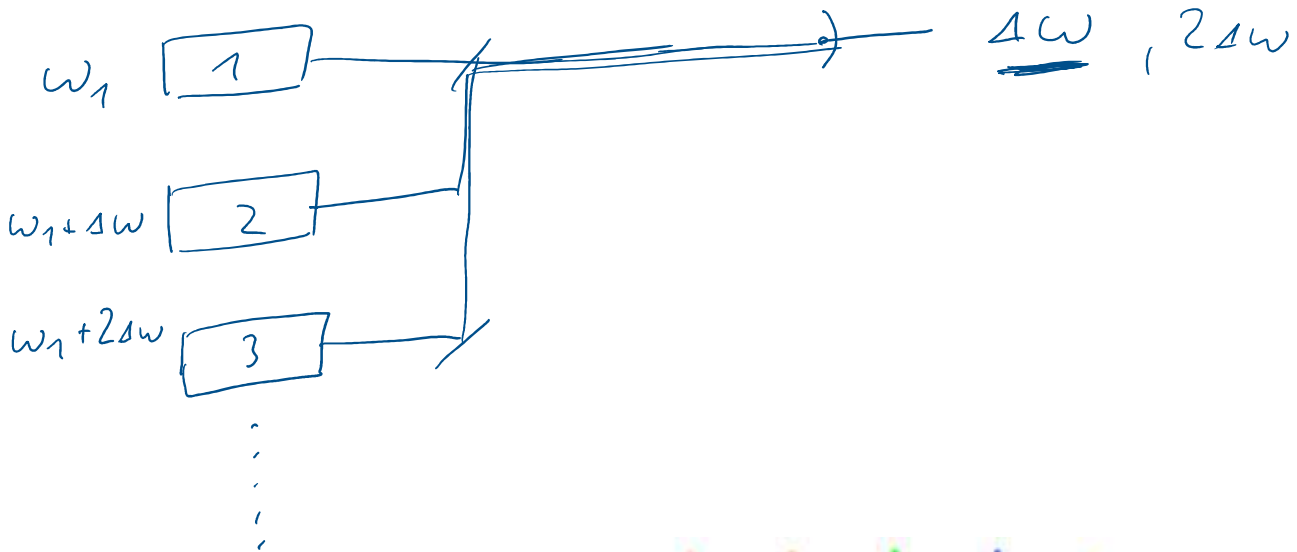
a regular "train" of pulses

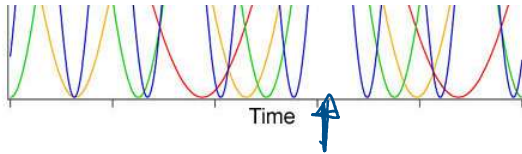
is THE SAME

as a superposition of many continuous waves
(cw)

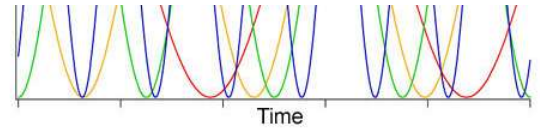
Let's combine several cw lasers

beat signals



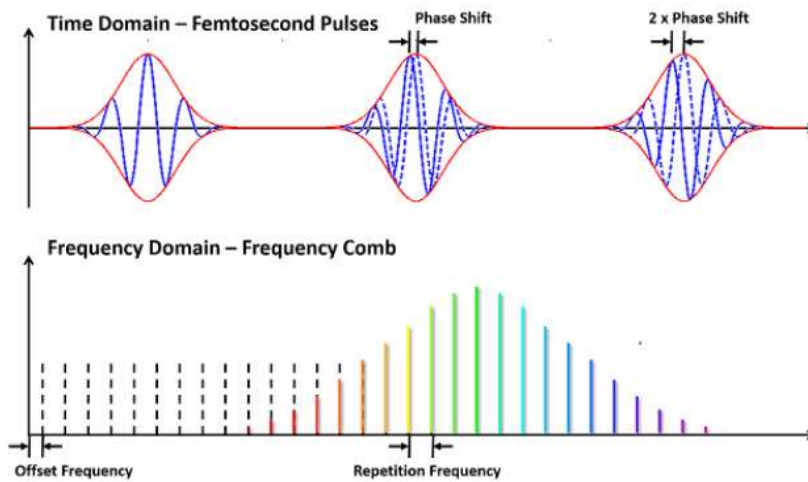


constructive interference



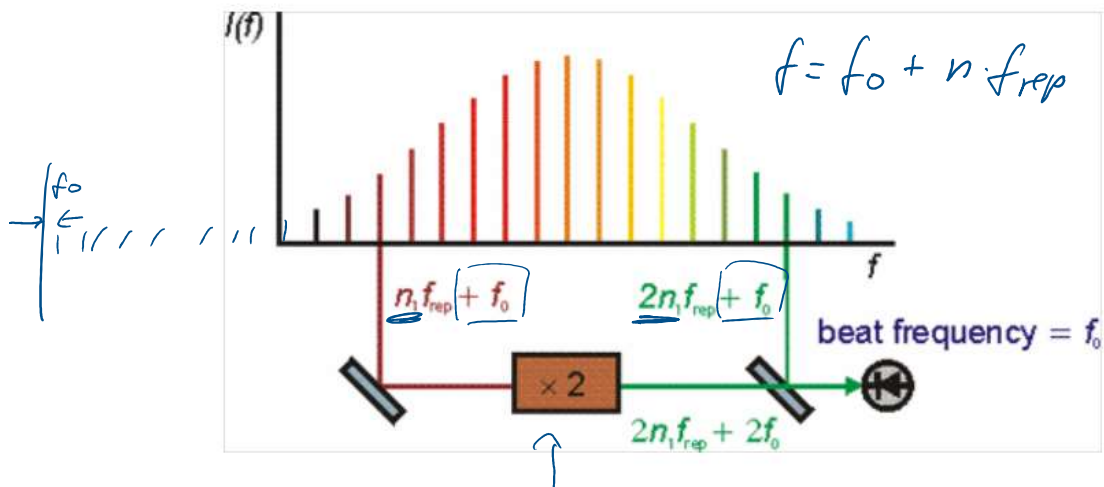
end pulse

Fourier transform



<https://www.laserfocusworld.com/articles/2015/03/cornell-cmos-compatible-mid-ir-optical-frequency-comb-fits-on-1-mm-chip.html>

Self-referenced comb



<http://www.npl.co.uk/science-technology/time-frequency/optical-frequency-standards-and-metrology/research/self-referencing-of-an-optical-frequency-comb>

f_{total}

$$E(t) = E_0 \cos(\omega t + \varphi)$$

↑
└───┬───┘ τ_{total}
└───┬───┘
└───┬───┘ $\varphi(t)$
↓
time-dependent phase